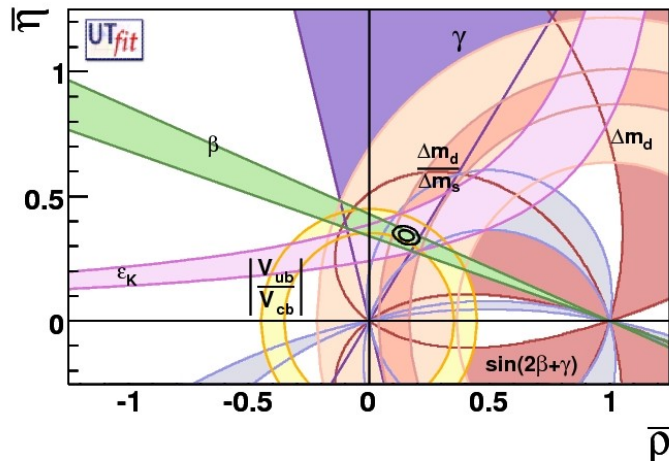
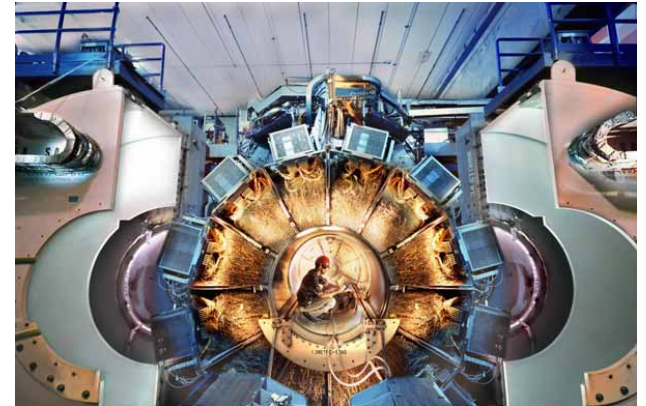


Flavour Physics and CP Violation



MARCELLA BONA



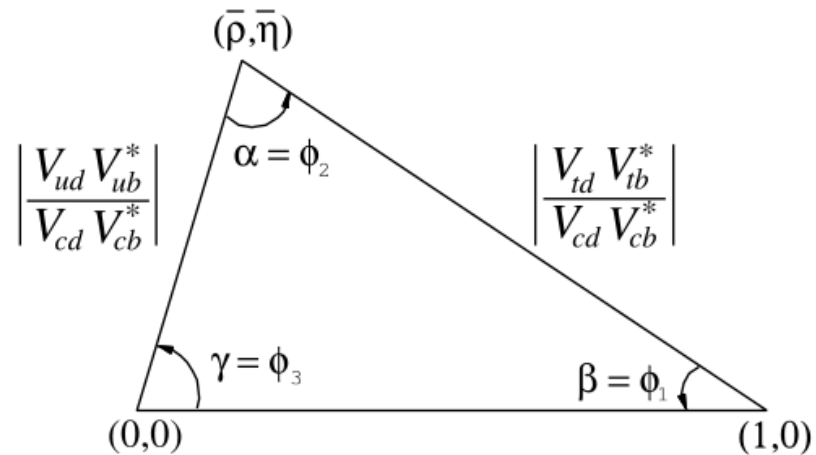
Post-FPCP 2018 Summer School

IIT Hyderabad, India

Lecture 3

Outline

- ◆ Short recap
- ◆ Angles of the unitarity triangle



The Unitarity Triangle [recap]

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

many observables
functions of $\bar{\rho}$ and $\bar{\eta}$:
overconstraining

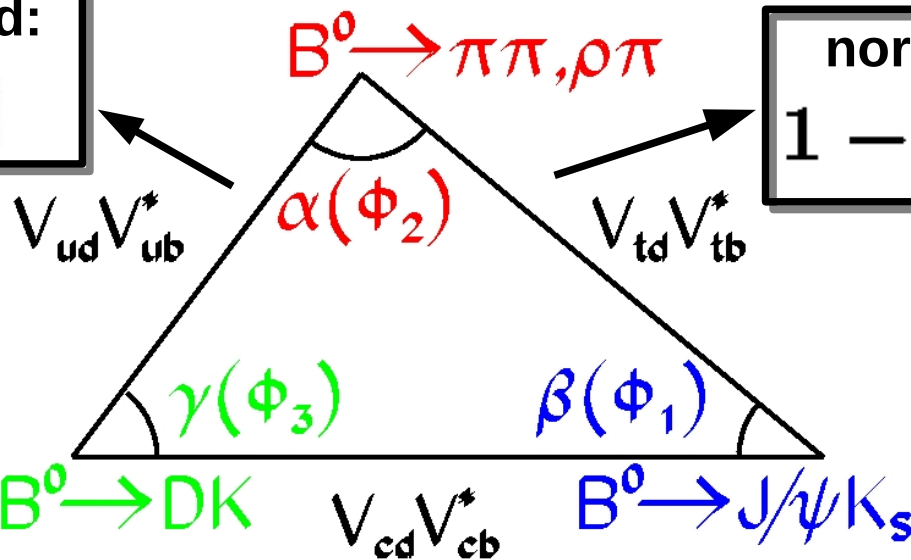
$$\alpha = \pi - \beta - \gamma$$

normalized:

$$\bar{\rho} + i\bar{\eta}$$

normalized:

$$1 - \bar{\rho} - i\bar{\eta}$$



$$\gamma = \text{atan} \left(\frac{\bar{\eta}}{\bar{\rho}} \right)$$

$$\beta = \text{atan} \left(\frac{\bar{\eta}}{(1 - \bar{\rho})} \right)$$

CPV Types for the B Meson System [recap]

⊙ Define the quantity λ :
$$\lambda_{f_{CP}} = \frac{q}{p} \cdot \frac{\bar{A}_{f_{CP}}}{A_{f_{CP}}}$$

1. Indirect CP violation, or CPV in the mixing:

$$|q/p| \neq 1$$

2. Direct CP violation, or CPV in the decays:

$$|\bar{A}/A| \neq 1$$

both neutral
and charged B

3. CP violation in interference between mixing and decay: $\text{Im}\lambda \neq 0$

neutral B

Time evolution and CP violation [recap]

- ⊙ If we consider that both B^0 and \bar{B}^0 can decay to the same final state and considering here a final state that is a CP eigenstate, then the time evolution of the physical system becomes:

$$f(B_{phys}^0 \rightarrow f_{CP}, \Delta t) = \frac{\Gamma}{4} e^{-\Gamma|\Delta t|} [1 - S_{f_{CP}} \sin(\Delta m_d \Delta t) + C_{f_{CP}} \cos(\Delta m_d \Delta t)]$$

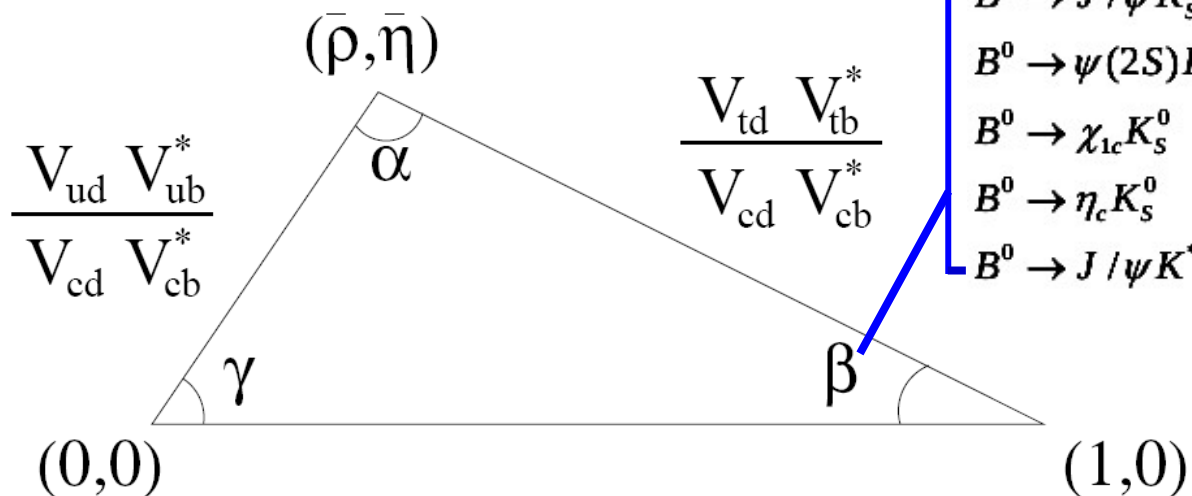
$$f(\bar{B}_{phys}^0 \rightarrow f_{CP}, \Delta t) = \frac{\Gamma}{4} e^{-\Gamma|\Delta t|} [1 + S_{f_{CP}} \sin(\Delta m_d \Delta t) - C_{f_{CP}} \cos(\Delta m_d \Delta t)]$$

- ⊙ direct CP violation $C \neq 0$ $C_f (= -A_f) = \frac{1 - |\lambda_{f_{CP}}|^2}{1 + |\lambda_{f_{CP}}|^2}$
- ⊙ CP violation in interference $S \neq 0$ $S_f = \frac{2 \text{Im} \lambda_{f_{CP}}}{1 + |\lambda_{f_{CP}}|^2}$

β/ϕ_1 angle

Theoretically cleaner (SM uncertainties $\sim 10^{-2}$ to 10^{-3})
 → tree dominated decays to Charmonium + K^0 final states.

$$\beta \equiv \arg \left[-V_{cd} V_{cb}^* / V_{td} V_{tb}^* \right]$$

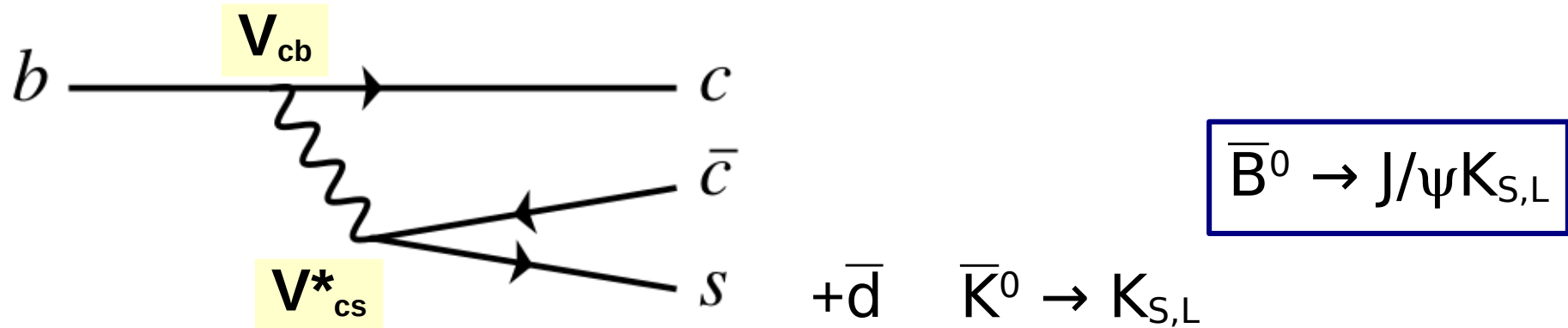


- $b \rightarrow c\bar{c}s$
- $B^0 \rightarrow J/\psi K_L^0$
- $B^0 \rightarrow J/\psi K_S^0$
- $B^0 \rightarrow \psi(2S)K_S^0$
- $B^0 \rightarrow \chi_{1c} K_S^0$
- $B^0 \rightarrow \eta_c K_S^0$
- $B^0 \rightarrow J/\psi K^{*0}$
- $B \rightarrow J/\psi \pi^0$
- $B \rightarrow D^{(*)+} D^{(*)-}$
- $B \rightarrow \eta' K^0$
- $B \rightarrow \rho K^0$
- $B \rightarrow \omega K^0$
- $B \rightarrow \pi^0 K^0$
- $B \rightarrow \phi K^{(*)0}$
- $B \rightarrow KKK^0$
- $B \rightarrow f^0(980)K^0$

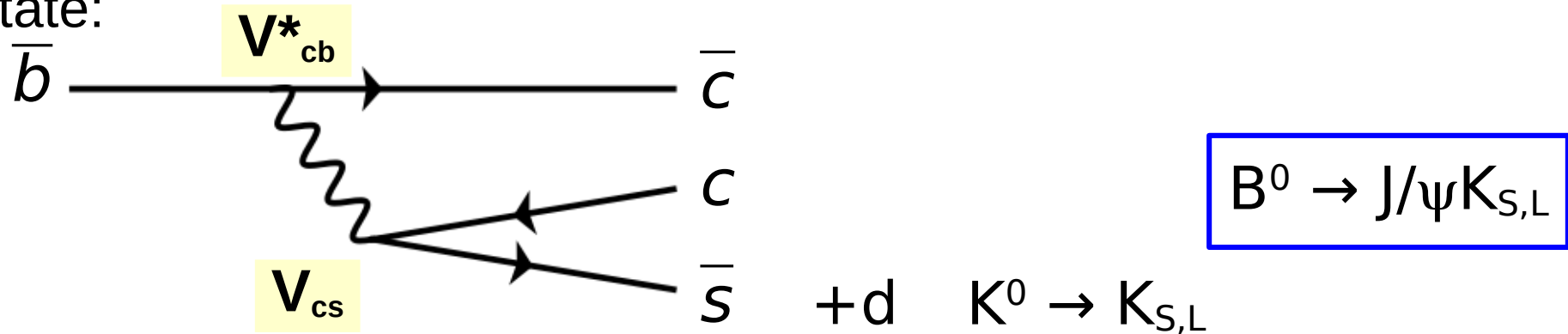
$$\beta \equiv \arg[-V_{cd}V_{cb}^*/V_{td}V_{tb}^*]$$

$\sin 2\beta$ in golden $b \rightarrow \bar{c}\bar{s}$ modes

leading-order tree decays to $\bar{c}\bar{s}$ final states



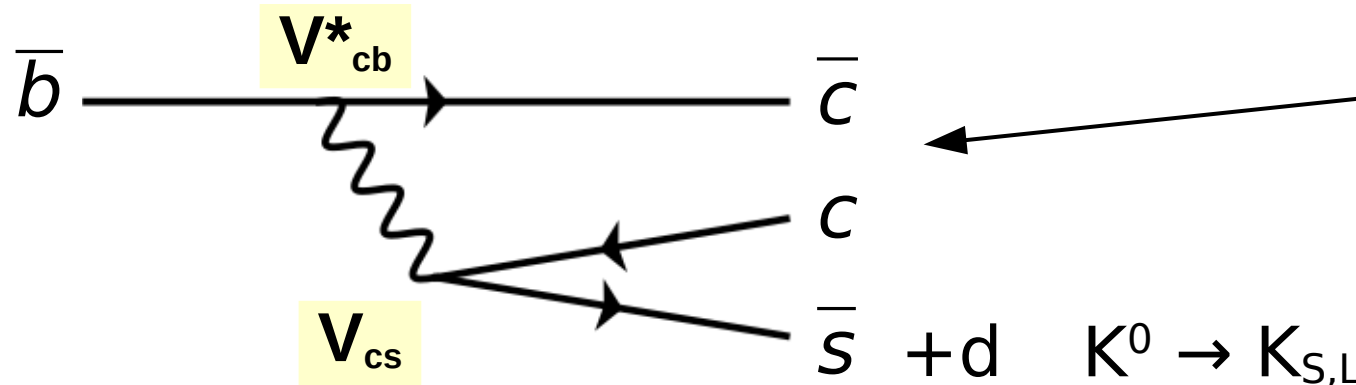
here the CKM elements contributing are $V_{cb}V_{cs}^*$ that in our Wolfenstein CKM parameterisation have no phase. The CP conjugated case is also leading to (about) the same final state:



$$\beta \equiv \arg[-V_{cd}V_{cb}^*/V_{td}V_{tb}^*]$$

sin2β in golden b → c̄cs modes

leading-order tree decays to c̄cs final states



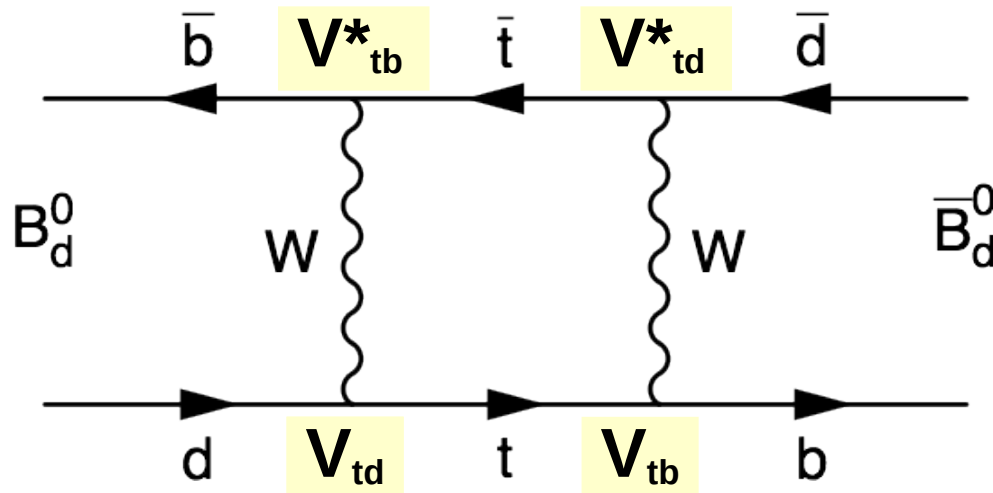
$$B^0 \rightarrow J/\psi K_{S,L}$$

tree diagram

$$\frac{\bar{A}}{A} = \frac{V_{cb}V_{cs}^*}{V_{cb}^*V_{cs}} \frac{V_{cs}V_{cd}^*}{V_{cs}^*V_{cd}}$$

K mixing

because both B and B̄ can decay in this common final state, this can interfere with the oscillation diagram:



$$\lambda = \frac{q A(\bar{B} \rightarrow f)}{p A(B \rightarrow f)} = \frac{V_{td}^* V_{tb}}{V_{td} V_{tb}^*} \frac{\bar{A}}{A} \sim e^{-i2\beta} \frac{\bar{A}}{A}$$

$$\beta \equiv \arg[-V_{cd}V_{cb}^*/V_{td}V_{tb}^*]$$

sin2β in golden b → c \bar{c} s modes

$$B^0 \rightarrow J/\psi K_{S,L}$$

no possibility to generate this way direct or indirect CPV

$$\lambda_{CP} = \eta_{CP} \frac{q}{p} \frac{\bar{A}}{A} = \eta_{CP} \underbrace{\frac{V_{td}V_{tb}^*}{V_{tb}^*V_{td}} \frac{V_{cb}V_{cd}^*}{V_{cd}^*V_{cb}}}_{e^{-i2\beta}}$$

$$|\lambda_{CP}| = 1$$

$$\hookrightarrow C_{f_{CP}} = 0$$

$$\text{Im } \lambda_{CP} = -\eta_{CP} \sin 2\beta$$

$$\hookrightarrow S_{f_{CP}} = -\eta_{CP} \sin 2\beta$$

$$\left\{ \begin{array}{l} J/\psi (c\bar{c}) \rightarrow J^{PC} = 1^{--} \\ K_S \sim K_1 \rightarrow \eta_{CP} = +1 \\ L=1 \rightarrow P = (-1)^L \end{array} \right.$$

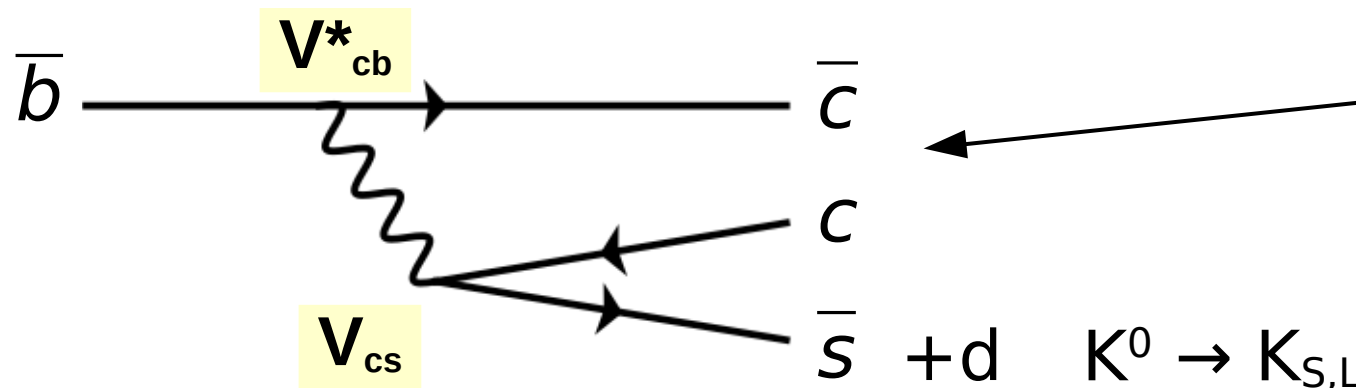
$$\eta_{CP}(J/\psi K_S) = -1$$

$$\eta_{CP}(J/\psi K_L) = +1$$

CPV in interference between mixing and decay

Why $J/\psi K_{S,L}$ mode is golden

leading-order tree decays to $c\bar{c}s$ final states



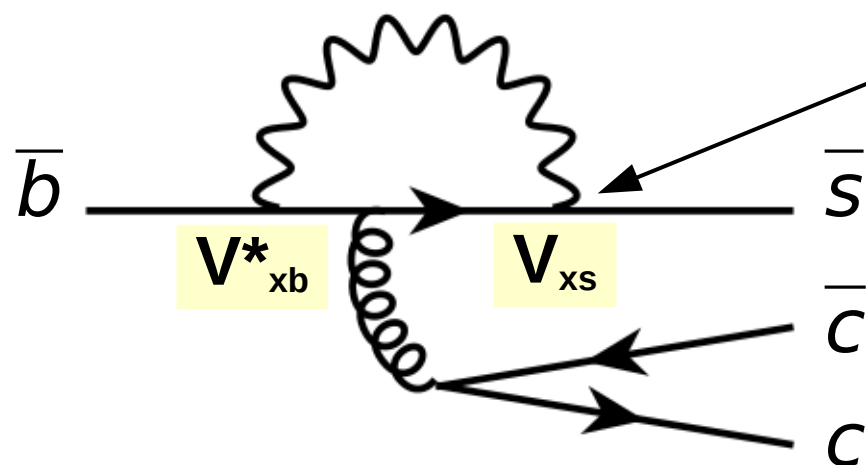
$$B^0 \rightarrow J/\psi K_{S,L}$$

tree diagram

$$\frac{\bar{A}}{A} = \frac{V_{cb}V_{cs}^*}{V_{cb}^*V_{cs}} \frac{V_{cs}V_{cd}^*}{V_{cs}^*V_{cd}}$$

K mixing

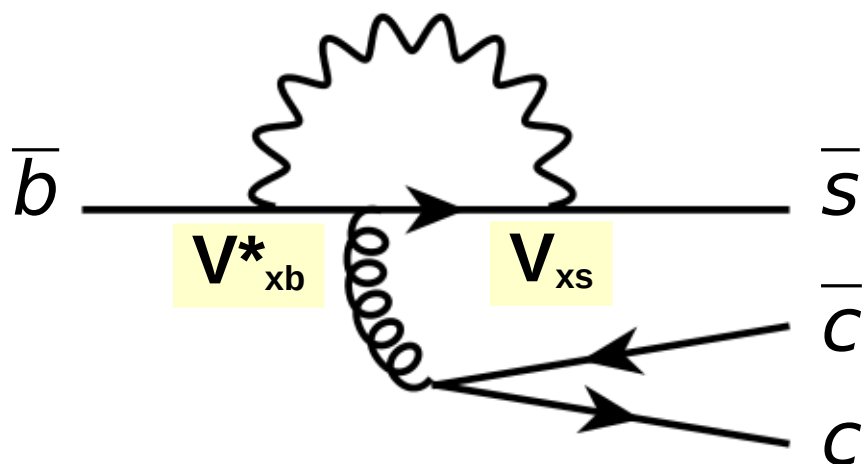
possible penguin contributions:



where x can be any up-type quark hence this counts for three penguin diagrams

can this be a problem?

Why $J/\psi K_{S,L}$ mode is golden



$$\begin{cases} x=u \rightarrow P^u \sim V_{ub}V_{us}^* \\ x=c \rightarrow P^c \sim V_{cb}V_{cs}^* \\ x=t \rightarrow P^t \sim V_{tb}V_{ts}^* \end{cases}$$

using this unitary condition ($2^{\text{nd}} \rightleftharpoons 3^{\text{rd}}$ family), we eliminate $V_{tb}V_{ts}^*$

$$V_{ub}V_{us}^* + V_{cb}V_{cs}^* + V_{tb}V_{ts}^* = 0 \quad \rightarrow \quad V_{tb}V_{ts}^* = -V_{ub}V_{us}^* - V_{cb}V_{cs}^*$$

thus the amplitude is:

$$A_{\text{ccs}} \sim \underbrace{V_{cb}V_{cs}^*}_{\mathcal{O}(\lambda^2)} (T + P^c - P^t) + \underbrace{V_{ub}V_{us}^*}_{\mathcal{O}(\lambda^4)} (P^u - P^t)$$

CKM-suppressed
pollution by penguins

$$\beta \equiv \arg[-V_{cd}V_{cb}^*/V_{td}V_{tb}^*]$$

sin2β in golden b → ccs modes

⊙ branching fraction: $O(10^{-3})$

the colour-suppressed tree dominates

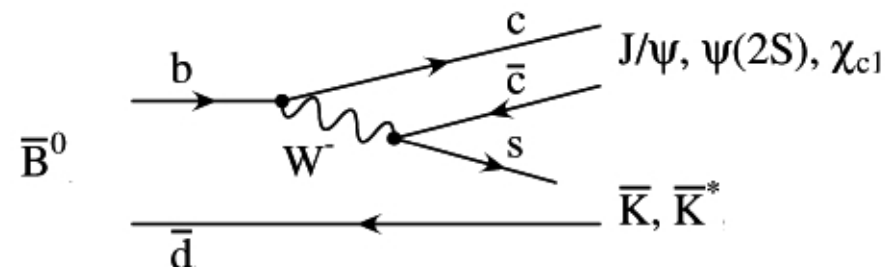
and the penguin pollution has

the same weak phase of the tree or is CKM suppressed

$$\odot A_{CP}(t) = \frac{\Gamma(\bar{B}^0(t) \rightarrow f_{CP}) - \Gamma(B^0(t) \rightarrow f_{CP})}{\Gamma(\bar{B}^0(t) \rightarrow f_{CP}) + \Gamma(B^0(t) \rightarrow f_{CP})}$$

$$S \sim \sin 2\beta$$

$$C \sim 0$$



⊙ theoretical uncertainty:

⊙ model-independent data-driven estimation from $J/\psi\pi^0$ data:

$$\Delta S_{J/\psi K^0} = S_{J/\psi K^0} - \sin 2\beta = -0.01 \pm 0.01$$

M.Ciuchini et al.
arXiv:1102.0392 [hep-ph].

⊙ model-dependent estimates of the u- and c- penguin biases

$$\Delta S_{J/\psi K^0} = S_{J/\psi K^0} - \sin 2\beta \sim O(10^{-3})$$

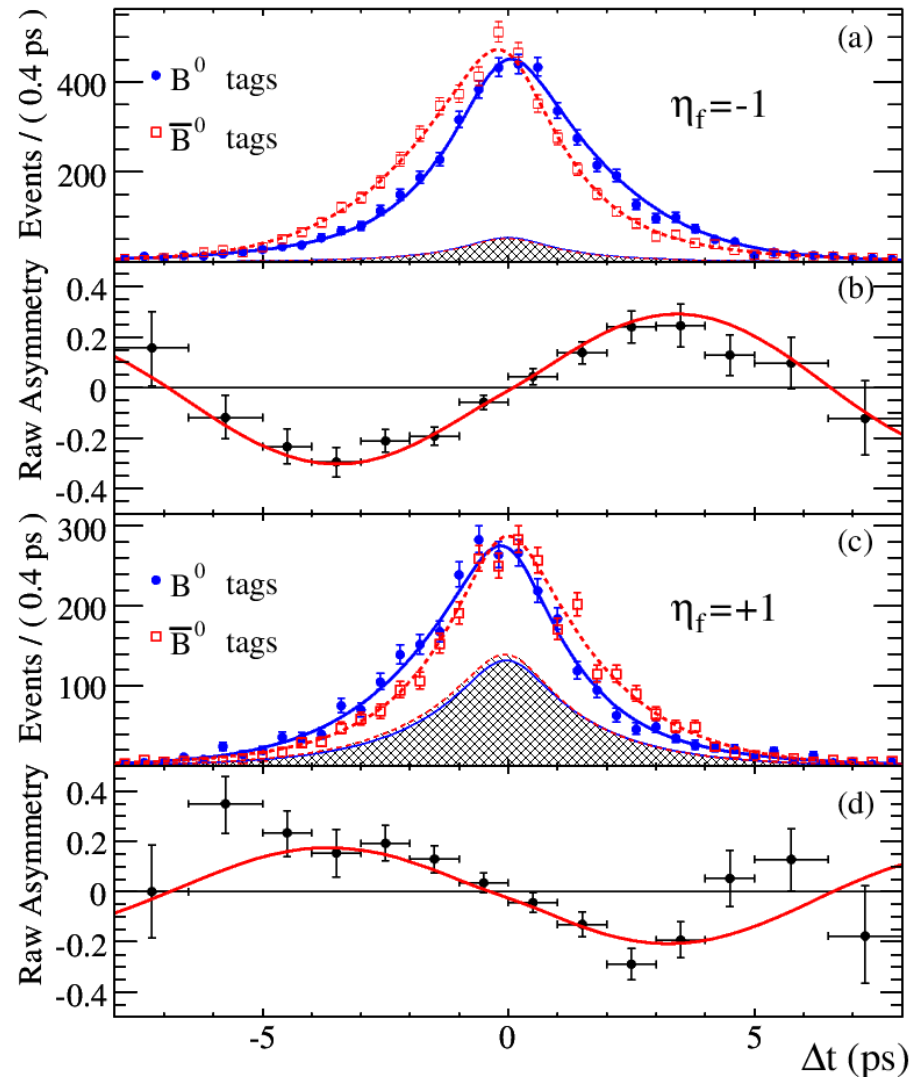
H.Li, S.Mishima
JHEP 0703:009 (2007)

$$\Delta S_{J/\psi K^0} = S_{J/\psi K^0} - \sin 2\beta \sim O(10^{-4})$$

H.Boos et al.
Phys. Rev. D73, 036006 (2006)

$$\beta \equiv \arg[-V_{cd}V_{cb}^*/V_{td}V_{tb}^*]$$

sin2 β in golden $b \rightarrow \bar{c}cs$ modes



$$A_{CP}(t) = S \sin(\Delta m_d \Delta t) - C \cos(\Delta m_d \Delta t)$$

Sine term has a non-zero coefficient and this tells us that there is CP violation in the interference between mixing and decay amplitudes in $\bar{c}cs$ decays.

Heavy FLavour AVeraging (HFLAV) group for $J/\psi K_{S,L}$

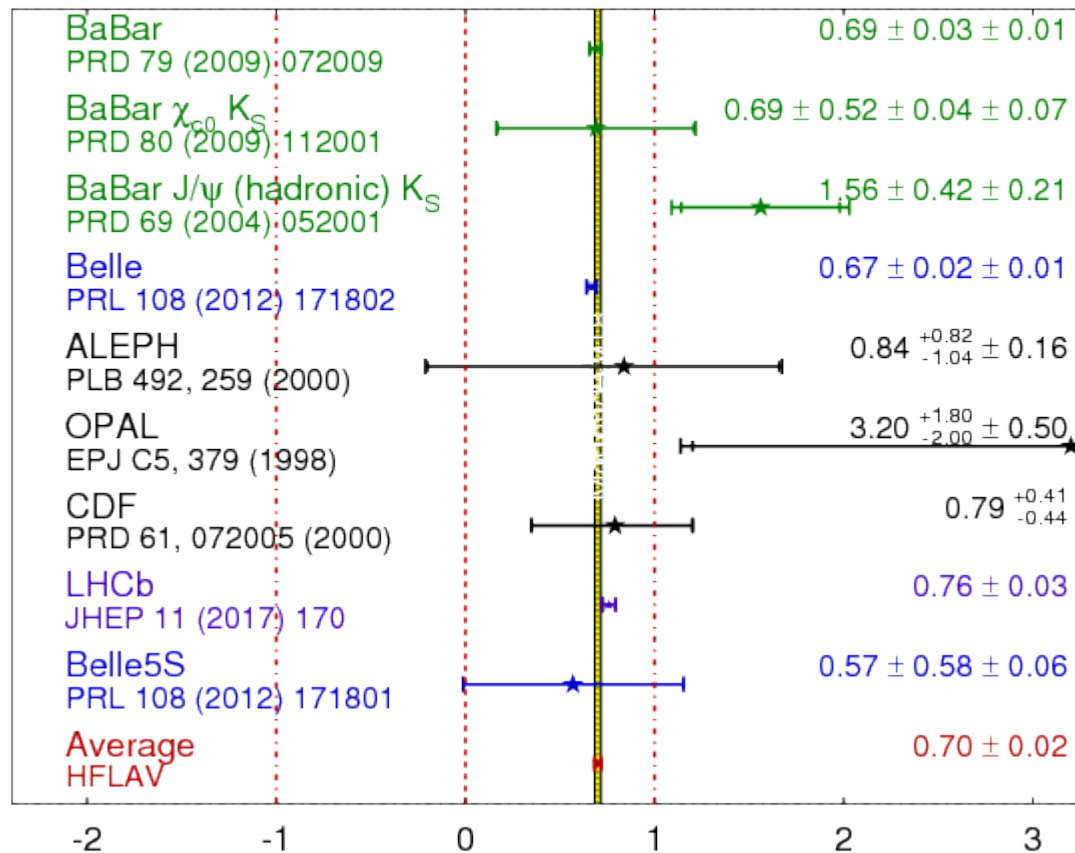
$$S = \sin 2\beta = 0.690 \pm 0.018$$

$$\beta \equiv \arg[-V_{cd}V_{cb}^*/V_{td}V_{tb}^*]$$

$\sin 2\beta$ in $b \rightarrow \bar{c}cs$ modes

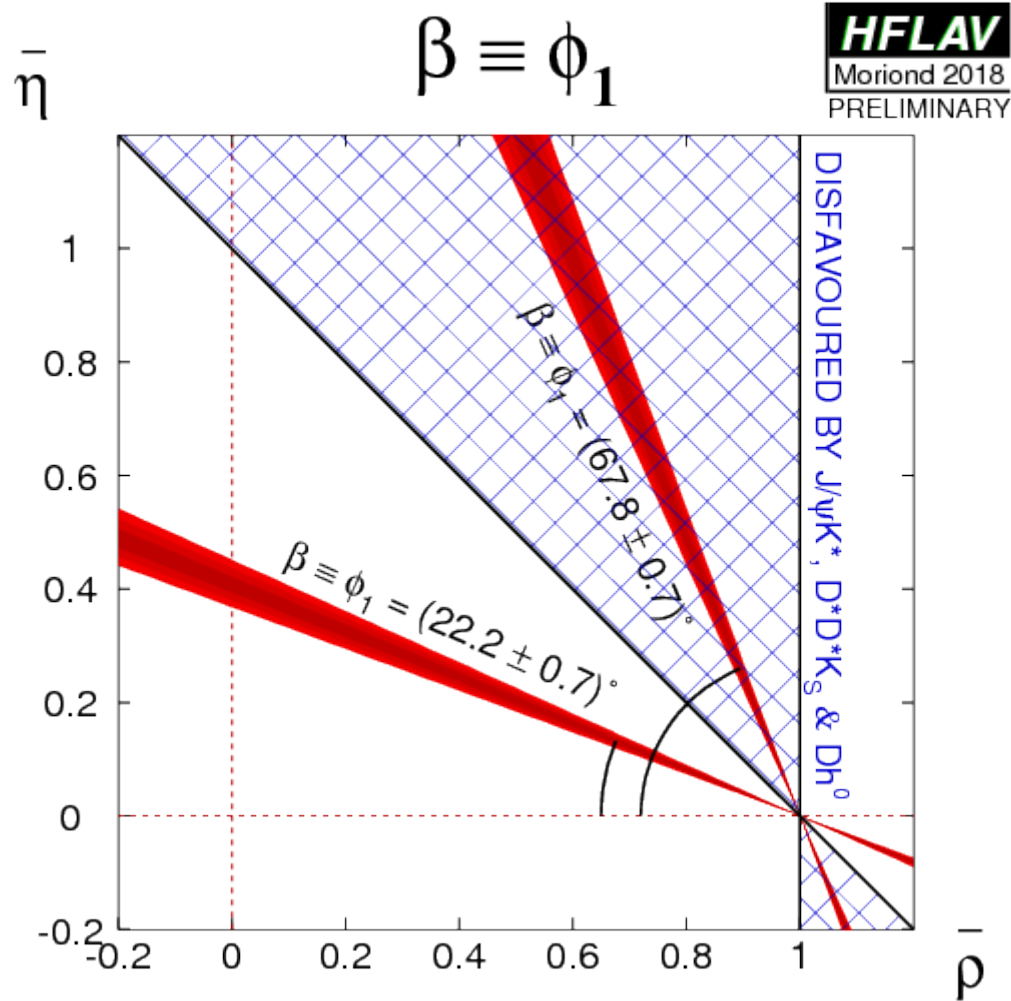
$$\sin(2\beta) \equiv \sin(2\phi_1)$$

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$$\beta \equiv \arg[-V_{cd}V_{cb}^*/V_{td}V_{tb}^*]$$

angle β in $b \rightarrow \bar{c}\bar{c}s$ modes



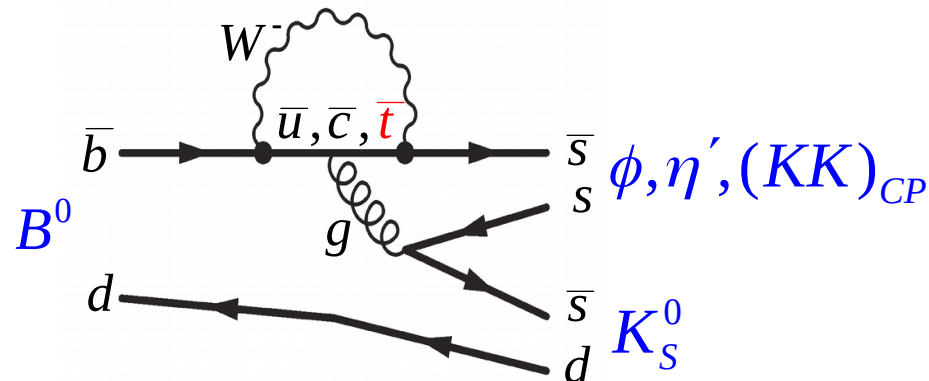
Searching for new physics via other $b \rightarrow c\bar{c}s$ modes

⊙ $\sin 2\beta$ has been measured to $O(1^\circ)$ accuracy in $b \rightarrow c\bar{c}s$ decays.

⊙ Can use this to search for signs of New Physics (NP) if:

- Identify a rare decay sensitive to $\sin 2\beta$ (loop dominated process).
- Measure S precisely in that mode (S_{eff}).
- Control the theoretical uncertainty on the Standard Model 'pollution' (ΔS_{SM}).
- Compute $\Delta S_{\text{NP}} = S_{\text{eff}} - S_{c\bar{c}s} - \Delta S_{\text{SM}}$

⊙ In the presence of NP: $\Delta S_{\text{NP}} \neq 0$



- ▶ New heavy particles can introduce new amplitudes affecting physical observables of loop dominated processes.
- ▶ Observables affected include branching fractions, CP asymmetries, forward backward asymmetries.. etc..
- ▶ The Standard Model contributions need to be understood

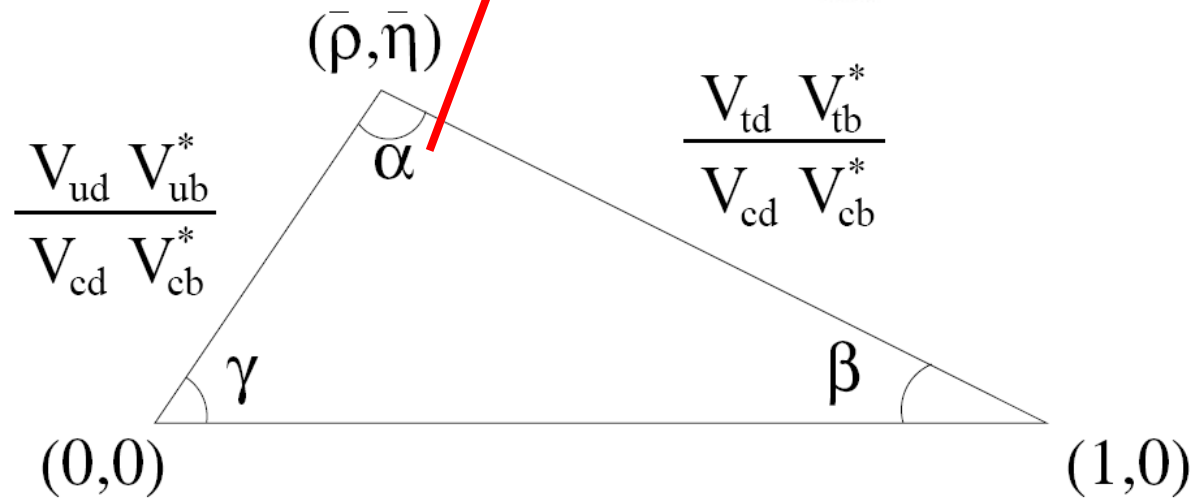
α/ϕ_2 angle

$$\alpha \equiv \arg \left[-V_{td} V_{tb}^* / V_{ud} V_{ub}^* \right]$$

$b \rightarrow u\bar{u}d$ transitions with possible loop contributions. Extract α using

- SU(2) Isospin relations.
- SU(3) flavour related processes.

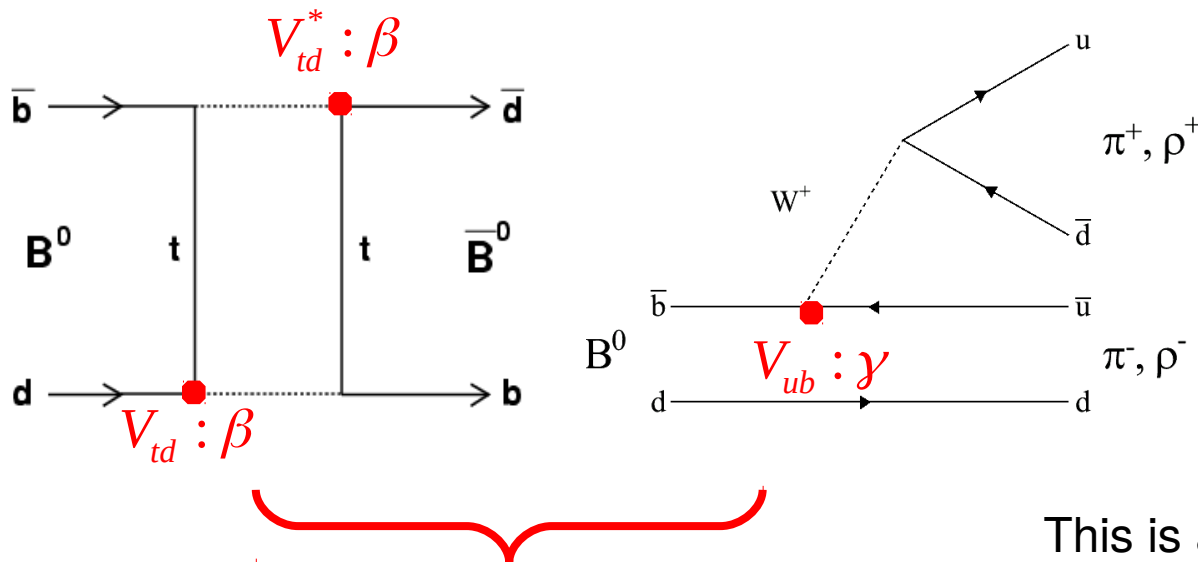
- $b \rightarrow u\bar{u}d$
- $B \rightarrow \pi\pi$
- $B \rightarrow \rho\pi$
- $B \rightarrow \rho\rho$
- $B \rightarrow a_1\pi$
- $B \rightarrow a_1\rho$
- $B \rightarrow b_1\pi$
- $B \rightarrow b_1\rho$
- $B \rightarrow a_1a_1$



$$\alpha \equiv \arg[-V_{td}V_{tb}^*/V_{ud}V_{ub}^*]$$

CP violation: α

- ⊙ Interference between box and tree results in an asymmetry that is sensitive to α in $B \rightarrow hh$ decays: $h = \pi, \rho, \dots$



$$C_{hh} = 0$$

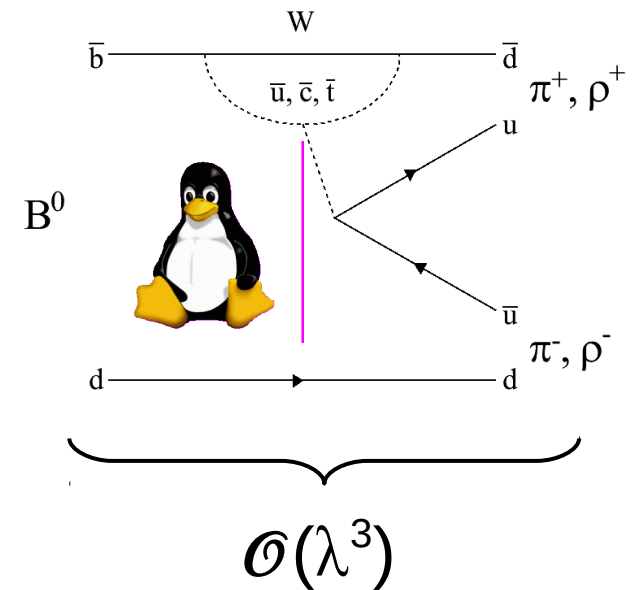
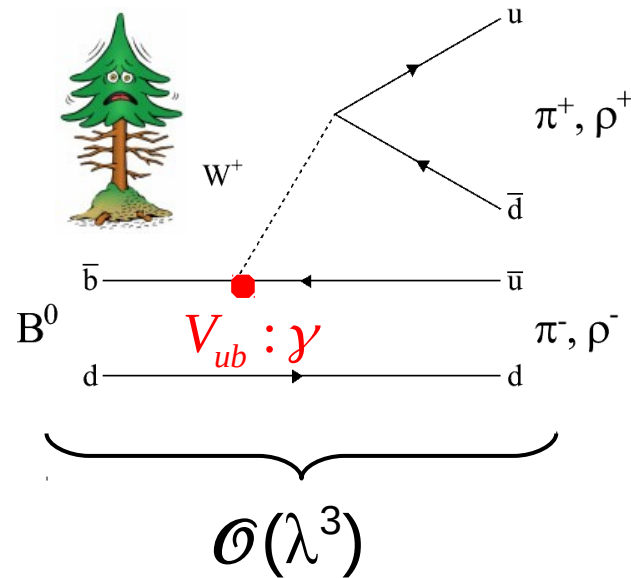
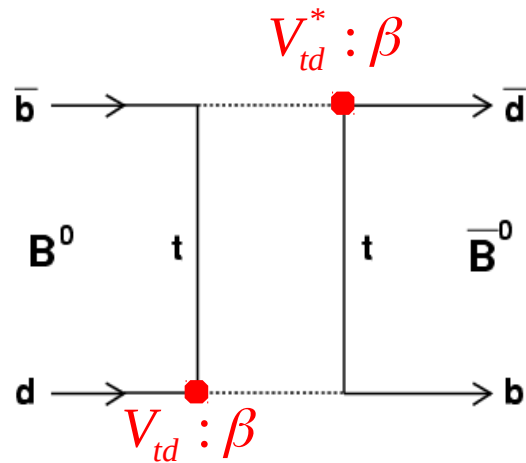
$$S_{hh} = \sin(2\alpha)$$

This is again a case of interference between mixing and decay. This scenario is equivalent to the measurement of $\sin 2\beta$ in Charmonium decays ... but in this case it is more complicated..

$$\alpha \equiv \arg[-V_{td}V_{tb}^*/V_{ud}V_{ub}^*]$$

CP violation: α

- Interference between box and tree results in an asymmetry that is sensitive to α in $B \rightarrow hh$ decays: $h = \pi, \rho, \dots$

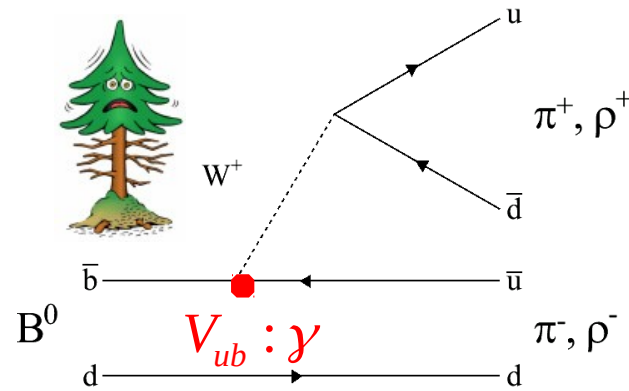
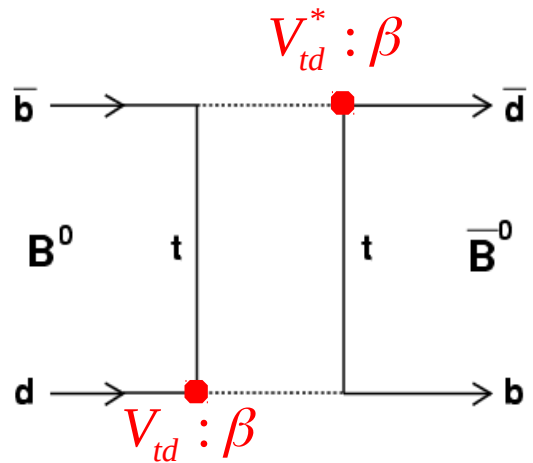


In this case the penguin diagram is not CKM suppressed so it spoils the clean measurement of the CP violation effect

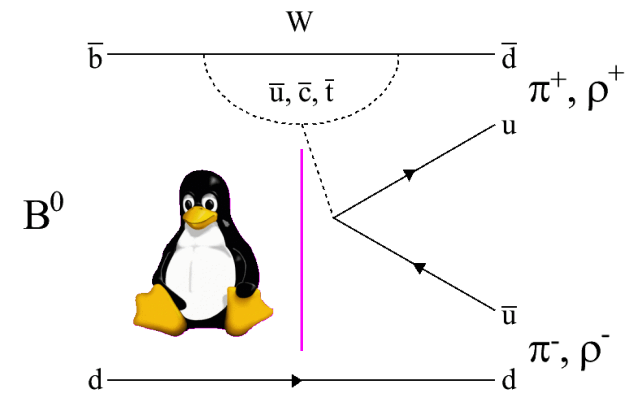
$$\alpha \equiv \arg[-V_{td}V_{tb}^*/V_{ud}V_{ub}^*]$$

CP violation: α

- Interference between box and tree results in an asymmetry that is sensitive to α in $B \rightarrow hh$ decays: $h = \pi, \rho, \dots$

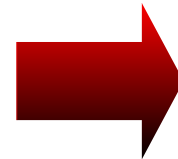


+ Loops (penguins)



$$C_{hh} = 0$$

$$S_{hh} = \sin(2\alpha)$$



$$C_{hh} \propto \sin(\delta)$$

$$S_{hh} = \sqrt{1 - C_{hh}^2} \sin(2\alpha_{\text{eff}})$$

$$\delta = \delta_P - \delta_T$$

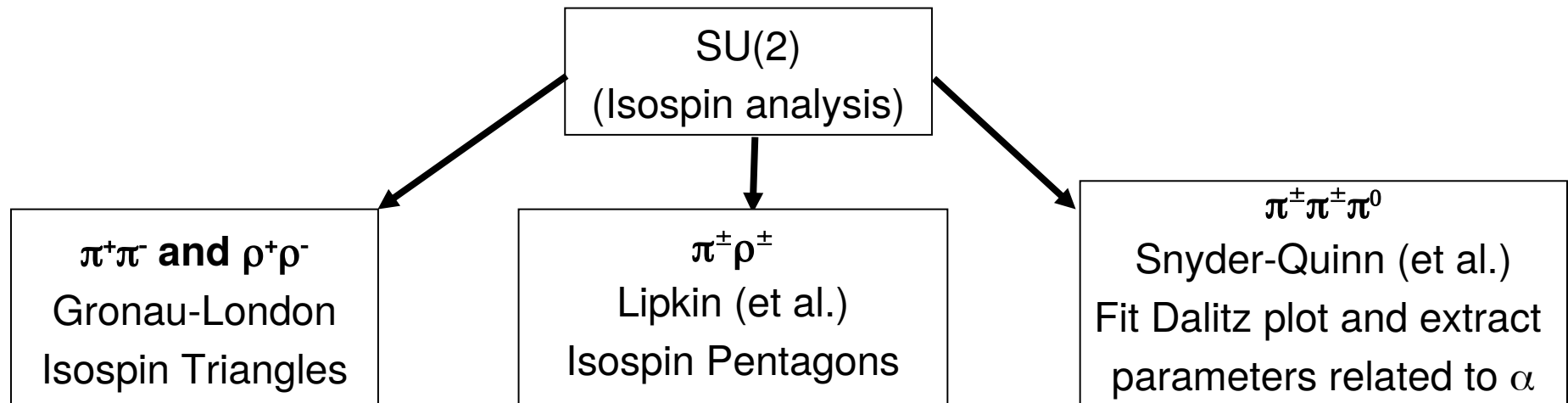
- Measure $S \propto \alpha_{\text{eff}}$

- Need to determine $\delta_\alpha = \alpha_{\text{eff}} - \alpha$ [P/T is different for each final state]

$$\alpha \equiv \arg[-V_{td}V_{tb}^*/V_{ud}V_{ub}^*]$$

Bounding penguins

- ◎ Several recipes describe how to bound penguins and measure α .
 - ◎ These are based on SU(2) [or SU(3)] symmetry.



◎ Use charged and neutral B decays to the hh final state to constrain the penguin contribution and measure α .

M. Gronau and D. London, **65**, 3381 (1990)

◎ Use charged and neutral B decays to the $\rho\pi$ final state to constrain the penguin contribution and measure α . Remove any overlapping regions in

H. Lipkin *et al.*, Phys. Rev. Lett. D **44**, 1454 (1991)

◎ Regions of the Dalitz plot with intersecting ρ bands are included in this analysis; this helps resolve ambiguities.

A. Snyder and H. Quinn, Phys. Rev. Lett. D **48**, 2139 (1993);
H. Quinn and J Silva, Phys. Rev. Lett. D **62**, 054002 (2000).

Isospin analysis

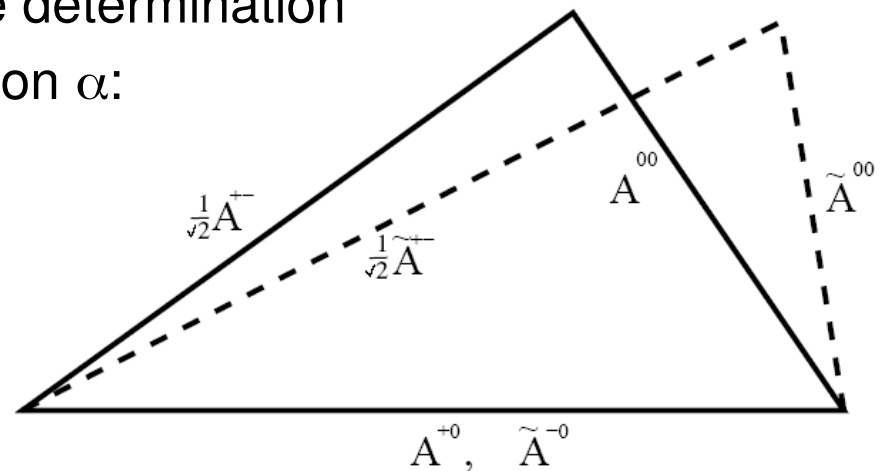
α : collecting the ingredients

from $\alpha_{\text{eff}} \rightarrow$ to α : isospin analysis

Channel	Decay Amplitudes
$\pi\pi$	$A(B^+ \rightarrow \pi^+\pi^0) = \frac{\sqrt{3}}{2}A_{3/2,2}$ $\frac{1}{\sqrt{2}}A(B^0 \rightarrow \pi^+\pi^-) = \frac{1}{\sqrt{12}}A_{3/2,2} - \sqrt{\frac{1}{6}}A_{1/2,0}$ $A(B^0 \rightarrow \pi^0\pi^0) = \frac{1}{\sqrt{3}}A_{3/2,2} + \sqrt{\frac{1}{6}}A_{1/2,0}$

- $B \rightarrow \pi^+\pi^-, \pi^+\pi^0, \pi^0\pi^0$ decays are connected from isospin relations
- $\pi\pi$ states can have $l = 2$ or $l = 0$
 - \Rightarrow the gluonic penguins contribute only to the $l = 0$ state ($\Delta l = 1/2$)
 - $\Rightarrow \pi^+\pi^0$ is a **pure $l = 2$** state ($\Delta l = 3/2$) and it gets contribution only from the **tree diagram**
 - \Rightarrow triangular relations allow for the determination of the phase difference induced on α :

Both $\text{BR}(B^0)$ and $\text{BR}(\bar{B}^0)$ have to be measured in all the $\pi\pi$ channels



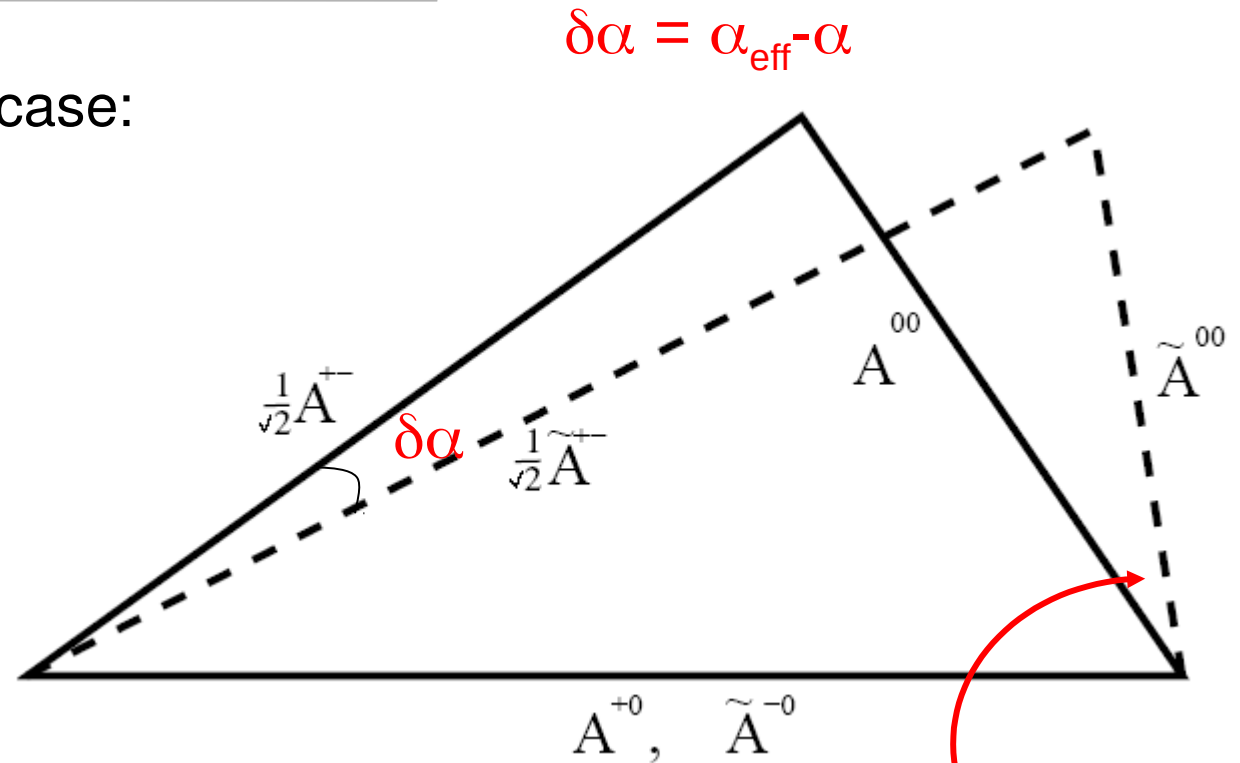
Isospin analysis

- Consider the simplest case:

$B \rightarrow \pi\pi / \rho\rho$ decays.

$$\frac{1}{\sqrt{2}} A^{+-} + A^{00} = A^{+0}$$

$$\frac{1}{\sqrt{2}} \bar{A}^{+-} + \bar{A}^{00} = \bar{A}^{+0}$$

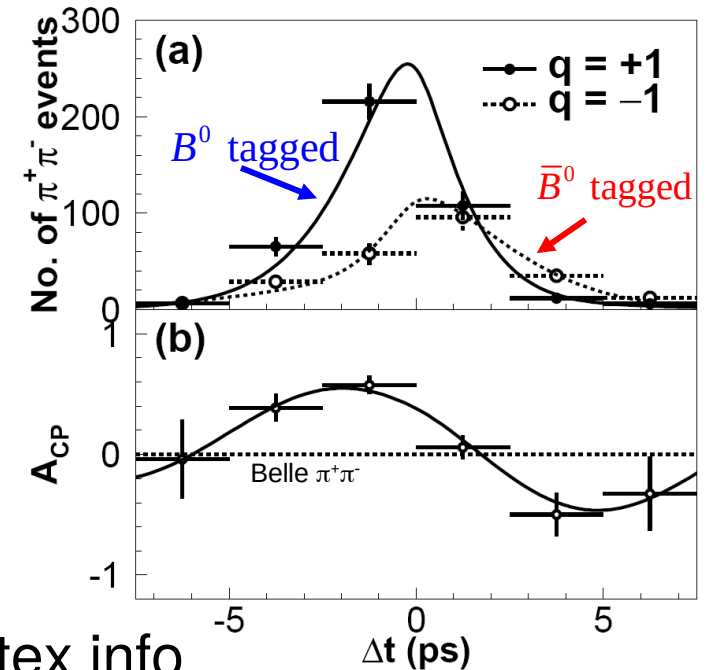
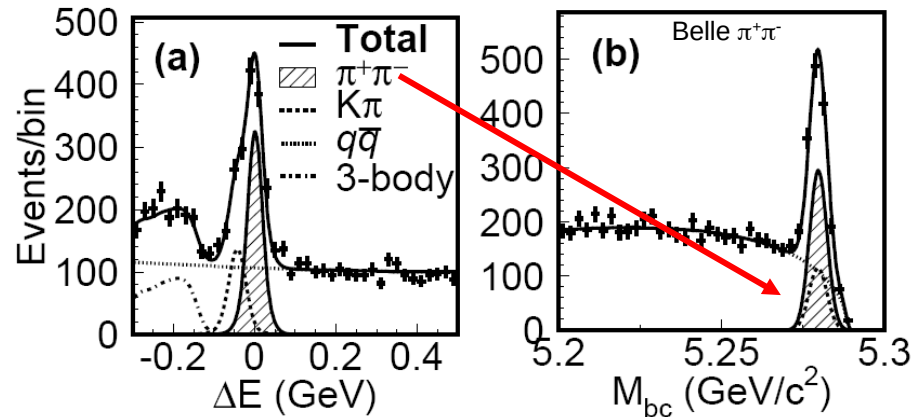


- There are SU(2) violating corrections to consider, for example electroweak penguins ($\sim 5\%$), but these are much smaller than current experimental accuracy and eventually they can be incorporated into the Isospin analysis.

Measuring S in $h^0 h^0$ provides an additional constraint on this angle.

$B \rightarrow \pi\pi$

- ⊙ Easy to isolate signal for $\pi^+\pi^-$ and $\pi^+\pi^0$ as these modes are relatively clean and have relatively large $B \sim O(5 \times 10^{-6})$.



- ⊙ Much harder to isolate $\pi^0\pi^0$: $B \sim 1.5 \times 10^{-6}$

- No tracks in the final state to provide vertex info.
- $B^0 \rightarrow \pi^0\pi^0 \rightarrow \gamma\gamma\gamma\gamma$ has a large ΔE resolution.

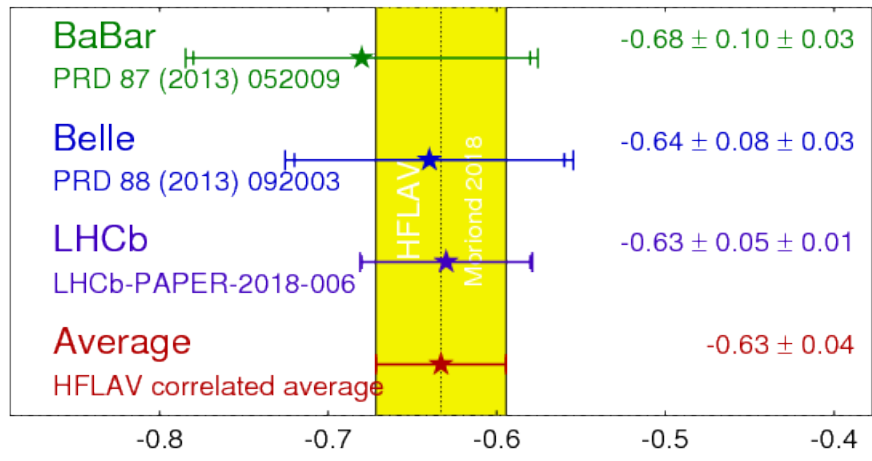
▷ Possible to separate flavour tags to measure C^{00} . This information completes the set of information required for an Isospin analysis.

$$\alpha \equiv \arg[-V_{td}V_{tb}^*/V_{ud}V_{ub}^*]$$

B → ππ

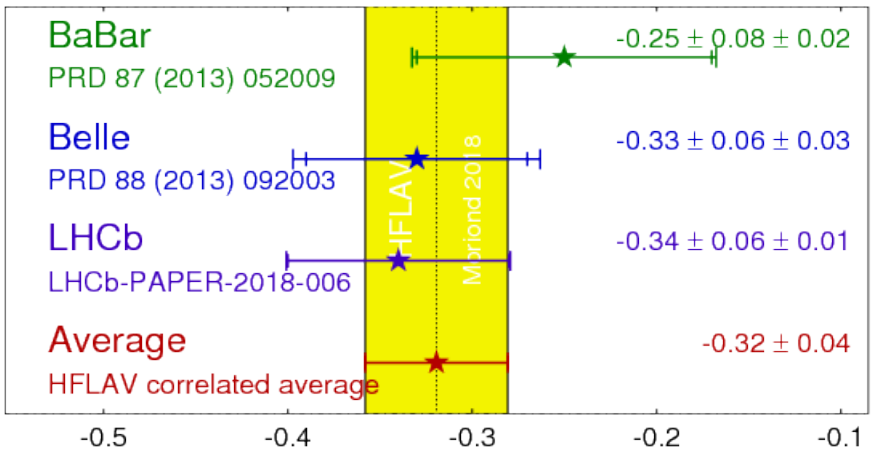
π⁺ π⁻ S_{CP}

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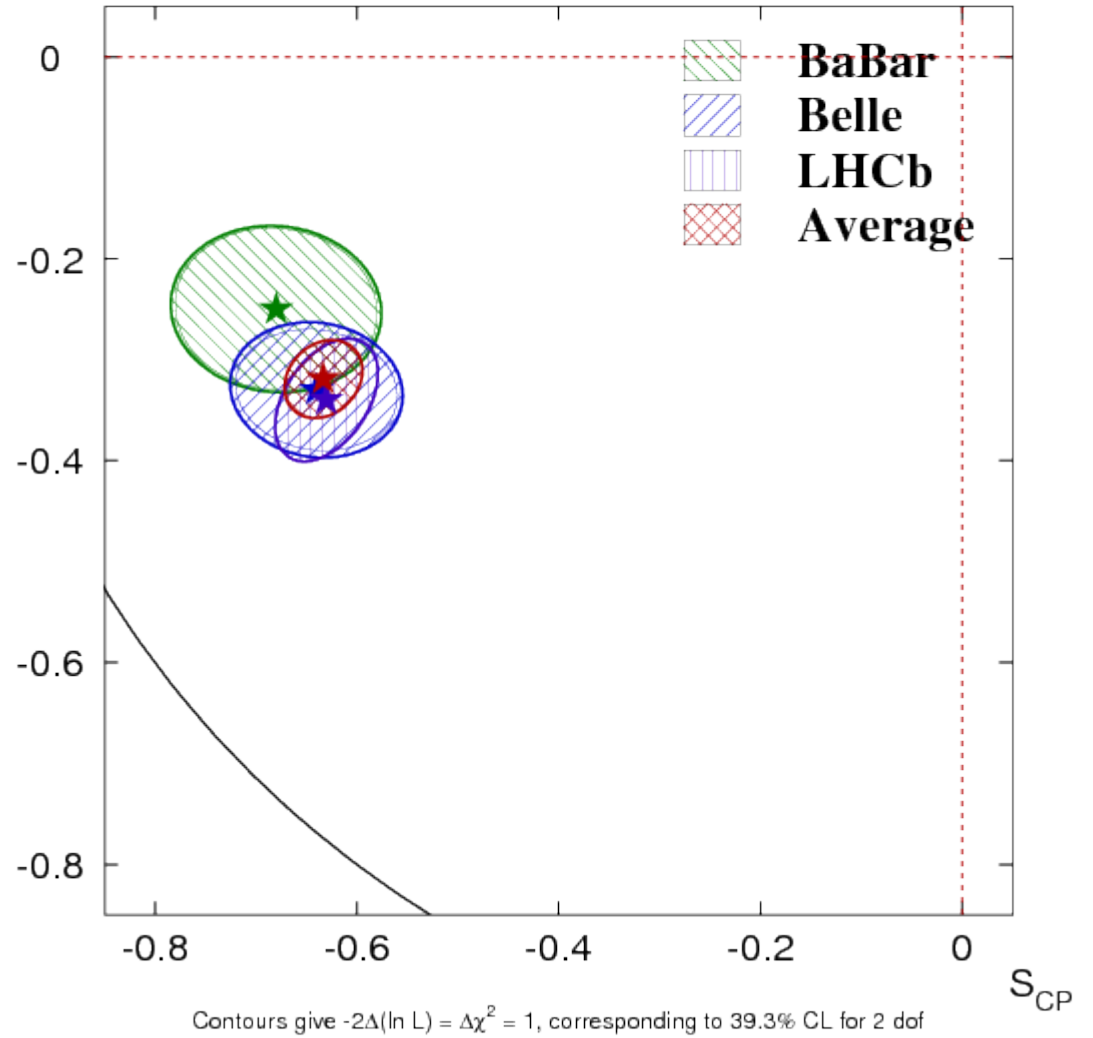
π⁺ π⁻ C_{CP}

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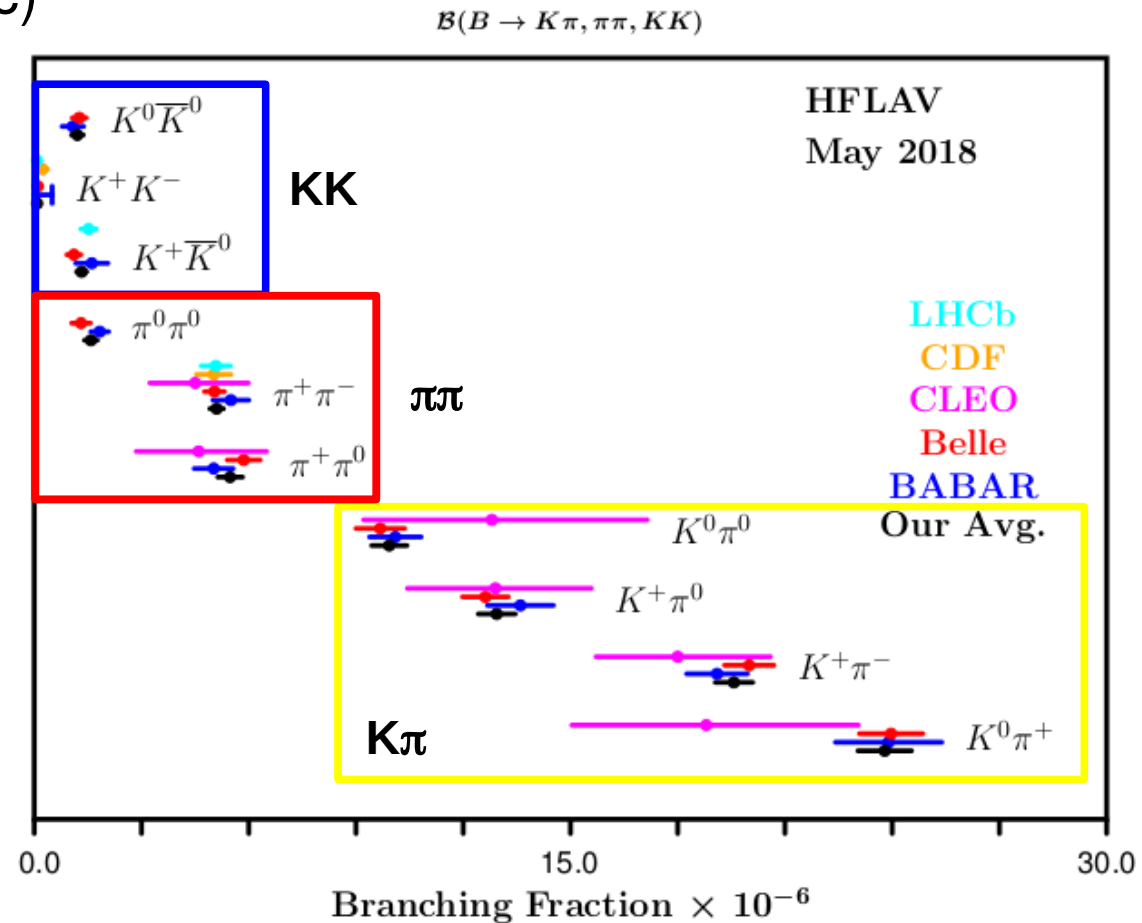
π⁺ π⁻ S_{CP} vs C_{CP}

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Isospin-related $\pi\pi$ decays

- simultaneous ML fit to all hh modes with h being π or K:
- ⊙ $B^+ \rightarrow \pi^+\pi^-$, $K^+\pi^-$, K^+K^- (and cc)
- ⊙ $B^+ \rightarrow \pi^+\pi^0$, $K^+\pi^0$ (and cc)



$$\alpha \equiv \arg[-V_{td}V_{tb}^*/V_{ud}V_{ub}^*]$$

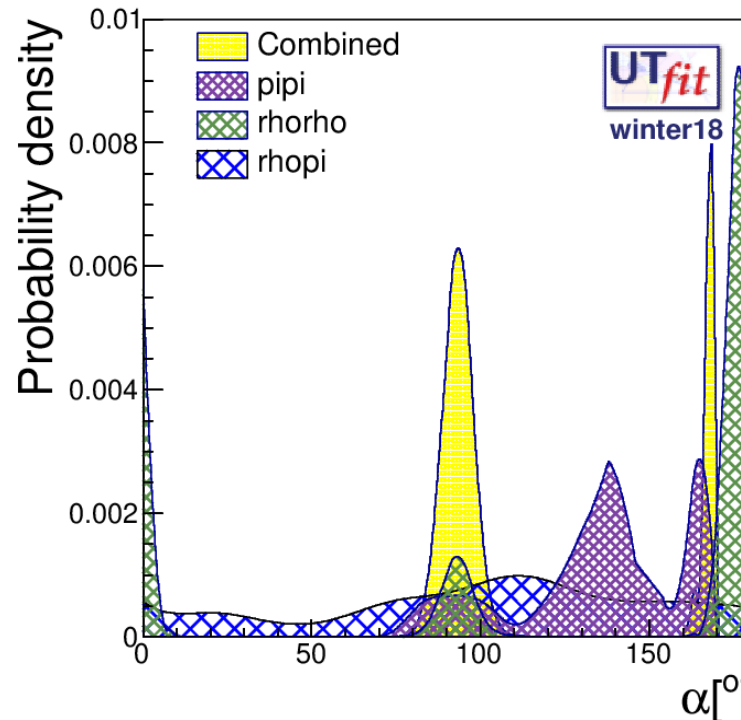
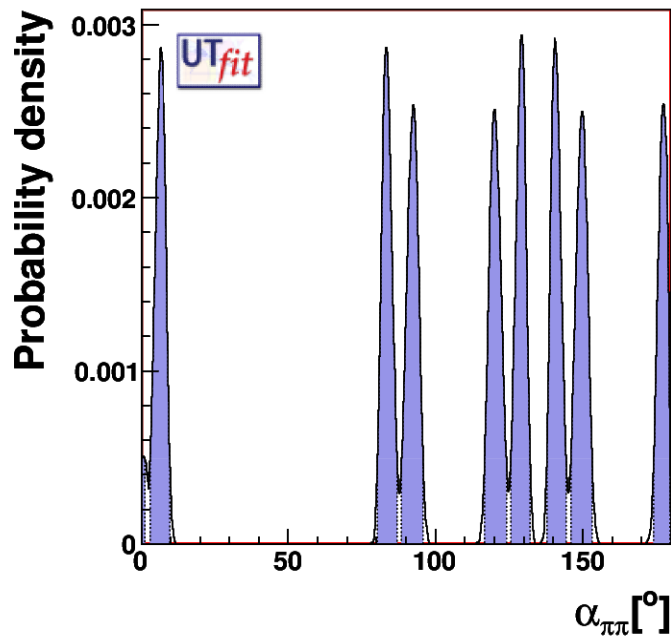
B → ππ

- Inputs from: $B^0 \rightarrow \pi^+ \pi^-$
- $B^+ \rightarrow \pi^+ \pi^0$
- $B^0 \rightarrow \pi^0 \pi^0$

additional information can be used: to reduce the degeneracy of the solutions and also to keep the amplitudes to go to infinity (unphysical)

for example Bs to KK (assuming SU(3) and a big uncertainty on that) can put an upper limit on the penguin amplitude

eight solutions to the isospin system: shown here a case with uncertainties reduced of a factor 10



from $\pi\pi$, $\rho\rho$, $\pi\rho$

combined SM:

$$\alpha = (93.3 \pm 5.6)^\circ$$

UTfit prediction:

$$\alpha = (90.1 \pm 2.2)^\circ$$

$$\alpha \equiv \arg[-V_{td}V_{tb}^*/V_{ud}V_{ub}^*]$$

B \rightarrow $\rho\rho$

● Vector-Vector modes: angular analysis required to determine the CP content. L=0,1,2 partial waves:

- ⊙ longitudinal: CP-even state
- ⊙ transverse: mixed CP states

● + -: two π^0 in the final state

● wide ρ resonance

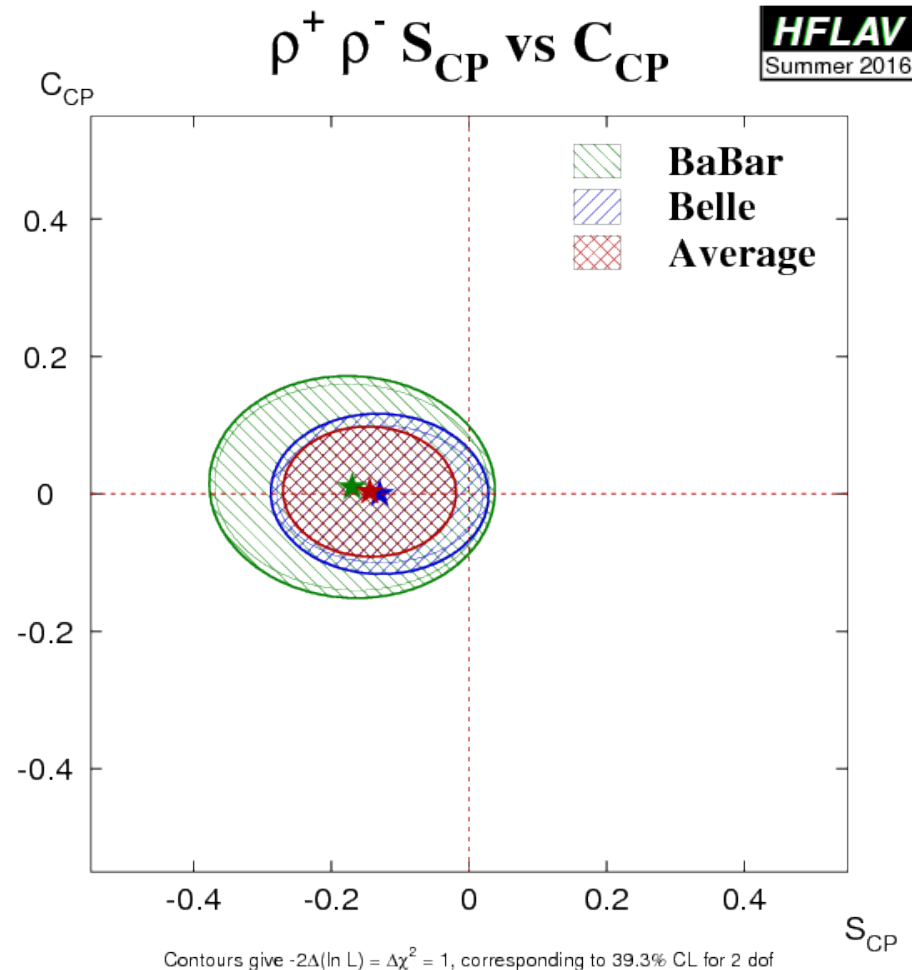
but

● BR 5 times larger with respect to $\pi\pi$

● penguin pollution smaller than in $\pi\pi$

● ρ are almost 100% polarized:

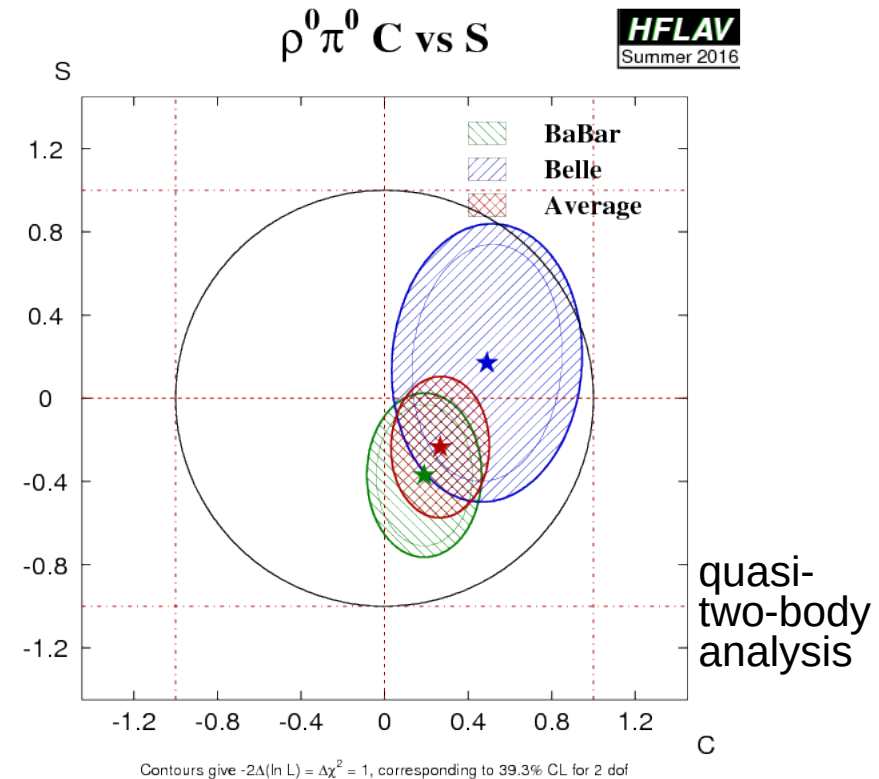
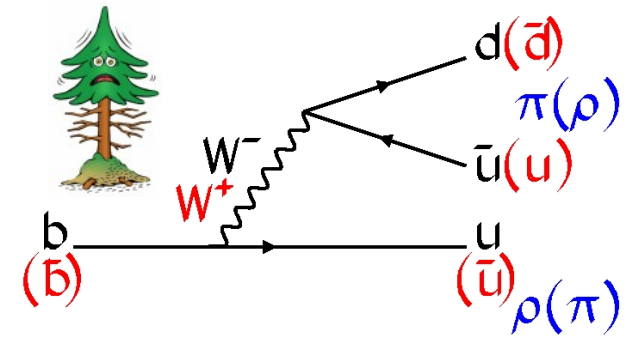
- ⊙ almost a pure CP-even state



$$\alpha \equiv \arg[-V_{td}V_{tb}^*/V_{ud}V_{ub}^*]$$

B \rightarrow $\rho\pi$ ($\pi^+\pi^-\pi^0$ Dalitz Plot)

- dominant decay $\rho\pi$ is not a CP eigenstate
- 5 amplitudes need to be considered:
 - ⊙ $B^0 \rightarrow \rho^+\pi^-, \rho^-\pi^+, \rho^0\pi^0$ and $B^+ \rightarrow \rho^+\pi^0, \rho^0\pi^+$
 - ⊙ Isospin pentagon
- or time-dependent dalitz
 - analysis: α extraction together with the strong phases exploiting the amplitude interference:
 - ⊙ interference at equal masses-squared give information on the strong phases between resonances



γ/ϕ_3 angle

$$\gamma \equiv \arg \left[-V_{ud} V_{ub}^* / V_{cd} V_{cb}^* \right]$$

$b \rightarrow c$ interfering with $b \rightarrow u$

$B \rightarrow D^{(*)} K^{(*)}$

$B^0 \rightarrow D^- K^0 \pi^+$

$B^0 \rightarrow D^{(*)} \pi$

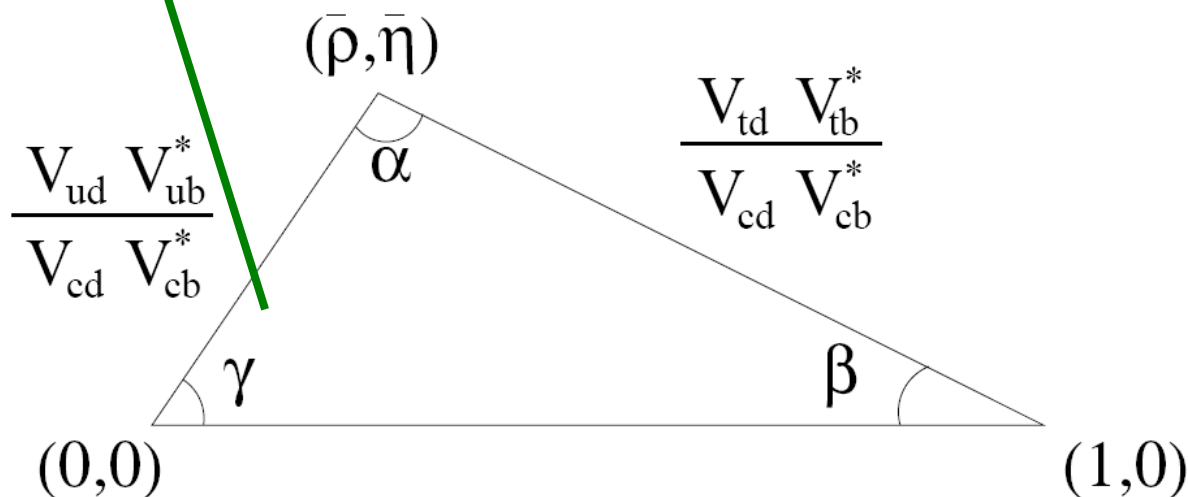
$B^0 \rightarrow D^{(*)} \rho$

+ charmless

Extract γ using $B \rightarrow D^{(*)} K^{(*)}$ final states using:

- GLW: Use CP eigenstates of D^0 .
- ADS: Interference between doubly suppressed decays.
- GGSZ: Use the Dalitz structure of $D \rightarrow K_s h^+ h^-$ decays.

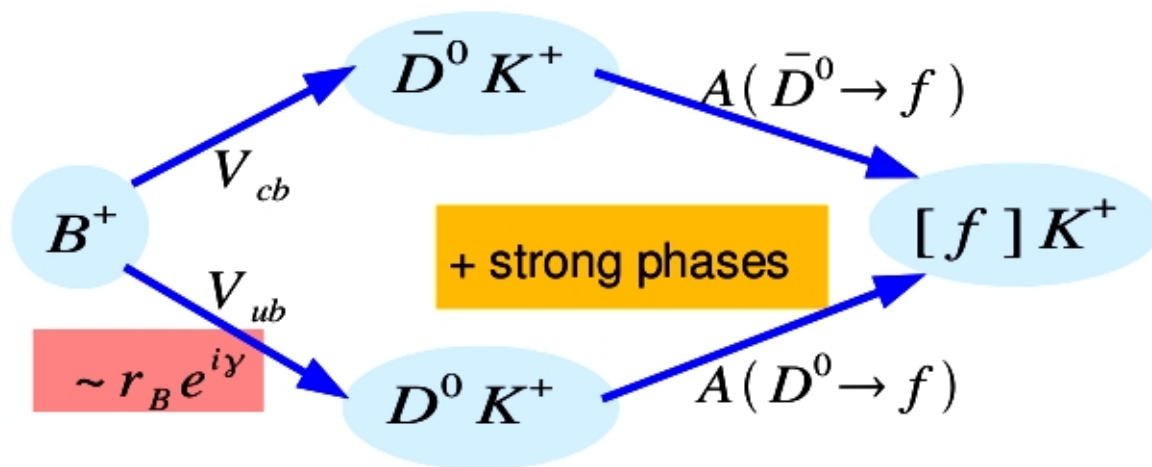
Measurements using neutral D mesons ignore D mixing.



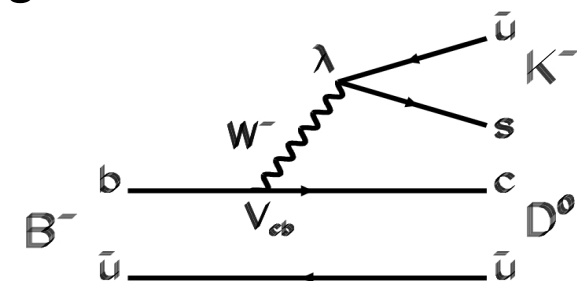
$$\gamma \equiv \arg[-V_{ud}V_{ub}^*/V_{cd}V_{cb}^*]$$

γ and DK trees

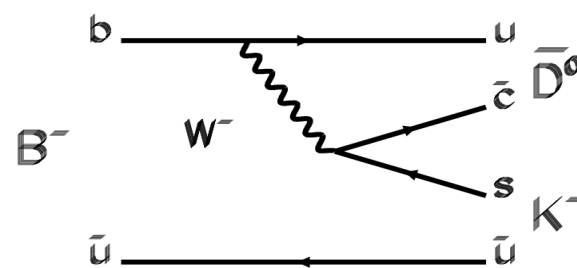
- ⊙ $D^{(*)}K^{(*)}$ decays: from BRs and BR ratios, no time-dependent analysis, just rates
- ⊙ the phase γ is measured exploiting interferences: two amplitudes leading to the same final states
- ⊙ some rates can be really small: $\sim 10^{-7}$



Theoretically clean (no penguins neglecting the D^0 mixing)



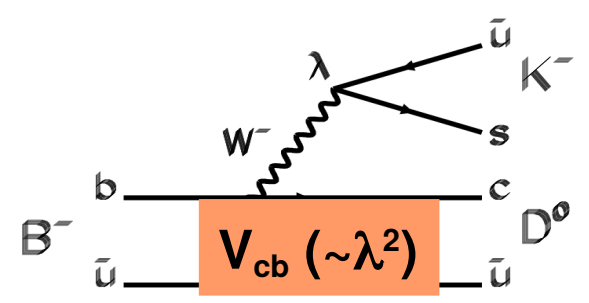
$V_{cb} (\sim \lambda^2)$



$V_{ub} = |V_{ub}| e^{-i\gamma} (\sim \lambda^3)$

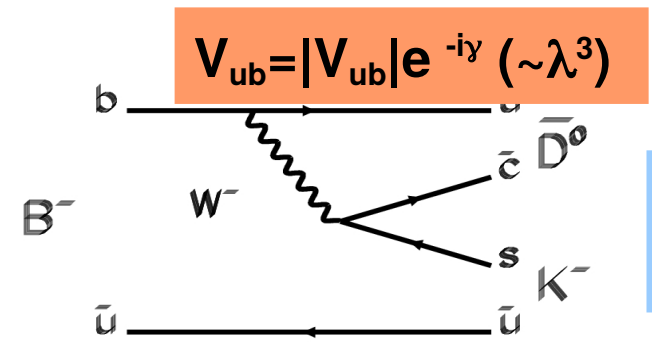
$$\gamma \equiv \arg[-V_{ud}V_{ub}^*/V_{cd}V_{cb}^*]$$

Sensitivity to γ : the ratio r_B



$$A(B^- \rightarrow D^0 K^-) = A_B$$

$$A(B^+ \rightarrow \bar{D}^0 K^+) = A_B$$



$$A(B^- \rightarrow \bar{D}^0 K^-) = A_B r_B e^{i(\delta_B - \gamma)}$$

$$A(B^+ \rightarrow D^0 K^+) = A_B r_B e^{i(\delta_B + \gamma)}$$

$\delta_B =$ strong phase diff.

$r_B =$ amplitude ratio

$$r_B = \left| \frac{B^- \rightarrow \bar{D}^0 K^-}{B^- \rightarrow D^0 K^-} \right| = \sqrt{\underbrace{\bar{\eta}^2 + \bar{\rho}^2}_{\sim 0.36}} \times \underbrace{F_{CS}}_{\text{hadronic contribution channel-dependent}}$$

- ◆ in $B^+ \rightarrow D^{(*)0} K^+$: r_B is ~ 0.1
- ◆ to be measured: $r_B(DK)$, $r_B^*(D^*K)$ and $r_B^s(DK^*)$

$$\gamma \equiv \arg[-V_{ud}V_{ub}^*/V_{cd}V_{cb}^*]$$

Three ways to make DK interfere

GLW(*Gronau, London, Wyler*) method:

more sensitive to r_B

uses the CP eigenstates $D^{(*)0}_{CP}$ with final states:

K^+K^- , $\pi^+\pi^-$ (CP-even), $K_S\pi^0$ (ω, ϕ) (CP-odd)

$$R_{CP\pm} = 1 + r_B^2 \pm 2r_B \cos \gamma \cos \delta_B \quad A_{CP\pm} = \frac{\pm 2r_B \sin \gamma \sin \delta_B}{1 + r_B^2 \pm 2r_B \cos \gamma \cos \delta_B}$$

ADS(*Atwood, Dunietz, Soni*) method: B^0 and \bar{B}^0 in the same final state with $D^0 \rightarrow K^+\pi^-$ (suppr.) and $\bar{D}^0 \rightarrow K^+\pi^-$ (fav.)

$$R_{ADS} = r_B^2 + r_{DCS}^2 + 2r_B r_{DCS} \cos \gamma \cos(\delta_B + \delta_D)$$

the most sensitive way to γ

D^0 Dalitz plot with the decays $B^- \rightarrow D^{(*)0}[K_S\pi^+\pi^-] K^-$

three free parameters to extract: γ , r_B and δ_B

γ : GLW Method

- GLW Method: Study $B^+ \rightarrow D_{CP}^0 X^+$ and $B^+ \rightarrow \bar{D} X^{++} cc$ ($\bar{D}^0 \rightarrow K^+ \pi^-$)
- X^+ is a strangeness one meson e.g. a K^+ or K^{*+} .
- D_{CP}^0 is a CP eigenstate (use these to extract γ):

$$D_{CP=+1}^0 = K^+ K^-, \pi^- \pi^+$$

$$D_{CP=-1}^0 = K_S^0 \pi^0, K_S^0 \omega, K_S^0 \phi$$

- 4 observables
- 3 unknowns:
 r_B, γ and δ

$$R_{CP\pm} = \frac{BF(B^- \rightarrow D_{\pm}^0 K^-) + BF(B^+ \rightarrow D_{\pm}^0 K^+)}{BF(B^- \rightarrow D^0 K^-) + BF(B^+ \rightarrow D^0 K^+)} = 1 + r_B^2 \pm 2r_B \cos \delta \cos \gamma$$

$$A_{CP\pm} = \frac{BF(B^- \rightarrow D_{\pm}^0 K^-) - BF(B^+ \rightarrow D_{\pm}^0 K^+)}{BF(B^- \rightarrow D_{\pm}^0 K^-) + BF(B^+ \rightarrow D_{\pm}^0 K^+)} = \pm 2r_B \sin \delta \sin \gamma / R_{CP\pm}$$

- The precision on γ is strongly dependent on the value of r_B .
 - ▷ $r_B \sim 0.1$ as this is a ratio of Cabibbo suppressed to Cabibbo allowed decays and also includes a colour suppression factor for $B^+ \rightarrow D^{(*)} K^{(*)} b \rightarrow u$ decays.
- Measurement has an 8-fold ambiguity on γ .

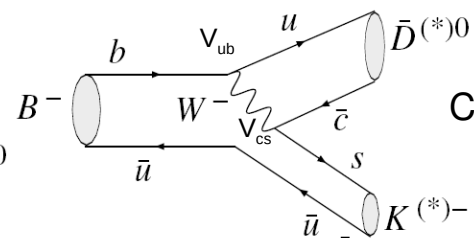
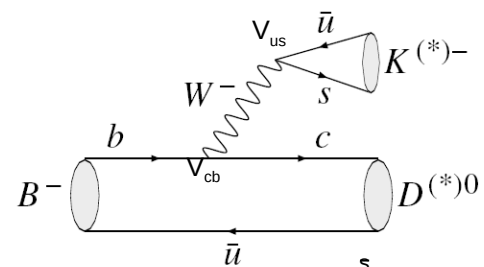
$$\gamma \equiv \arg[-V_{ud}V_{ub}^*/V_{cd}V_{cb}^*]$$

γ : ADS Method

Attwood, Dunietz, Soni, PRL 78 3257 (1997)

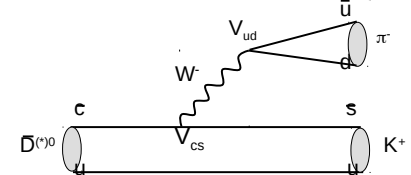
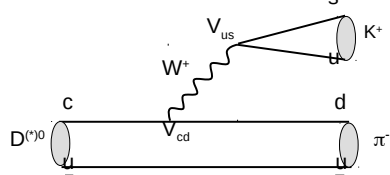
- ADS Method: Study $B^{\pm,0} \rightarrow D^{(*)0} K^{(*)\pm}$
- Reconstruct doubly suppressed decays with common final states and extract γ through interference between these amplitudes:

$B^- \rightarrow D^{(*)0} K^{(*)-}$
CKM Favoured



$B^- \rightarrow \bar{D}^{(*)0} K^{(*)-}$
CKM and Color Suppressed

$D^{(*)0} \rightarrow K^+ \pi^-$
Doubly CKM Suppressed



$\bar{D}^{(*)0} \rightarrow K^+ \pi^-$
CKM Favoured

- γ extracted using ratios of rates:

$$r_B^{(*)} = \left| \frac{A(B^- \rightarrow \bar{D}^{(*)0} K^-)}{A(B^- \rightarrow D^{(*)0} K^-)} \right|$$

$$r_D = \left| \frac{A(D^0 \rightarrow K^+ \pi^-)}{A(D^0 \rightarrow K^- \pi^+)} \right|$$

- ⊙ $\delta^{(*)} = \delta_B^{(*)} + \delta_D$
- ⊙ $\delta^{(*)}$ is the sum of strong phase differences between the two B and D decay amplitudes.
- ⊙ r_D and r_B are measured in B and charm factories.
- ⊙ δ_D is measured by CLEO-c

γ : GGSZ Method

● GGSZ (“Dalitz”) Method: Study $D^{(*)0}K^{(*)}$ using the $D^{(*)0} \rightarrow K_S^0 h^+ h^-$ Dalitz structure to constrain γ . ($h = \pi, K$)

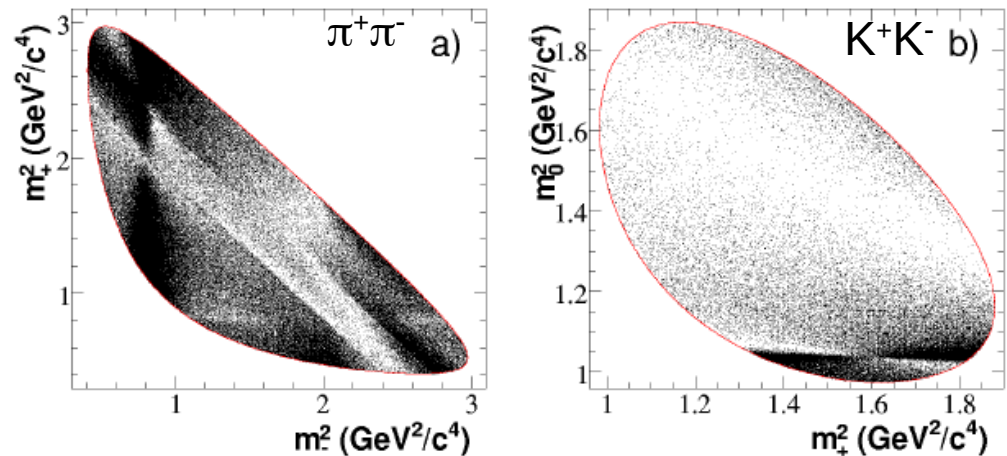
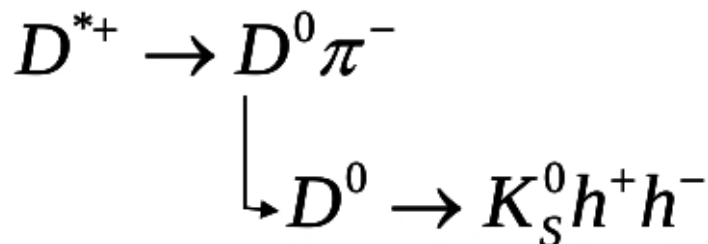
⊙ Self tagging: use charge for B^\pm decays or $K^{(*)}$ flavour for B^0 mesons.

$$A(B^\pm \rightarrow (K_S^0 h^+ h^-)_D K^\pm) \propto f(m_+^2, m_-^2) + f(m_-^2, m_+^2) r_B e^{i(\delta_B \pm \gamma)}$$

where $m_\pm = m_{K_S^0 h^\pm}$

⊙ Need detailed model of the amplitudes in the D meson Dalitz plot.

⊙ Use a control sample
(CLEO-c data or $D^{*+} \rightarrow D^0 \pi^+$)
to measure the Dalitz plot.

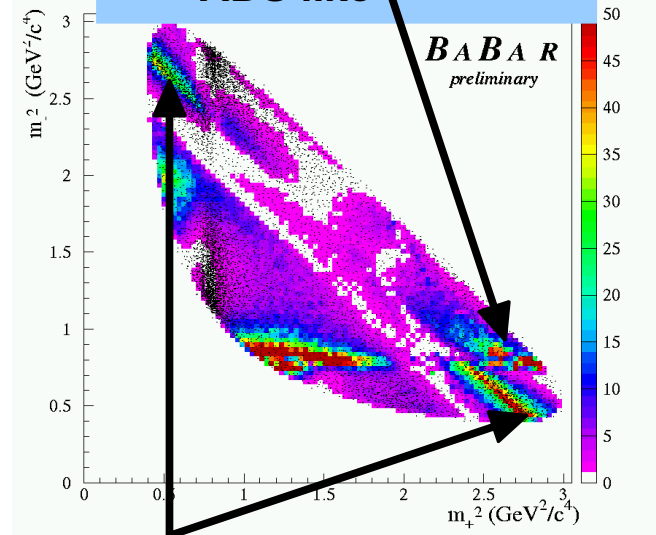


Control sample plots from BaBar GGSZ paper

γ : GGSZ Method

- ⊙ neutral D mesons reconstructed in three-body CP-eigenstate final states (typically $D^0 \rightarrow K_S \pi^- \pi^+$)
- ⊙ the complete structure (amplitude and strong phases) of the D^0 decay in the phase space is obtained on independent data sets and used as input to the analysis
- ⊙ use of the cartesian coordinate:
 - $x_{\pm} = r_B \cos(\delta \pm \gamma)$
 - $y_{\pm} = r_B \sin(\delta \pm \gamma)$
- ⊙ γ , r_B and δ_B are obtained from a simultaneous fit of the $K_S \pi^+ \pi^-$ Dalitz plot density for B^+ and B^-
- ⊙ need a model for the Dalitz amplitudes
- ⊙ 2-fold ambiguity on γ

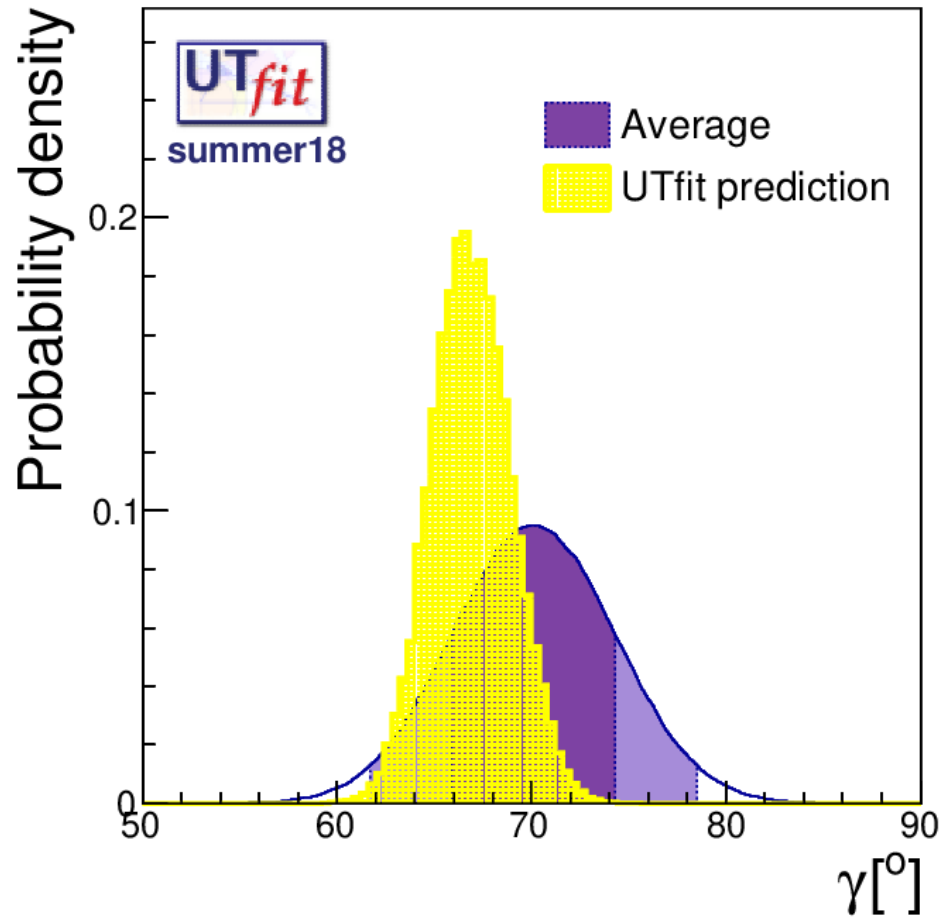
Interference of
 $B^- \rightarrow D^0 K^-$, $D^0 \rightarrow K^{*+} \pi^-$
(suppressed) with
 $B^- \rightarrow \bar{D}^0 K^-$, $\bar{D}^0 \rightarrow K^{*+} \pi^-$
~ ADS like



Interference of
 $B^- \rightarrow D^0 K^-$, $D^0 \rightarrow K^0_s \rho^0$
with
 $B^- \rightarrow \bar{D}^0 K^-$, $\bar{D}^0 \rightarrow K^0_s \rho^0$
~ GLW like

$$\gamma \equiv \arg[-V_{ud}V_{ub}^*/V_{cd}V_{cb}^*]$$

CP violation: γ



γ from B into DK decays:

combined: $(73.4 \pm 4.4)^\circ$

UTfit prediction: $(65.8 \pm 2.2)^\circ$

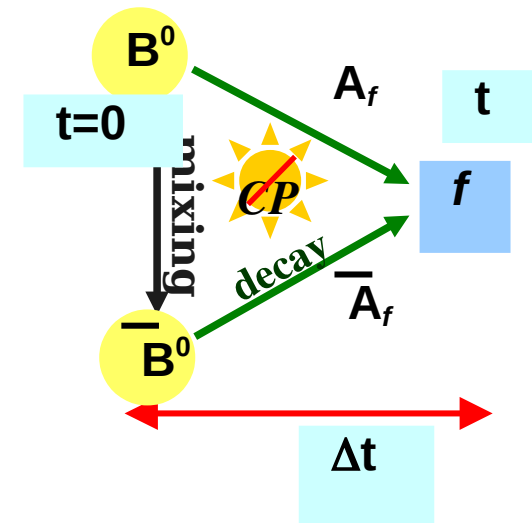
back-up

CP violation in interference between mixing and decay:

$$\lambda_{f_{CP}} = \frac{q}{p} \cdot \frac{\bar{A}_{f_{CP}}}{A_{f_{CP}}}$$

⊙ decays in final state f
 accessible to both a B or a \bar{B}
 (f is not necessarily a CP eigenstate)

⊙ if $\text{Im}\lambda \neq 0$ then \rightarrow CP violation



$$\lambda = \frac{q A(\bar{B} \rightarrow f)}{p A(B \rightarrow f)} = \frac{V_{td}^* V_{tb} \bar{A}}{V_{td} V_{tb}^* A} \sim e^{-i2\beta} \frac{\bar{A}}{A}$$

β is the
 mixing phase

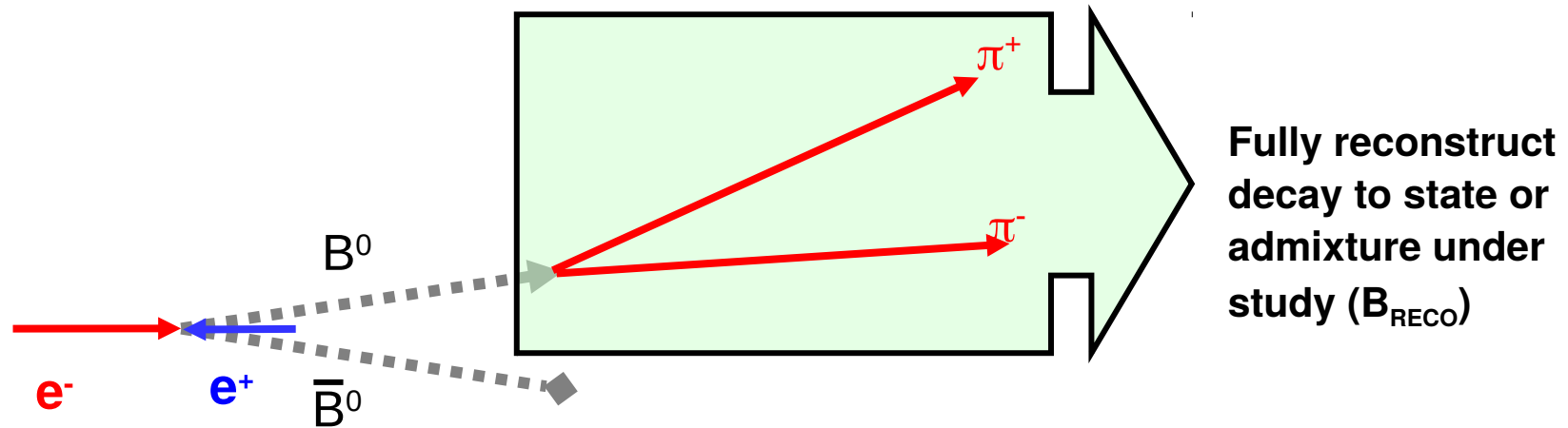
examples

	f	$\text{Arg}\left(\frac{\bar{A}}{A}\right)$	$ \lambda $	parameter
mixing	$B^0 \rightarrow l\nu X, D^{(*)}\pi(\rho, a_1)$	0	~ 0	ΔM_{B^0}
“sin 2 β ”	$B^0 \rightarrow J/\psi K^0, \dots$	0	1	sin 2 β
“sin 2 α ”	$B^0 \rightarrow \pi\pi, \rho\pi, \pi\pi\pi$	$\sim (-2\gamma)$	~ 1	sin 2 α
“sin(2 $\beta + \gamma$)”	$B^0 \rightarrow D^{(*)}\pi$	$\sim (-\gamma)$	~ 0.02	sin(2 $\beta + \gamma$)

$B\bar{B}$ pair coherent production

- ⊙ The B^0 and \bar{B}^0 mesons from the $Y(4S)$ are in a coherent $L = 1$ state:
 - ⊙ The $Y(4S)$ is a $b\bar{b}$ state with $J^{PC} = 1^{--}$.
 - ⊙ B mesons are scalars ($J^P = 0^-$)
 - ⇒ total angular momentum conservation
 - ⇒ the $B\bar{B}$ pair has to be produced in a **$L = 1$ state**.
- ⊙ The $Y(4S)$ decays strongly so B mesons are produced in the two flavour eigenstates B^0 and \bar{B}^0 :
 - ⊙ After production, each B evolves in time, but **in phase** so that at any time there is always exactly one B^0 and one \bar{B}^0 present, at least until one particle decays:
 - ⇒ If at a given time t one B could oscillate independently from the other, they could become a state made up of two identical mesons: but the $L = 1$ state is anti-symmetric, while a system of **two identical mesons (bosons!)** must be completely symmetric for the two particle exchange.
- ⊙ Once one B decays the other continues to evolve, and so it is possible to have events with **two B or two \bar{B} decays**.

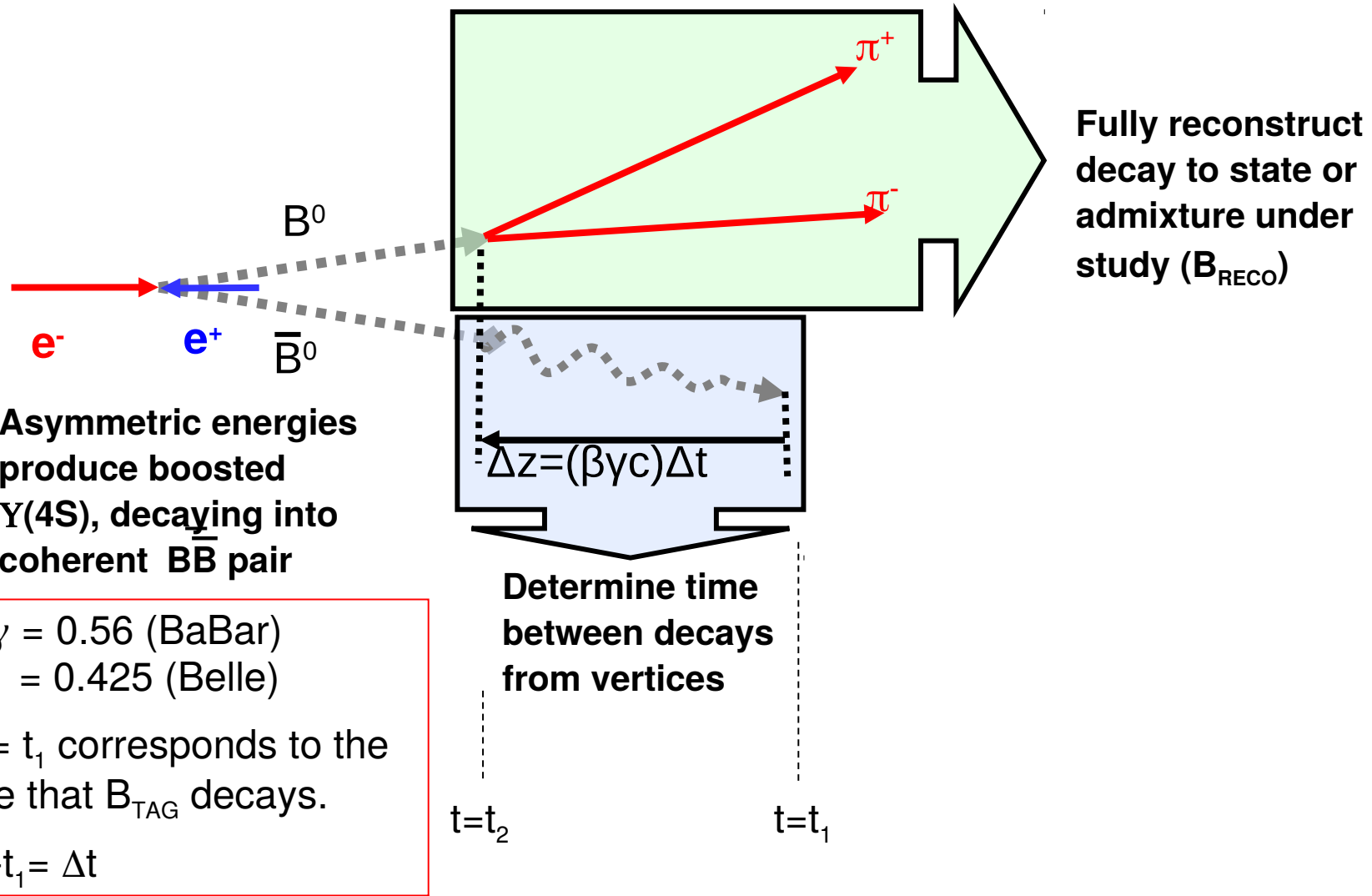
Measuring Δt



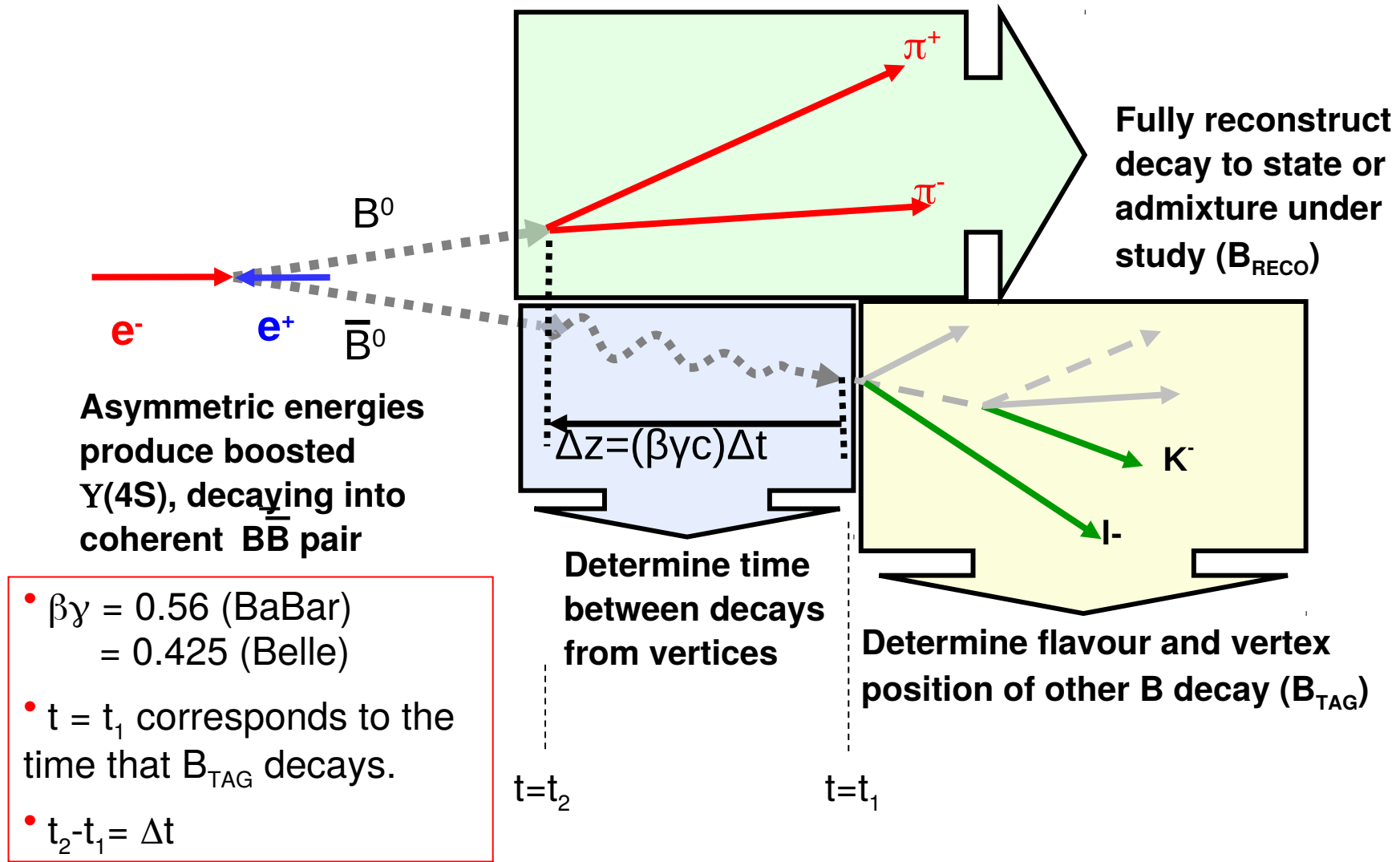
Asymmetric energies
produce boosted
 $Y(4S)$, decaying into
coherent $B\bar{B}$ pair

Fully reconstruct
decay to state or
admixture under
study (B_{RECO})

Measuring Δt



Measuring Δt



⇒ Then fit the Δt distribution to obtain the amplitude of sine and cosine terms.

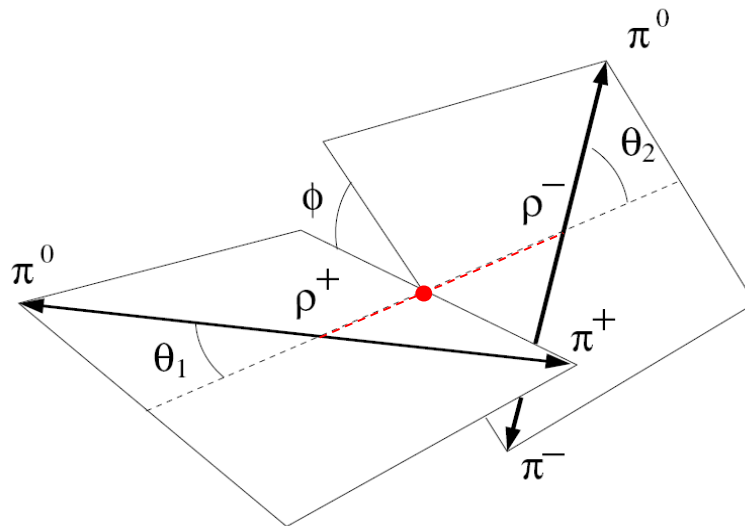
- (simplified) angular analysis

- Inputs from:

$$B^0 \rightarrow \rho^+ \rho^-$$

$$B^+ \rightarrow \rho^+ \rho^0$$

$$B^0 \rightarrow \rho^0 \rho^0$$



θ_i are the helicity angles: angles between the π^0 momentum and the direction opposite to that of the B^0 in the vector rest frame.

ϕ is the angle between the vector meson decay planes.

- We define the fraction of

longitudinally polarised events as:

$$\begin{aligned} \frac{\Gamma_L}{\Gamma} &= \frac{|H_0|^2}{|H_0|^2 + |H_{+1}|^2 + |H_{-1}|^2}, \\ &= f_L. \end{aligned}$$

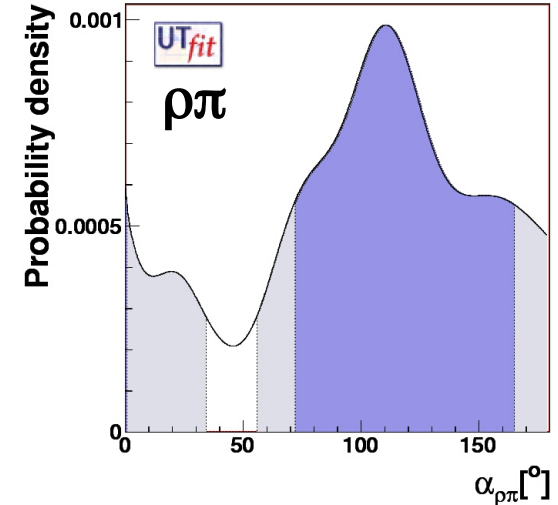
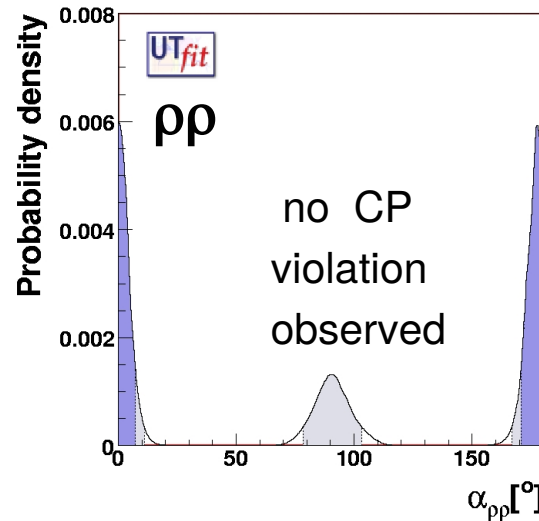
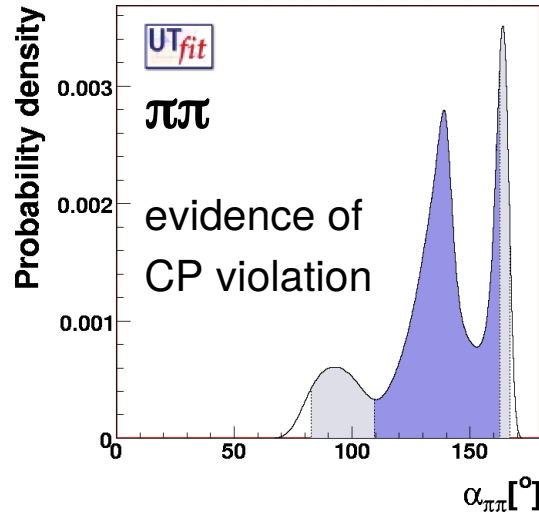
$$\frac{d^2\Gamma}{\Gamma d \cos \theta_1 d \cos \theta_2} = \frac{9}{4} \left[f_L \cos^2 \theta_1 \cos^2 \theta_2 + \frac{1}{4} (1 - f_L) \sin^2 \theta_1 \sin^2 \theta_2 \right]$$

- $f_L \sim 1$ for $B \rightarrow \rho\rho$ decays: this helps simplify extracting α .
- Can measure S^{00} as well as C^{00} to help resolve ambiguities.
- Finite width of the ρ is ignored in the α determination

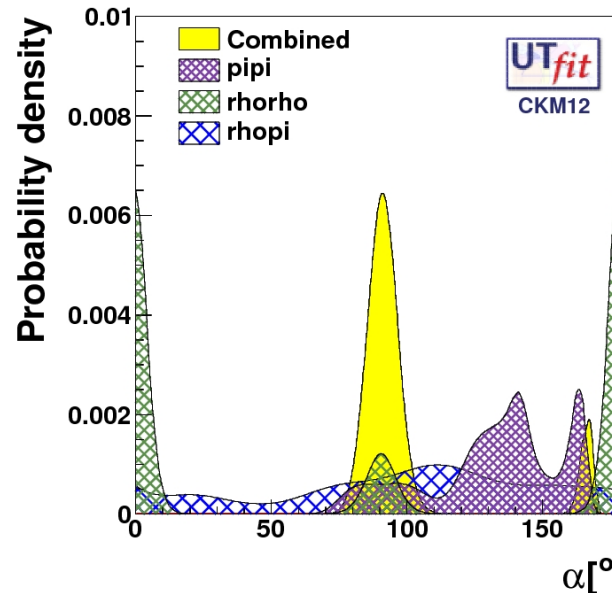
$$\alpha \equiv \arg[-V_{td}V_{tb}^*/V_{ud}V_{ub}^*]$$

CP violation: α

⊙ Combining all the modes to maximize our knowledge of α ..



bayesian analysis:
the quantity plotted is
now the Probability
Density Function (PDF)

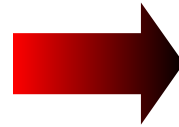
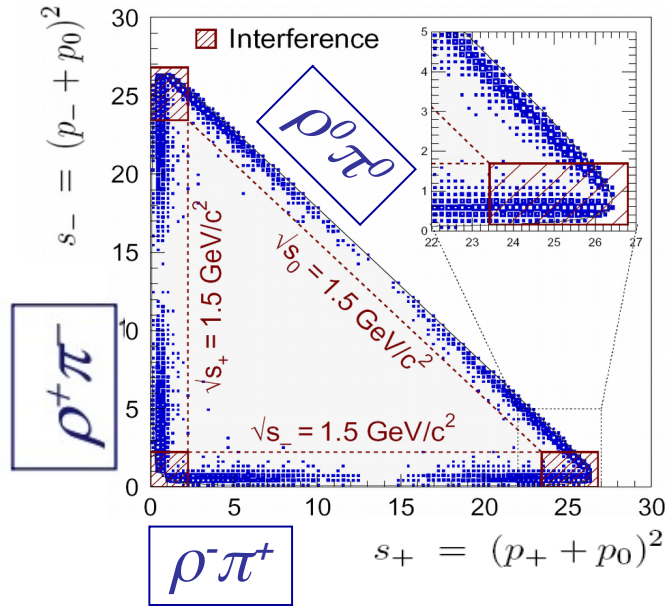


$\alpha_{SM} = (92 \pm 7)^\circ$

$$\alpha \equiv \arg \left[-V_{td} V_{tb}^* / V_{ud} V_{ub}^* \right]$$

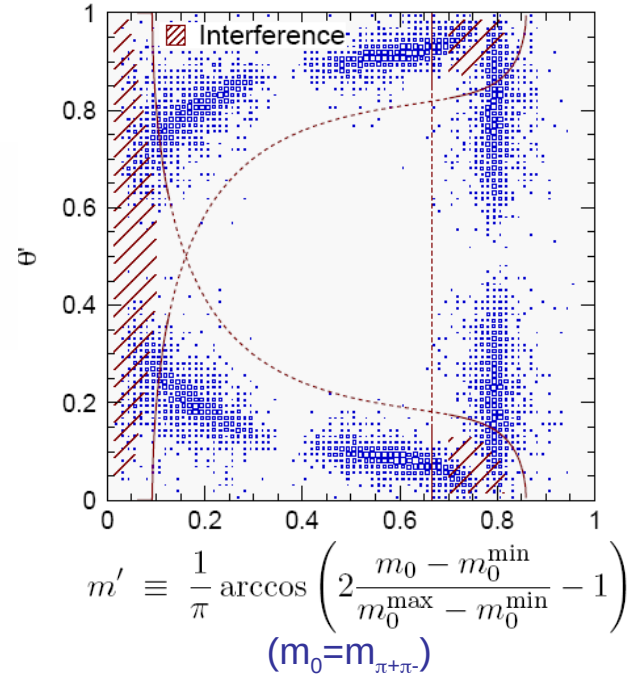
B \rightarrow $\rho\pi$ ($\pi^+\pi^-\pi^0$ Dalitz Plot)

- ⊙ Analyse a transformed Dalitz Plot to extract parameters related to α .
- ⊙ Use the Snyder-Quinn method.



($\theta_0 = \pi^+\pi^-$ helicity)

$$\theta' \equiv \frac{1}{\pi} \theta_0$$



- ⊙ Fit the time-dependence of the amplitudes in the Dalitz plot:

$$|\mathcal{A}_{3\pi}^{\pm}(\Delta t)|^2 = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \left[|\mathcal{A}_{3\pi}|^2 + |\bar{\mathcal{A}}_{3\pi}|^2 \mp (|\mathcal{A}_{3\pi}|^2 - |\bar{\mathcal{A}}_{3\pi}|^2) \cos(\Delta m_d \Delta t) \right. \\ \left. \pm 2\text{Im} \left[\bar{\mathcal{A}}_{3\pi} \mathcal{A}_{3\pi}^* \right] \sin(\Delta m_d \Delta t) \right],$$