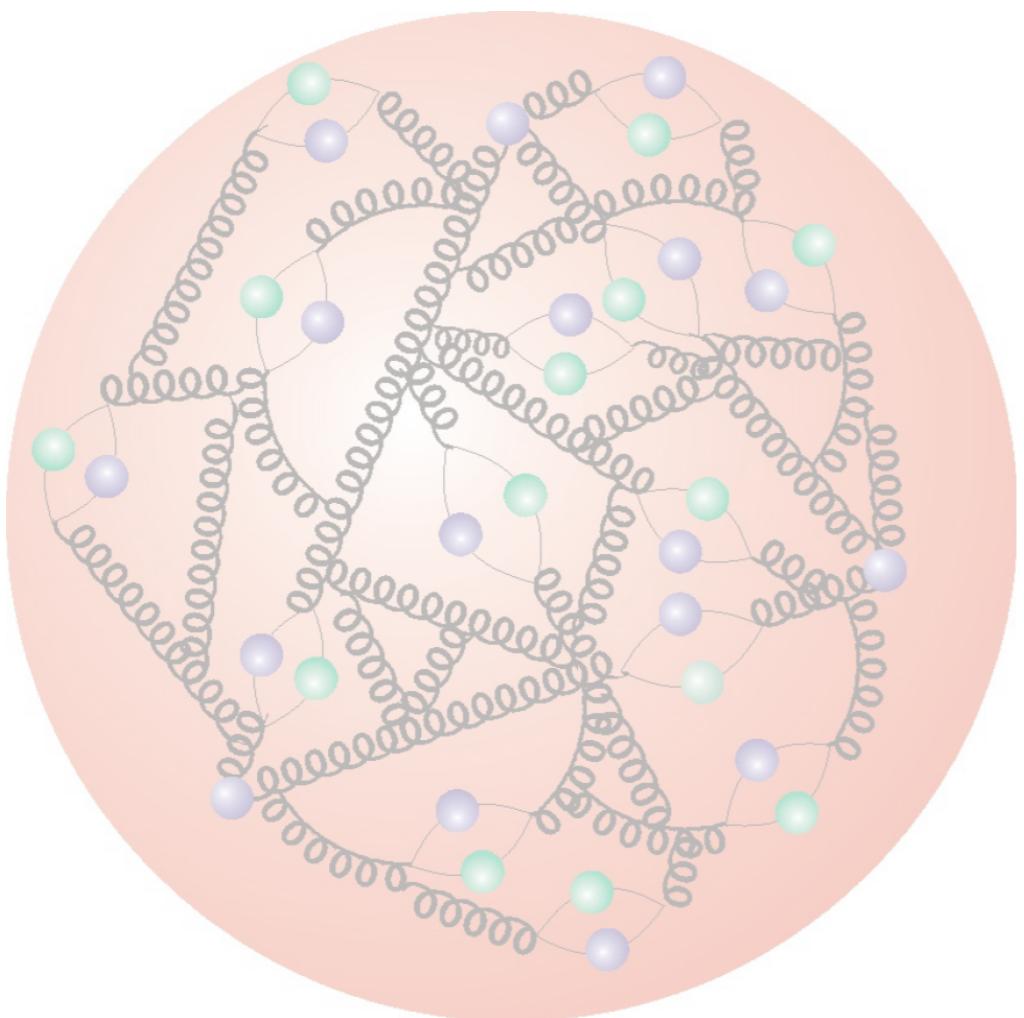


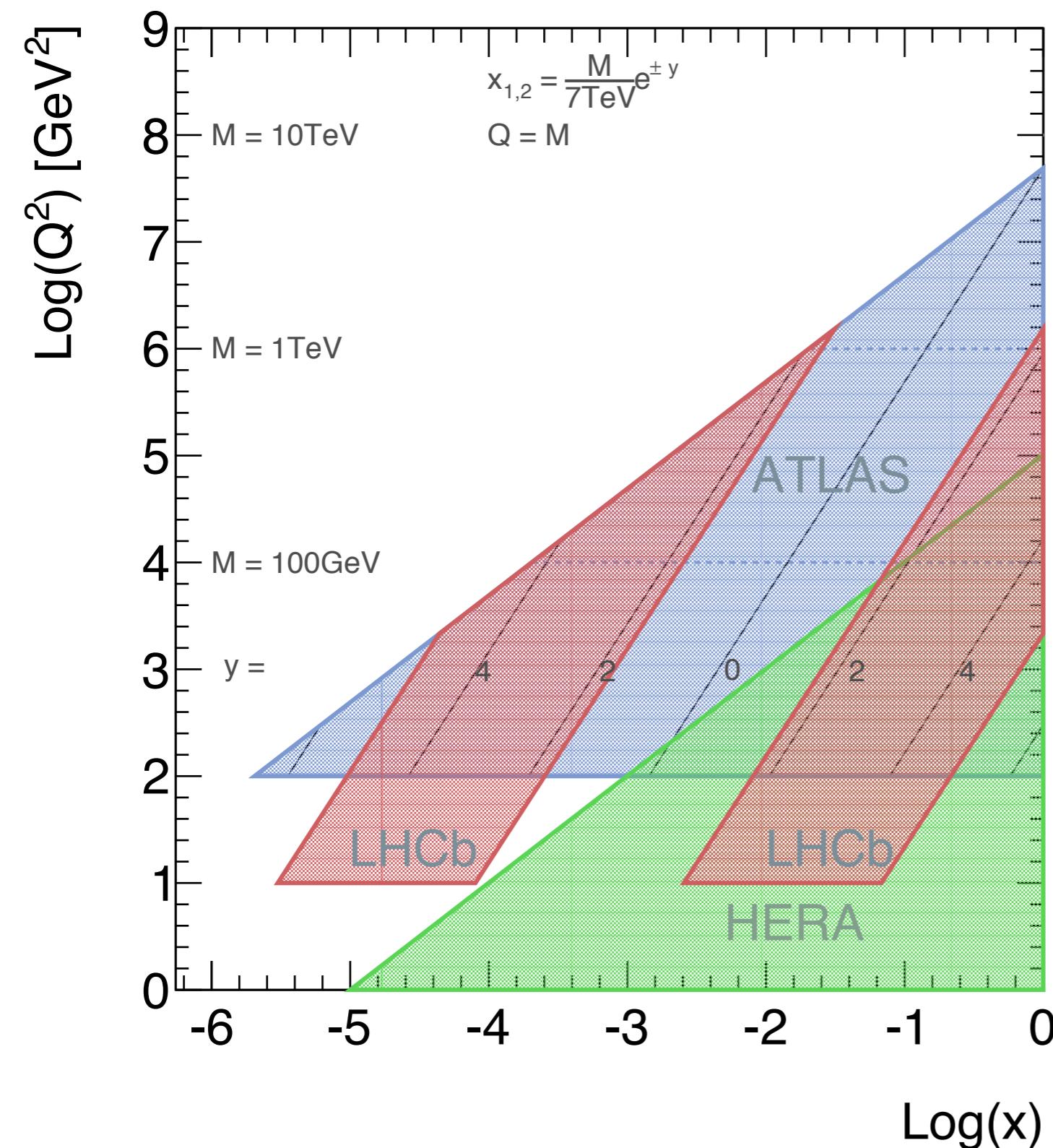
Precision QCD in DIS at HERA



- Introduction
- HERA-II Updates
- H1 NC/CC $e^\pm p$
- H1 NC High y $e^\pm p$
- ZEUS NC $e^+ p$
- HERAPDF Plans



Where Are We Going?



LHC: largest mass states at large x

For central production $x=x_1=x_2$

$$M = x\sqrt{s}$$

i.e. $M > 1\text{ TeV}$ probes $x > 0.1$

Searches for high mass states require precision knowledge at high x

Z' / quantum gravity / susy searches...

DGLAP evolution allows predictions to be made

High x predictions rely on

- data (DIS / fixed target)
- sum rules
- behaviour of PDFs as $x \rightarrow 1$

Structure Functions



$$\frac{d\sigma_{NC}^\pm}{dxdQ^2} = \frac{2\pi\alpha^2}{x} \left[\frac{1}{Q^2} \right]^2 \left[Y_+ \tilde{F}_2 \mp Y_- x \tilde{F}_3 - y^2 \tilde{F}_L \right]$$

$$\frac{d\sigma_{CC}^\pm}{dxdQ^2} = \frac{G_F^2}{4\pi x} \left[\frac{M_W^2}{M_W^2 + Q^2} \right]^2 \left[Y_+ \tilde{W}_2^\pm \mp Y_- x \tilde{W}_3^\pm - y^2 \tilde{W}_L^\pm \right]$$

$$Y_\pm = 1 \pm (1-y)^2$$

$$\tilde{F}_2 \propto \sum (xq_i + x\bar{q}_i)$$

Dominant contribution

The NC reduced cross section defined as:

$$x\tilde{F}_3 \propto \sum (xq_i - x\bar{q}_i)$$

Only sensitive at high $Q^2 \sim M_Z^2$

$$\tilde{F}_L \propto \alpha_s \cdot xg(x, Q^2)$$

Only sensitive at low Q^2 and high y

similarly for pure weak CC analogues:

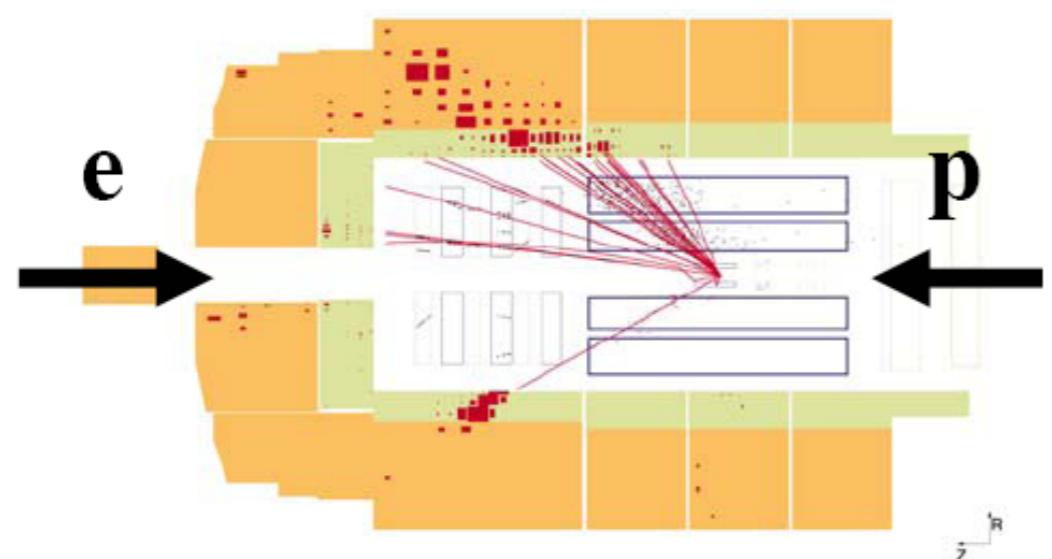
$$W_2^\pm, xW_3^\pm \text{ and } W_L^\pm$$

$$\tilde{\sigma}_{NC}^\pm \sim \tilde{F}_2 \mp \frac{Y_-}{Y_+} x \tilde{F}_3$$

The CC reduced cross section defined as:

$$\sigma_{CC}^\pm = \frac{2\pi x}{G_F^2} \left[\frac{M_W^2 + Q^2}{M_W^2} \right]^2 \frac{d\sigma_{CC}^\pm}{dxdQ^2}$$

$$\frac{d\sigma_{CC}^\pm}{dxdQ^2} = \frac{1}{2} \left[Y_+ W_2^\pm \mp Y_- x W_3^\pm - y^2 W_L^\pm \right]$$



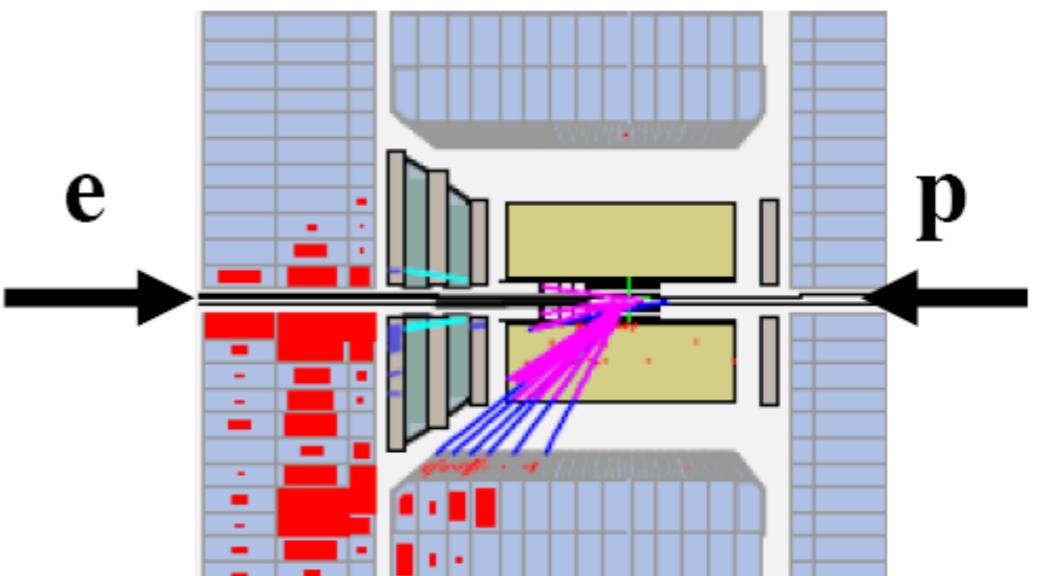
Neutral current event selection:

High P_T isolated scattered lepton
Suppress huge photo-production background by
imposing longitudinal energy-momentum
conservation

Kinematics may be reconstructed in many ways:
energy/angle of hadrons & scattered lepton
provides excellent tools for sys cross checks

Removal of scattered lepton provides a
high stats “pseudo-charged current sample”
Excellent tool to cross check CC analysis

Final selection: $\sim 10^5$ events per sample at high Q^2
 $\sim 10^7$ events for $10 < Q^2 < 100 \text{ GeV}^2$



Charged current event selection:

Large missing transverse momentum (neutrino)
Suppress huge photo-production background
Topological finders to remove cosmic muons

Kinematics reconstructed from hadrons
Final selection: $\sim 10^3$ events per sample

HERA Operation



HERA-I operation 1993-2000

$E_e = 27.6 \text{ GeV}$

$E_p = 820 / 920 \text{ GeV}$

$\int \mathcal{L} \sim 110 \text{ pb}^{-1}$ per experiment

HERA-II operation 2003-2007

$E_e = 27.6 \text{ GeV}$

$E_p = 920 \text{ GeV}$

$\int \mathcal{L} \sim 330 \text{ pb}^{-1}$ per experiment

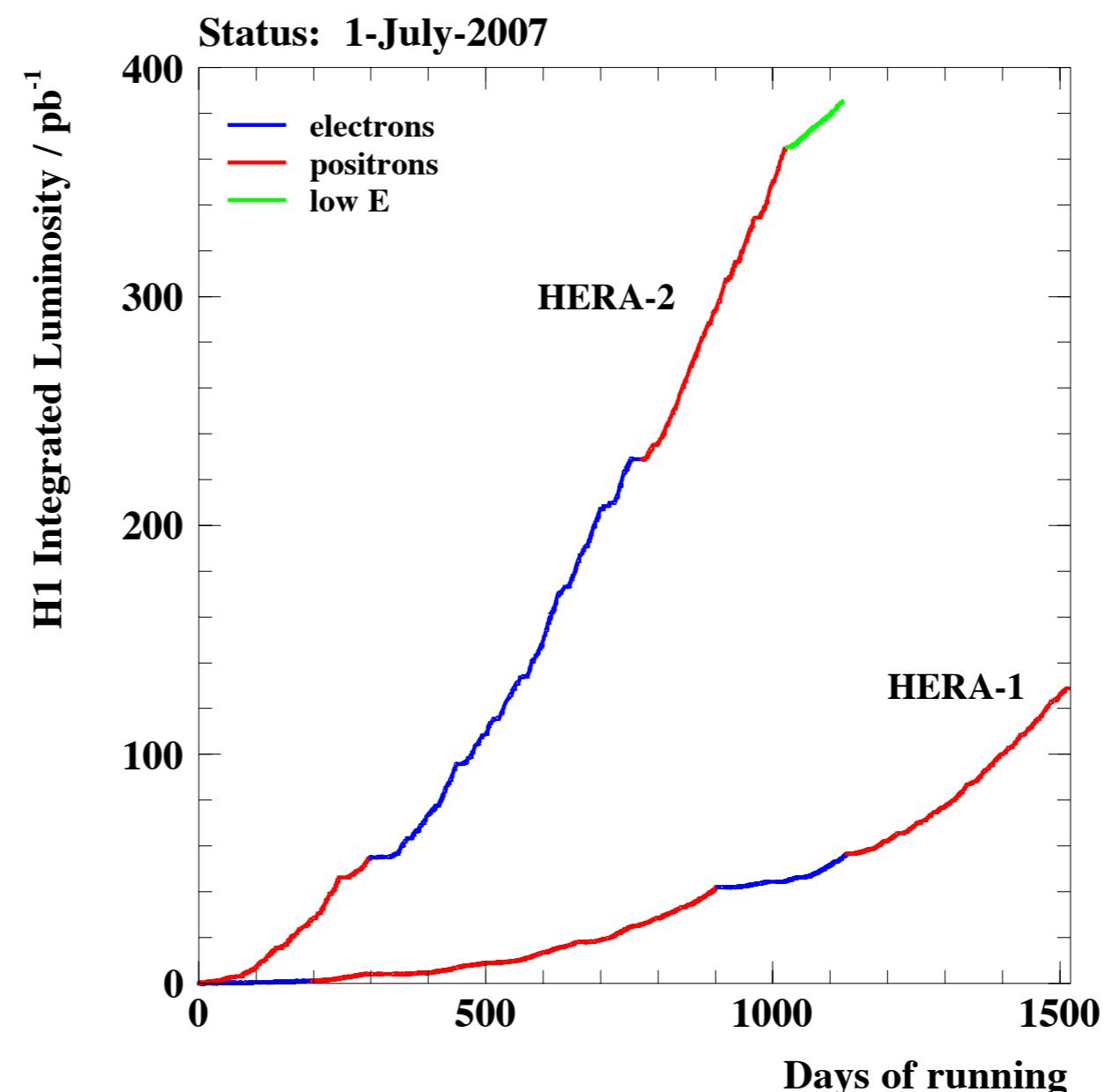
Longitudinally polarised leptons

Low Energy Run 2007

$E_e = 27.6 \text{ GeV}$

$E_p = 575 \& 460 \text{ GeV}$

Dedicated F_L measurement





Summary of HERA-I datasets
Combined in HERAPDF1.0

Available since 2009

Data Set		x Range		Q^2 Range GeV 2		\mathcal{L} pb $^{-1}$	e^+e^-	\sqrt{s} GeV
H1 svx-mb	95-00	5×10^{-6}	0.02	0.2	12	2.1	e^+p	301-319
H1 low Q^2	96-00	2×10^{-4}	0.1	12	150	22	e^+p	301-319
H1 NC	94-97	0.0032	0.65	150	30000	35.6	e^+p	301
H1 CC	94-97	0.013	0.40	300	15000	35.6	e^+p	301
H1 NC	98-99	0.0032	0.65	150	30000	16.4	e^-p	319
H1 CC	98-99	0.013	0.40	300	15000	16.4	e^-p	319
H1 NC HY	98-99	0.0013	0.01	100	800	16.4	e^-p	319
H1 NC	99-00	0.0013	0.65	100	30000	65.2	e^+p	319
H1 CC	99-00	0.013	0.40	300	15000	65.2	e^+p	319
ZEUS BPC	95	2×10^{-6}	6×10^{-5}	0.11	0.65	1.65	e^+p	301
ZEUS BPT	97	6×10^{-7}	0.001	0.045	0.65	3.9	e^+p	301
ZEUS SVX	95	1.2×10^{-5}	0.0019	0.6	17	0.2	e^+p	301
ZEUS NC	96-97	6×10^{-5}	0.65	2.7	30000	30.0	e^+p	301
ZEUS CC	94-97	0.015	0.42	280	17000	47.7	e^+p	301
ZEUS NC	98-99	0.005	0.65	200	30000	15.9	e^-p	319
ZEUS CC	98-99	0.015	0.42	280	30000	16.4	e^-p	319
ZEUS NC	99-00	0.005	0.65	200	30000	63.2	e^+p	319
ZEUS CC	99-00	0.008	0.42	280	17000	60.9	e^+p	319

High Q^2 NC and CC data limited to
100 pb $^{-1}$ e^+p
16 pb $^{-1}$ e^-p

HERA Structure Function Data



Up till now HERA-II datasets only partially published

ZEUS CC e^-p	175 pb^{-1}	EPJ C 61 (2009) 223-235
ZEUS CC e^+p	132 pb^{-1}	EPJ C 70 (2010) 945-963
ZEUS NC e^-p	170 pb^{-1}	EPJ C 62 (2009) 625-658
ZEUS NC e^+p	135 pb^{-1}	ZEUS-prel-11-003
HI CC e^-p	149 pb^{-1}	HIprelim-09-043
HI CC e^+p	180 pb^{-1}	HIprelim-09-043
HI NC e^-p	149 pb^{-1}	HIprelim-09-042
HI NC e^+p	180 pb^{-1}	HIprelim-09-042



ZEUS CC e^-p	175 pb^{-1}	EPJ C 61 (2009) 223-235
ZEUS CC e^+p	132 pb^{-1}	EPJ C 70 (2010) 945-963
ZEUS NC e^-p	170 pb^{-1}	EPJ C 62 (2009) 625-658
ZEUS NC e^+p	135 pb^{-1}	arXiv:1208.6138
HI CC e^-p	149 pb^{-1}	arXiv:1206.7007
HI CC e^+p	180 pb^{-1}	
HI NC e^-p	149 pb^{-1}	
HI NC e^+p	180 pb^{-1}	



HERA-II datasets
Combined in HERAPDF1.5
(except ZEUS NC e^+p)

breakdown of HERA-II data samples

	R	L
e^-p	$\mathcal{L} = 47.3 \text{ pb}^{-1}$ $P_e = (+36.0 \pm 1.0)\%$	$\mathcal{L} = 104.4 \text{ pb}^{-1}$ $P_e = (-25.8 \pm 0.7)\%$
e^+p	$\mathcal{L} = 101.3 \text{ pb}^{-1}$ $P_e = (+32.5 \pm 0.7)\%$	$\mathcal{L} = 80.7 \text{ pb}^{-1}$ $P_e = (-37.0 \pm 0.7)\%$

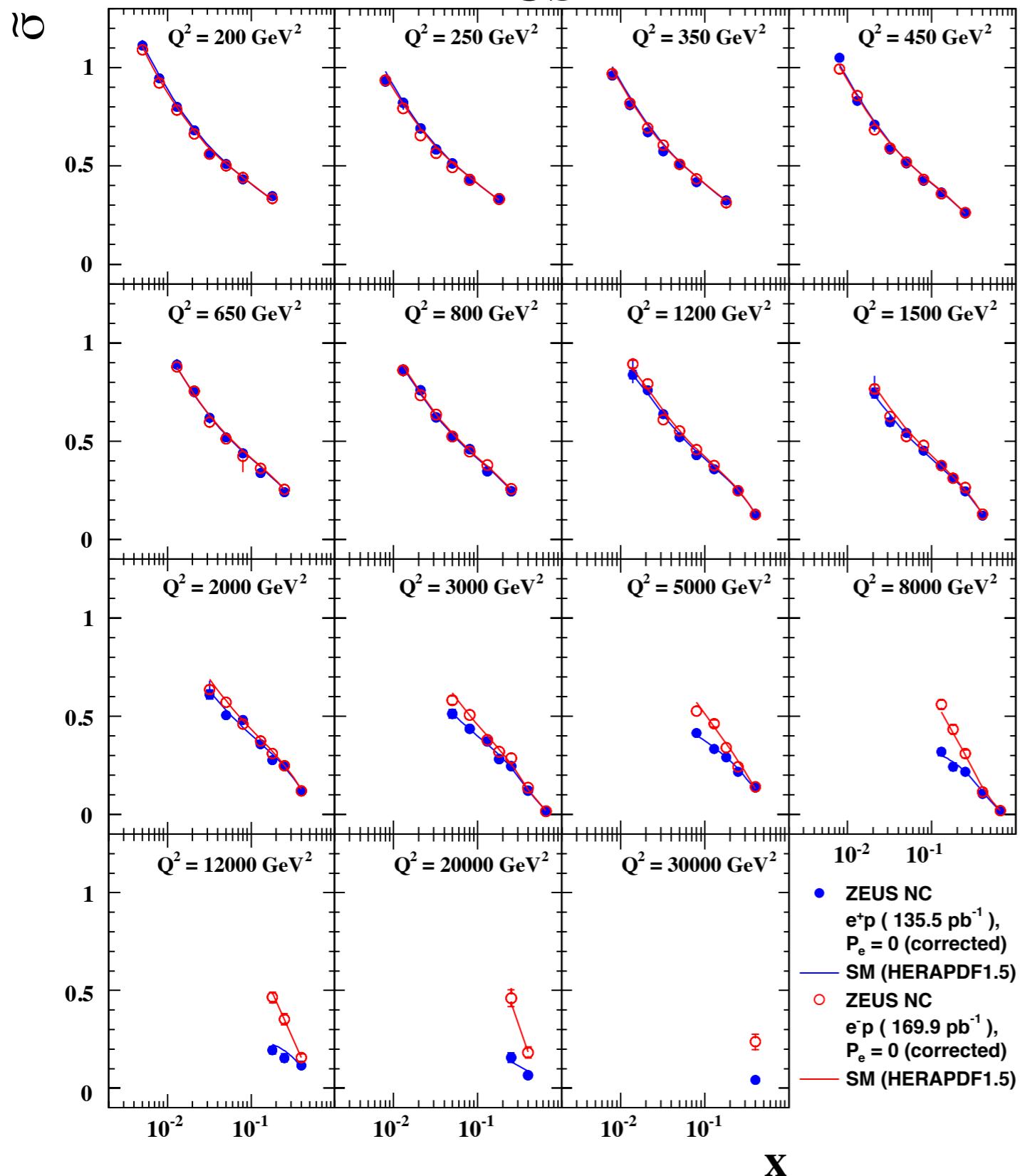
Complete the analyses of HERA high Q^2 inclusive structure function data

New published data increase $\int \mathcal{L}$ by
~ factor 3 for e^+p
~ factor 10 for e^-p
much improved systematic uncertainties

High Q^2 NC Cross Sections



ZEUS



High Q^2 is the EW physics regime

Final measurement of ZEUS NC e^+p data

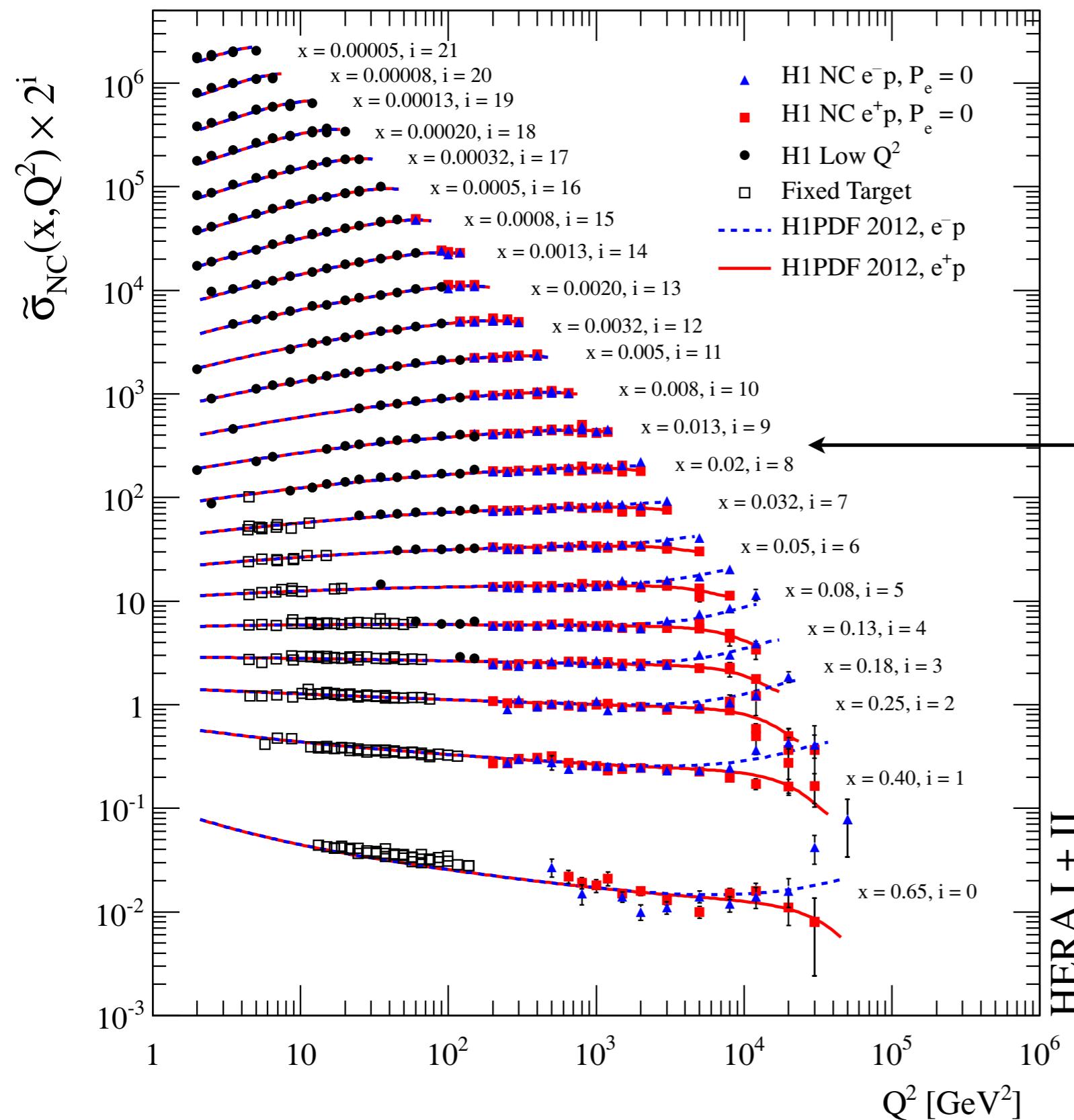
Shown here for $P=0$
Polarised measurements also available

Compared to published NC e^-p data

High Q^2 NC Cross Sections



H1 Collaboration



H1 precision 1.5% for $Q^2 < 500 \text{ GeV}^2$
 \Rightarrow factor 2 reduction in error wrt HERA-I

Statistics limited at higher Q^2 and high x

Extended reach at high x compared to H1
preliminary data

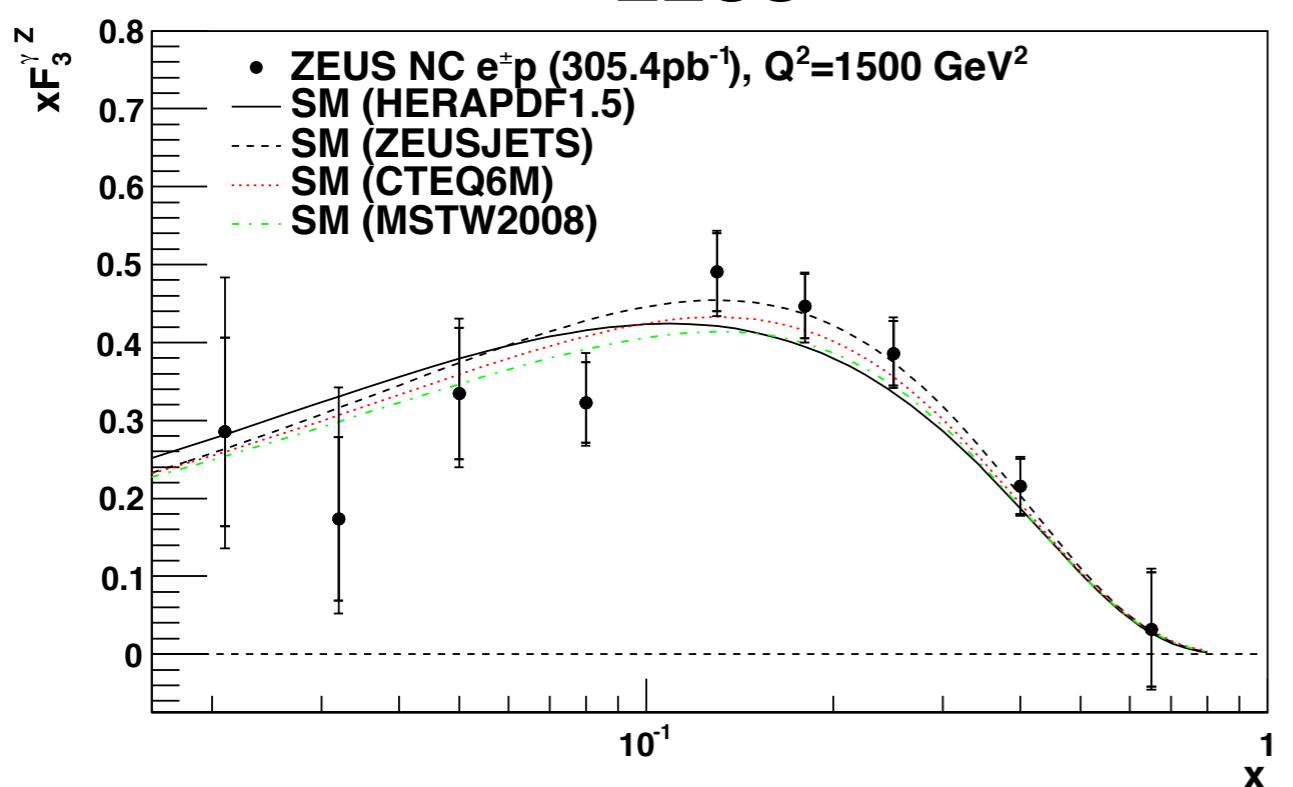
This x region is the ‘sweet spot’
High precision with long Q^2 lever arm
 x -range relevant for Higgs production

Combination of high Q^2 data
HERA-I and HERA-II

Larger HERA-II luminosity
 \rightarrow improved precision at high x / Q^2

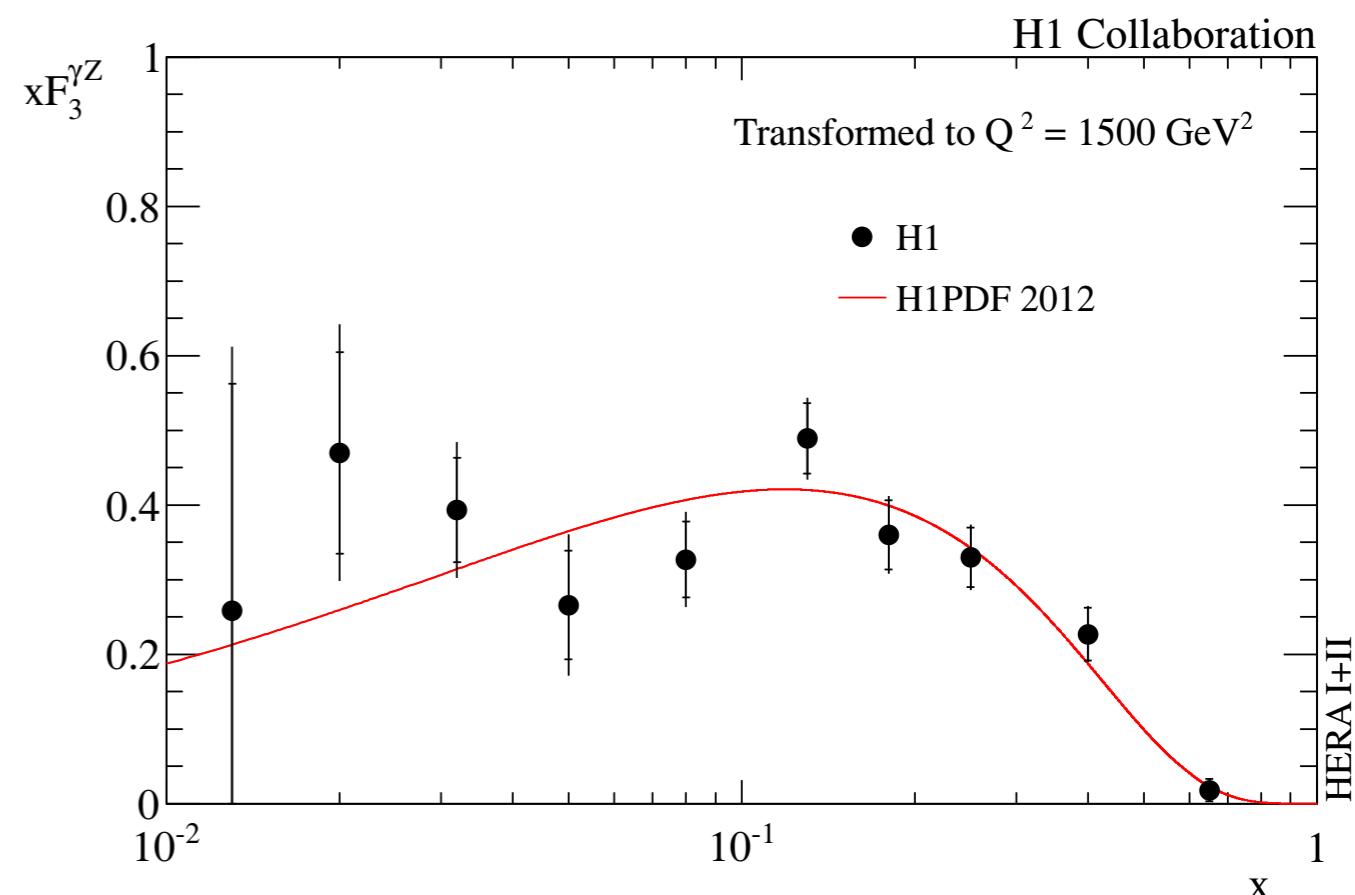


ZEUS



At high Q^2 $x F_3$ arises due to Z^0 effects
enhanced e^- cross section wrt e^+

Difference is $x F_3$
Sensitive to valence PDFs



$$x \tilde{F}_3 = \frac{Y_+}{2Y_-} (\tilde{\sigma}_{NC}^- - \tilde{\sigma}_{NC}^+) \approx a_e \chi_Z x F_3^{\gamma Z}$$

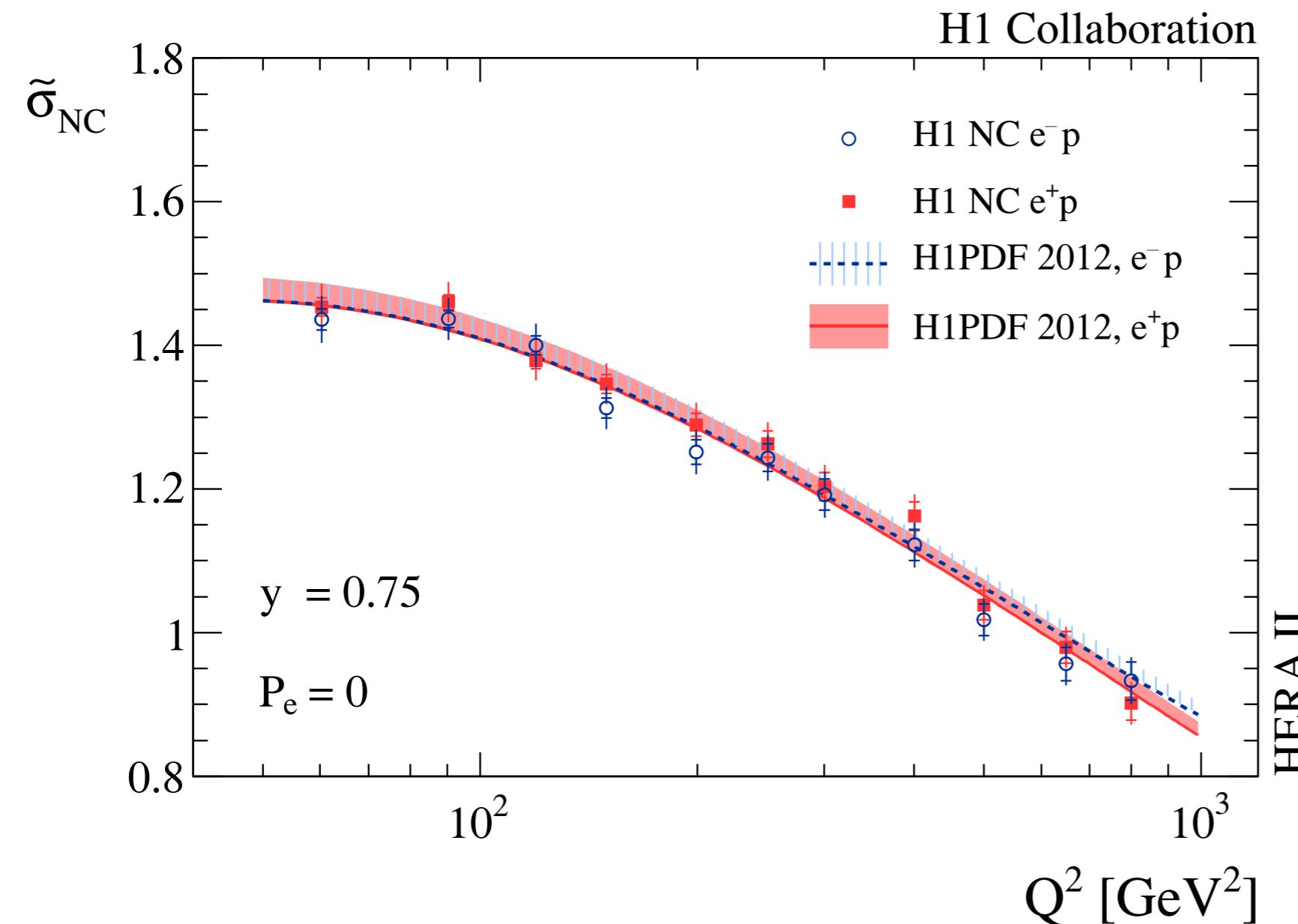
$$x \tilde{F}_3 \propto \sum (x q_i - x \bar{q}_i)$$

H1 measure integral of $x F_3^{\gamma Z}$ - validate sumrule:

$$\int_{0.016}^{0.725} dx F_3^{\gamma Z}(x, Q^2 = 1500 \text{ GeV}^2) = 1.22 \pm 0.09(\text{stat}) \pm 0.07(\text{syst})$$

LO integral predicted to
be $5/3 + \mathcal{O}(\alpha_S/\pi)$

NC Cross Sections at High y



Measurement extension to high y at high Q^2

Sensitive to F_L and xg

Difficult measurement:
 - low scattered electron energy $E_e > 5 \text{ GeV}$
 - large photoproduction background

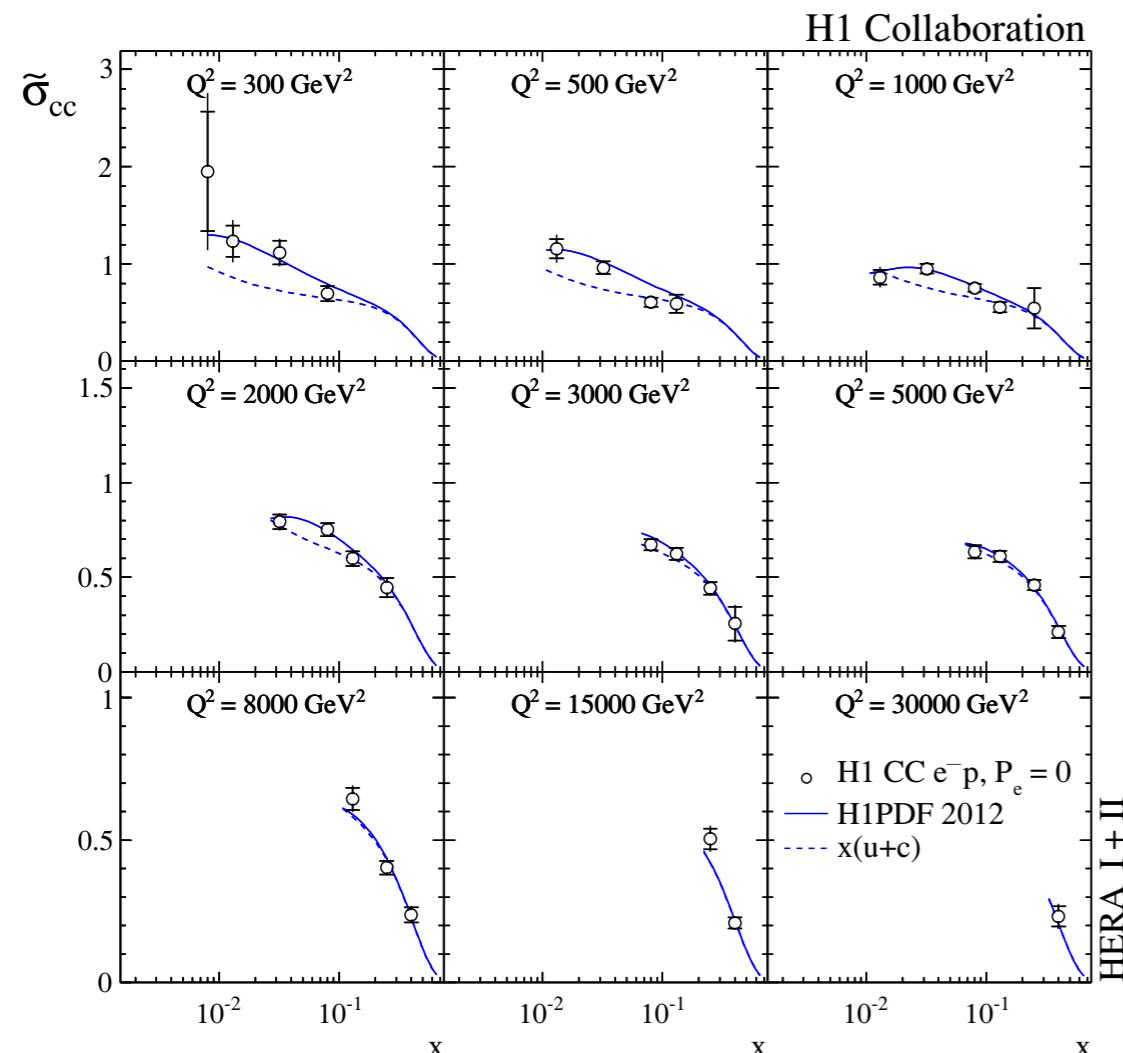
Total uncertainty reduced by factor 2:
 HERA-I ~4%
 HERA-II ~2%

High Q^2 CC Cross Sections



Electron scattering

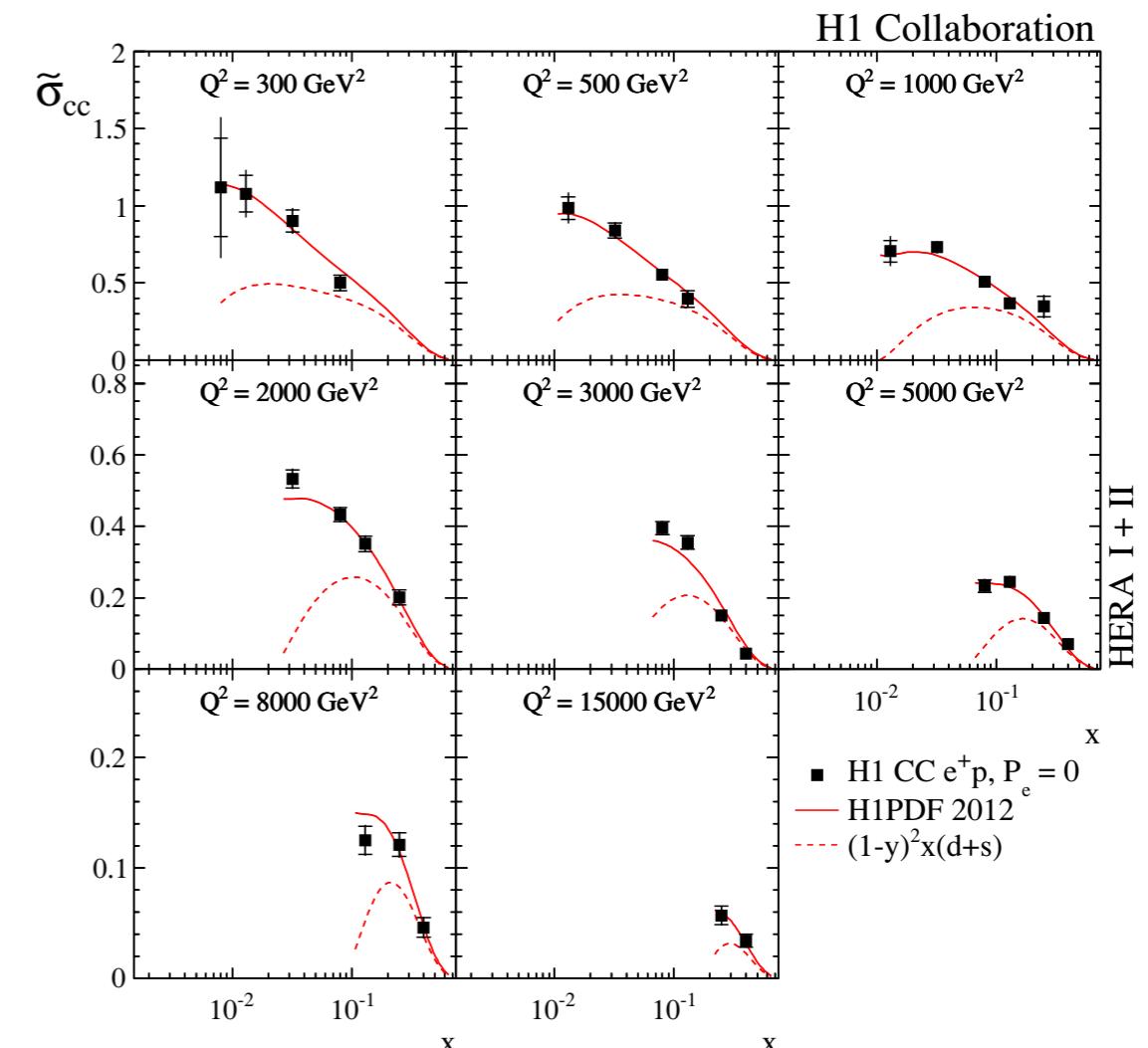
$$\frac{d^2\sigma_{CC}^-}{dx dQ^2} = \frac{G_F^2}{2\pi} \left(\frac{M_W^2}{M_W^2 + Q^2} \right)^2 \left[(u+c) + (1-y)^2(\bar{d} + \bar{s}) \right]$$



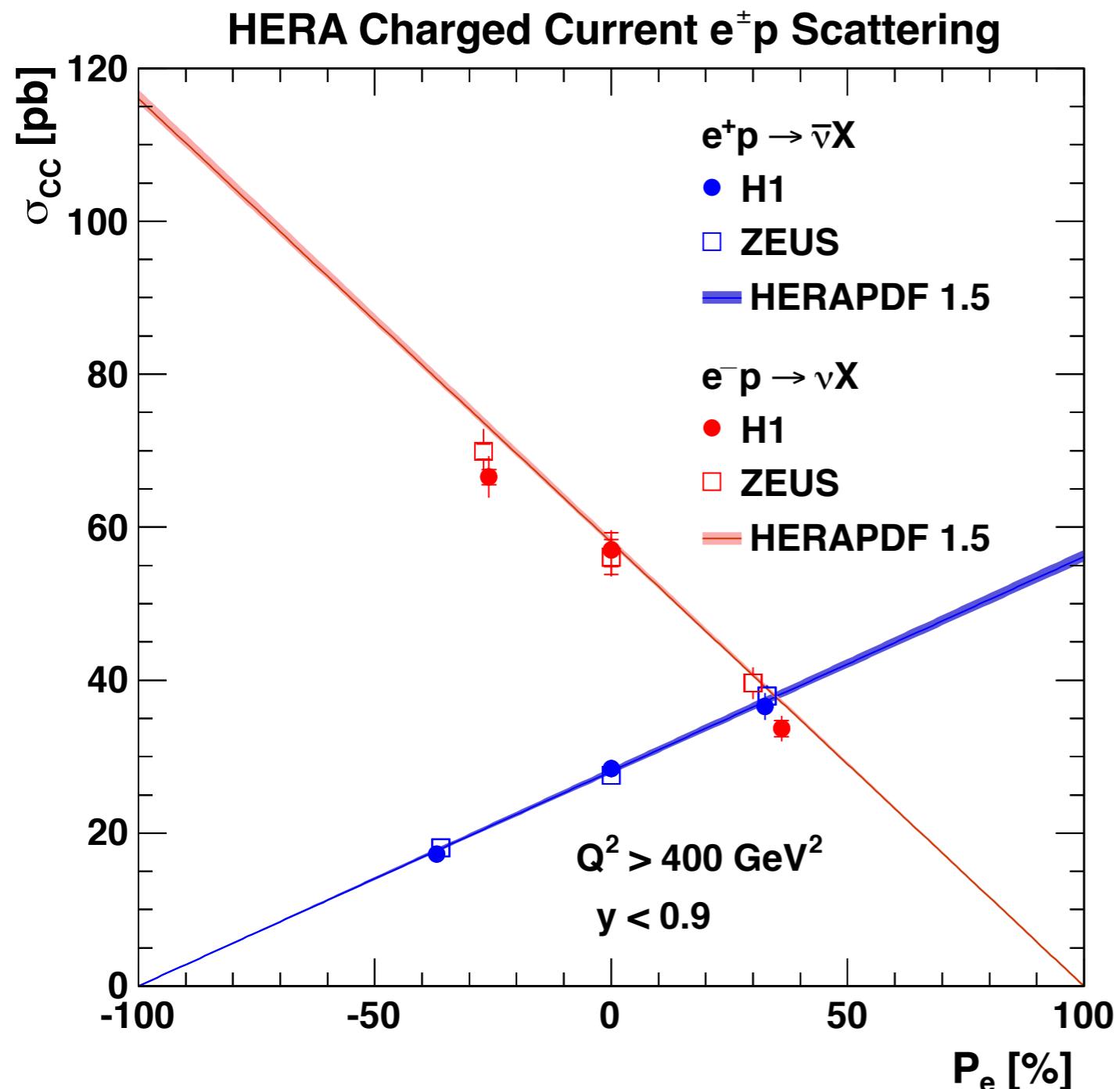
H1 combination of high Q^2 CC data (HERA-I+II)
 Improvement of total uncertainty
 Dominated by statistical errors
 Provide important flavour decomposition information

Positron scattering

$$\frac{d^2\sigma_{CC}^+}{dx dQ^2} = \frac{G_F^2}{2\pi} \left(\frac{M_W^2}{M_W^2 + Q^2} \right)^2 \left[(\bar{u} + \bar{c}) + (1-y)^2(d + s) \right]$$

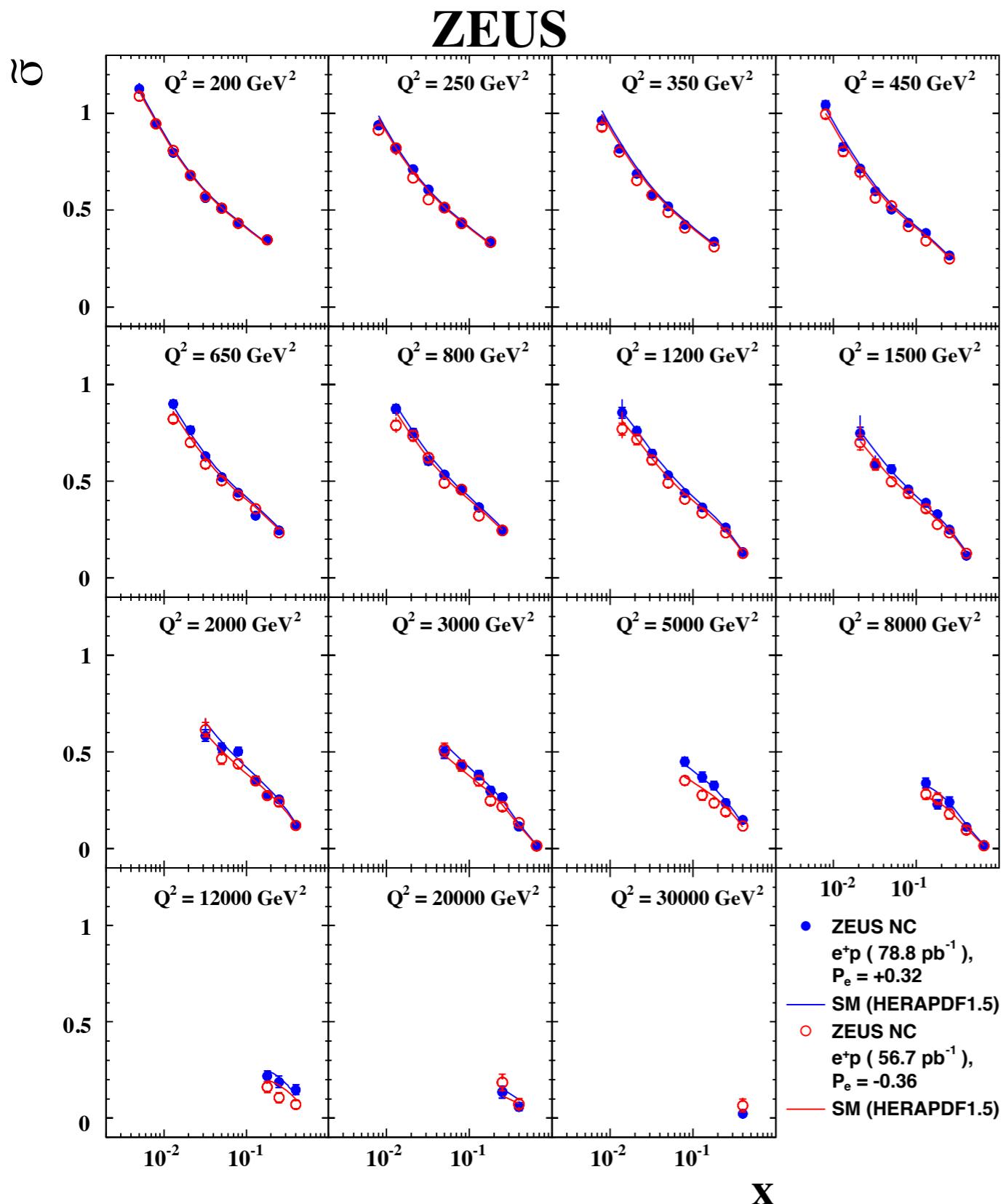


CC e^+ data provide strong d_v constraint at high x
 Precision limited by statistics: typically 5-10%
 HERA-I precision of 10-15% for $e^+ p$
 Large gain to come after combination with ZEUS



Polarisation dependence of CC cross section
now final from H1 and ZEUS

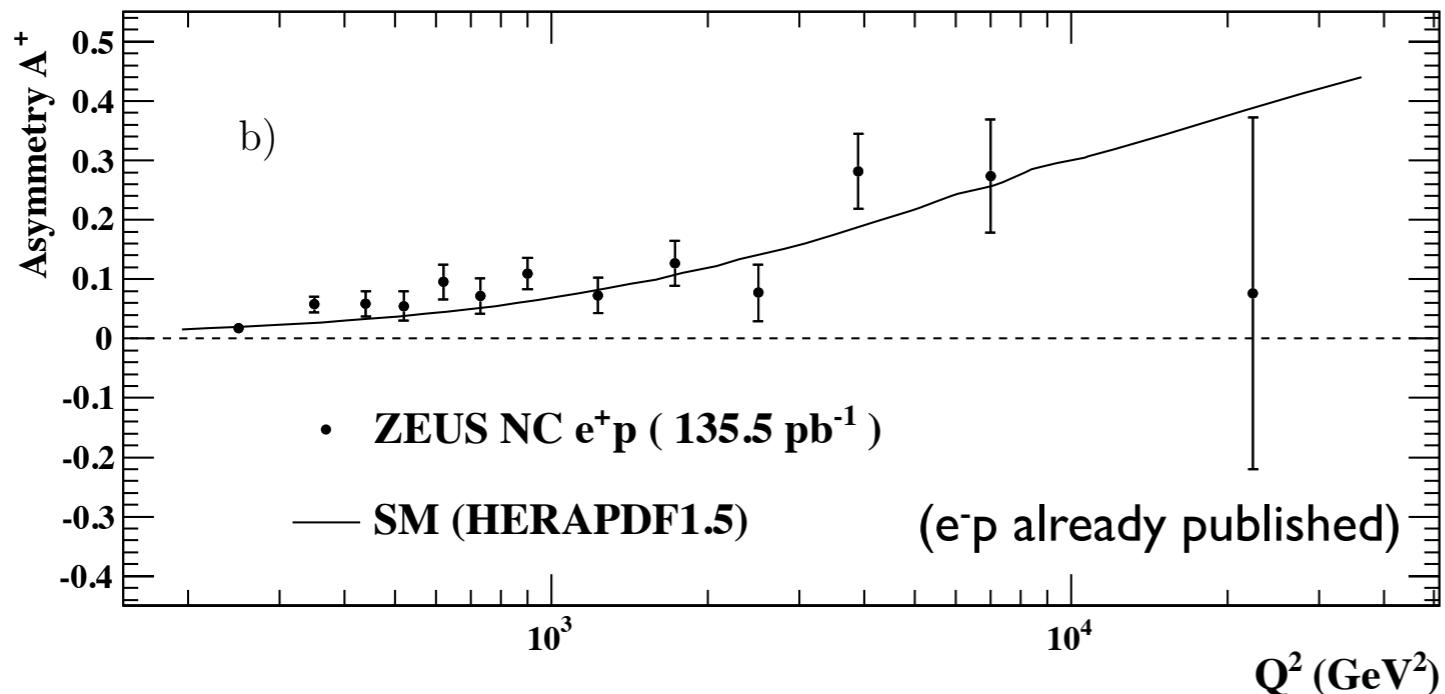
Polarised NC Cross Sections



Polarised NC measurements completed
for e^+p , e^-p , L-handed, R-handed scattering

Difference in L,R scattering visible at high Q^2

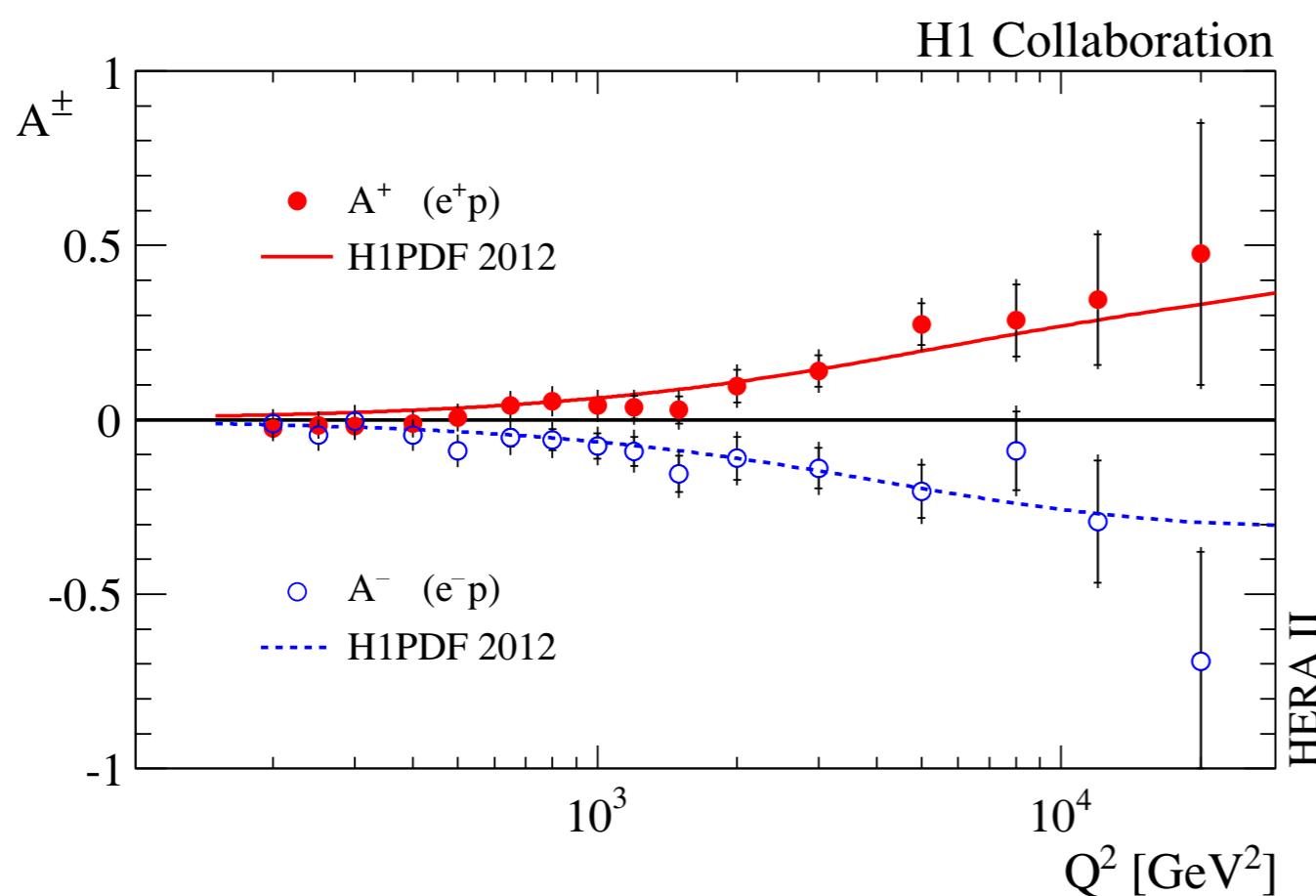
NC Polarisation Asymmetry



NC polarisation asymmetry:

$$A^\pm = \frac{2}{P_L^\pm - P_R^\pm} \cdot \frac{\sigma^\pm(P_L^\pm) - \sigma^\pm(P_R^\pm)}{\sigma^\pm(P_L^\pm) + \sigma^\pm(P_R^\pm)}$$

At large x $A^\pm \propto \pm \kappa \frac{1 + d_v/u_v}{4 + d_v/u_v}$

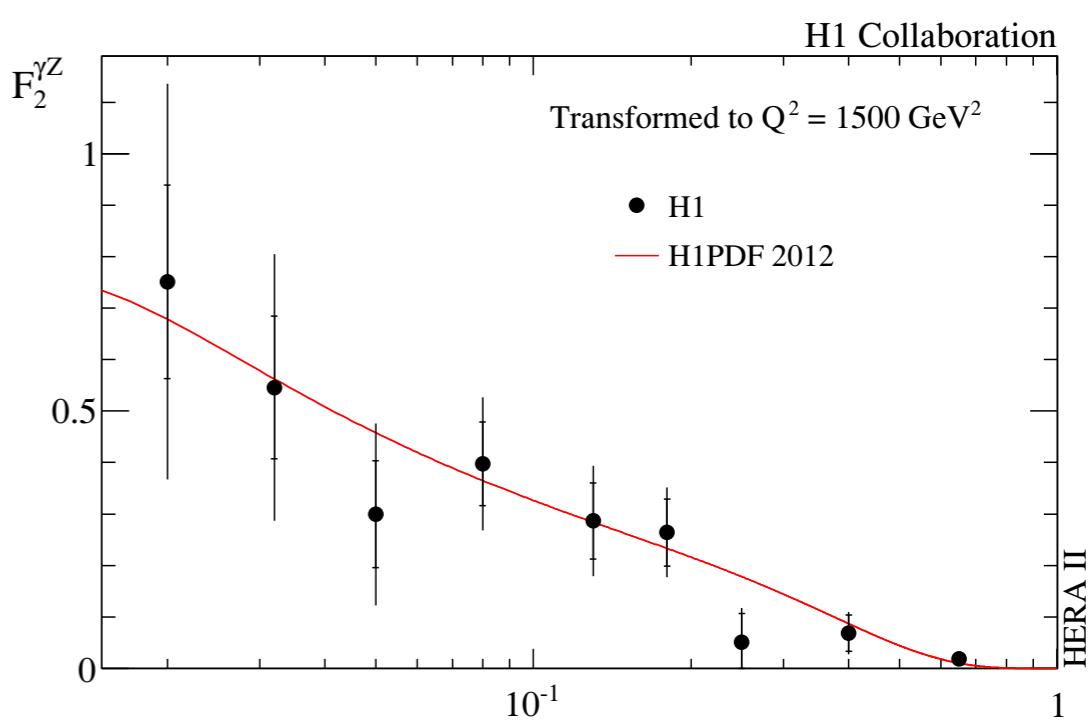
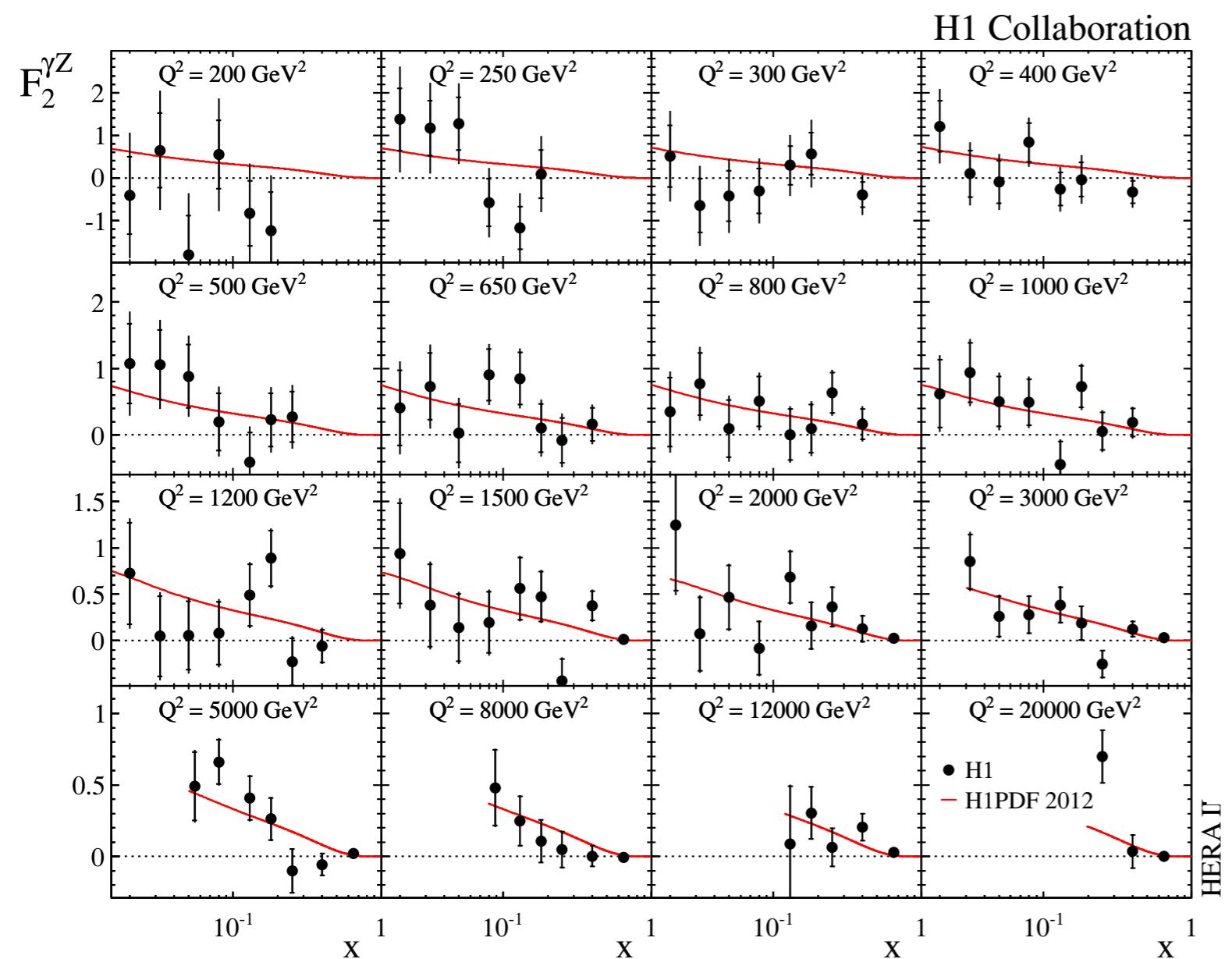




Measuring the difference in NC polarised cross sections gives access to new structure functions:

$$\frac{\sigma^\pm(P_L^\pm) - \sigma^\pm(P_R^\pm)}{P_L^\pm - P_R^\pm} = \frac{\kappa Q^2}{Q^2 + M_Z^2} \left[\boxed{\mp a_e F_2^{\gamma Z}} + \frac{Y_-}{Y_+} v_e x F_3^{\gamma Z} - \frac{Y_-}{Y_+} \frac{\kappa Q^2}{Q^2 + M_Z^2} (v_e^2 + a_e^2) x F_3^Z \right]$$

xF₃ terms eliminated by subtracted e⁻p from e⁺p



Combined H1 Data



New H1 data are combined with all previously published H1 inclusive cross section measurements

854 data points averaged to 413 measurements

$$\chi^2/\text{ndf} = 412/441 = 0.93$$

Normalisation shifts for H1 data after averaging

Source	Shift in units of standard deviation	Shift in % of cross section
$\delta^{\mathcal{L}1}$ (BH Theory)	-0.39	-0.19
$\delta^{\mathcal{L}2}$ (e^+ 94-97)	-0.46	-0.66
$\delta^{\mathcal{L}3}$ (e^- 98-99)	-0.69	-1.20
$\delta^{\mathcal{L}4}$ (e^+ 99-00)	-0.07	-0.10
$\delta^{\mathcal{L}5}$ (QEDC)	0.81	1.70
$\delta^{\mathcal{L}6}, \delta^{\mathcal{L}7}$ ($e^+ L + R$)	0.84	0.80
$\delta^{\mathcal{L}8}, \delta^{\mathcal{L}9}$ ($e^- L + R$)	0.84	0.89

Precision medium Q^2
HERA-I data ~unshifted

New high Q^2 HERA-II
data shifted by ~1.7%
(less than 1 std.dev)



New PDF fit performed: can be thought of as a ‘stepping-stone’ towards HERAPDF2.0

$$\begin{aligned}xg(x) &= A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{25}, \\ xu_v(x) &= A_{uv} x^{B_{uv}} (1-x)^{C_{uv}} (1+E_{uv} x^2), \\ xd_v(x) &= A_{dv} x^{B_{dv}} (1-x)^{C_{dv}}, \\ x\bar{U}(x) &= A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}}, \\ x\bar{D}(x) &= A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}. \end{aligned}$$

Parameter	Central Value	Lower Limit	Upper Limit
f_s	0.31	0.23	0.38
m_c (GeV)	1.4	1.35 (for $Q_0^2 = 1.8$ GeV)	1.65
m_b (GeV)	4.75	4.3	5.0
Q_{\min}^2 (GeV 2)	3.5	2.5	5.0
Q_0^2 (GeV 2)	1.9	1.5 ($f_s = 0.29$)	2.5 ($m_c = 1.6$, $f_s = 0.34$)

13 parameter fit: additional flexibility given to u_v and d_v compared to H1PDF2009 / HERAPDF1.0

Apply momentum/counting sum rules:

$$\int_0^1 dx \cdot (xu_v + xd_v + x\bar{U} + x\bar{D} + xg) = 1$$

$$\int_0^1 dx \cdot u_v = 2 \quad \int_0^1 dx \cdot d_v = 1$$

Parameter constraints:

$$B_{U\bar{U}} = B_{D\bar{D}}$$

$$sea = 2 \times (U\bar{U} + D\bar{D})$$

$$U\bar{U} = D\bar{D} \text{ at } x=0$$

$$f_s = s\bar{s}/D\bar{D}$$

$$Q_0^2 = 1.9 \text{ GeV}^2 \text{ (below } m_c)$$

$$Q^2 > 3.5 \text{ GeV}^2$$

$$2 \times 10^{-4} < x < 0.65$$

Fits performed using RT-VFNS

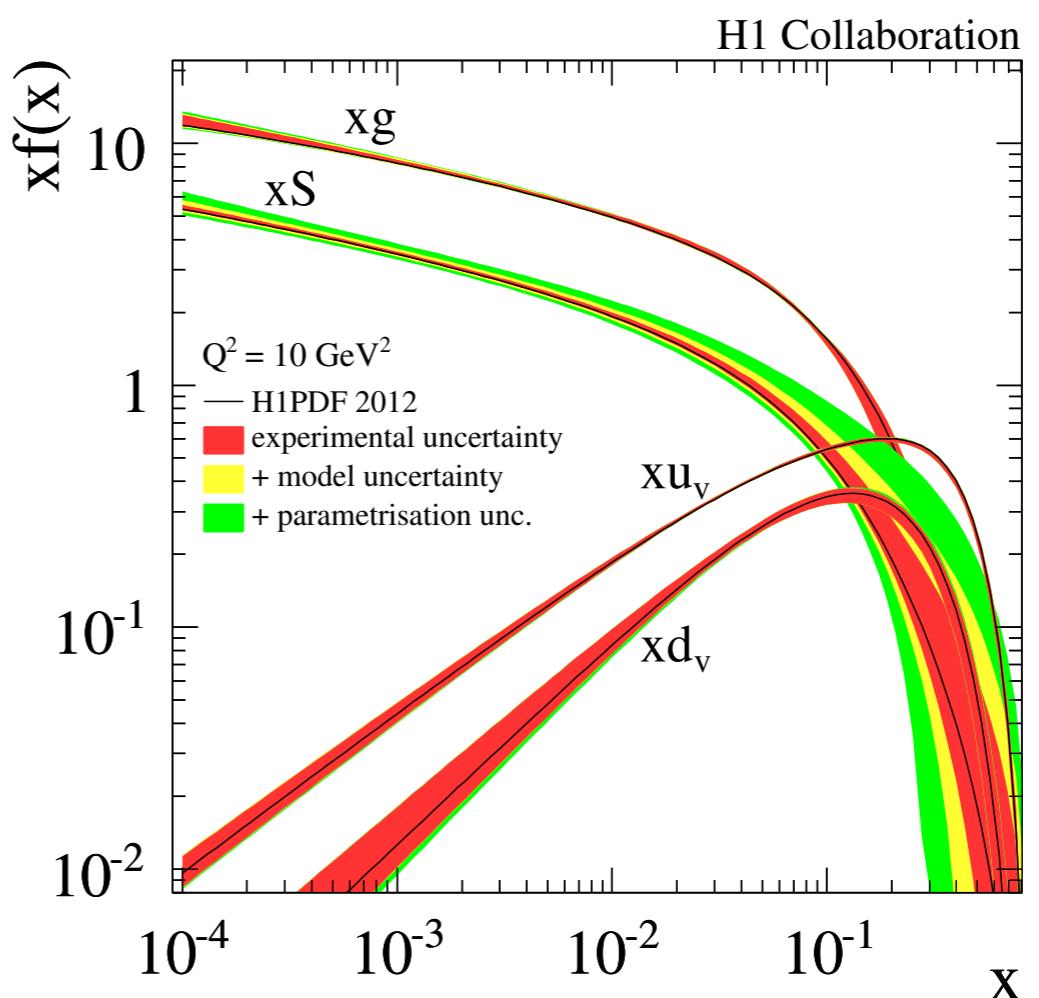
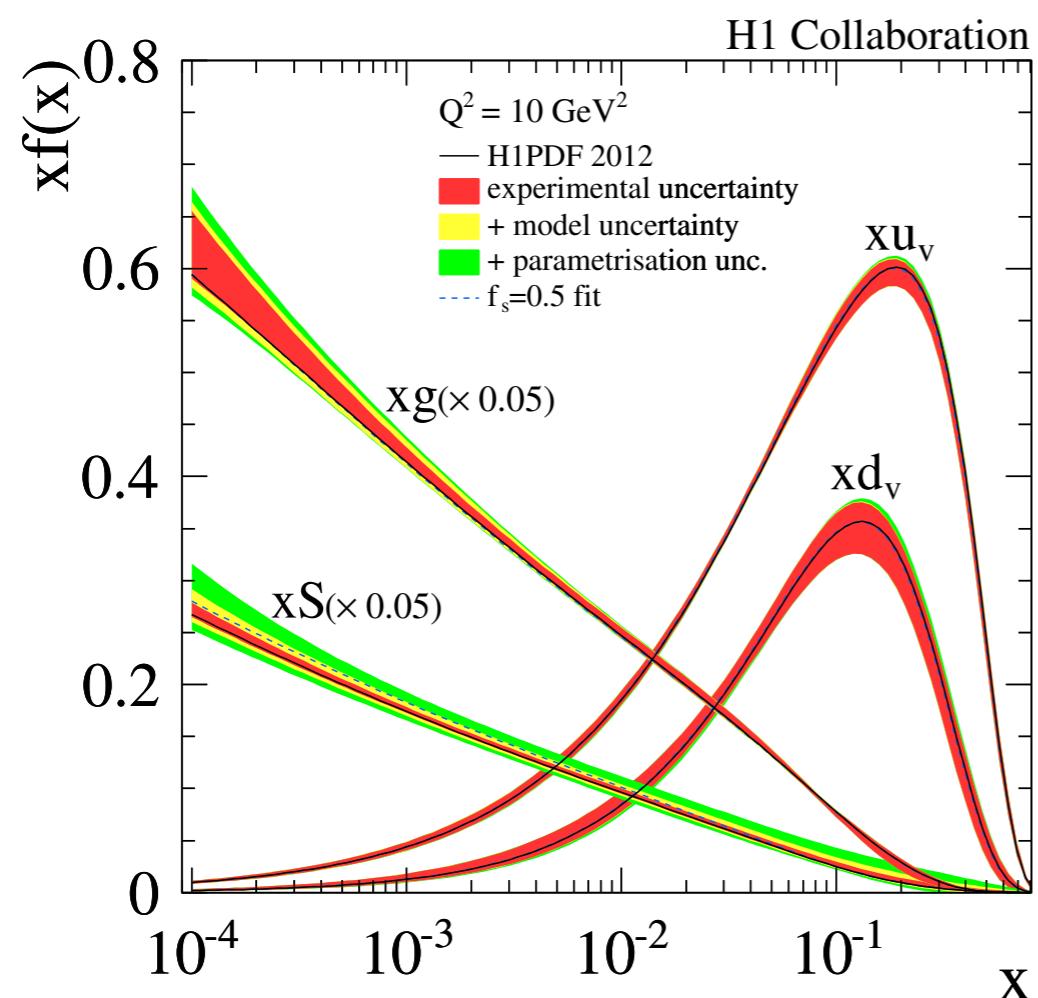
Experimental uncertainties produced using RMS spread of 400 replica fits

Parameterisation uncertainty determined from envelope of 14 parameter fit & Q_0^2 variations

Error band is applied to central value fit \Rightarrow asymmetric errors since mean of replicas \neq central fit

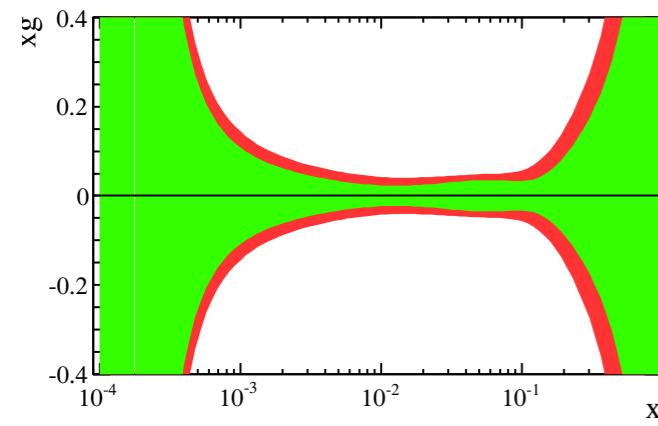
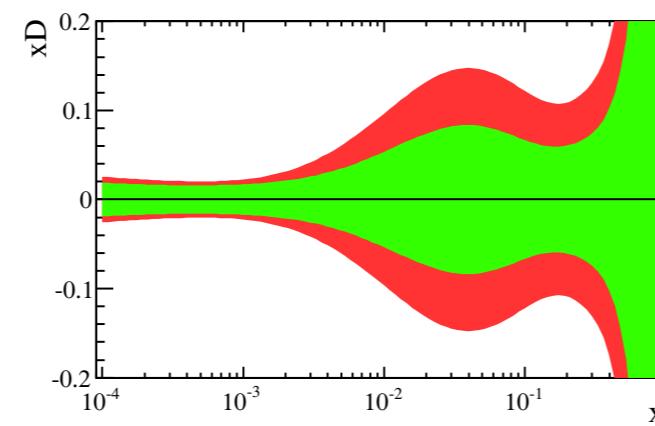
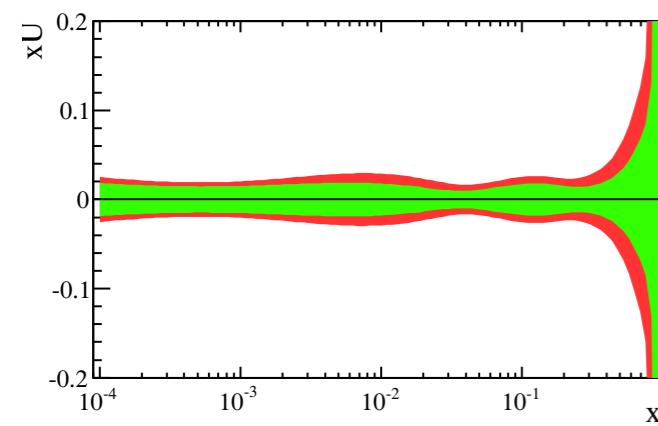
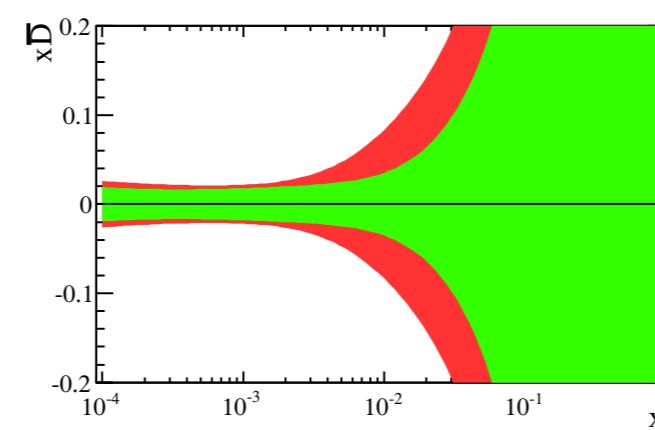
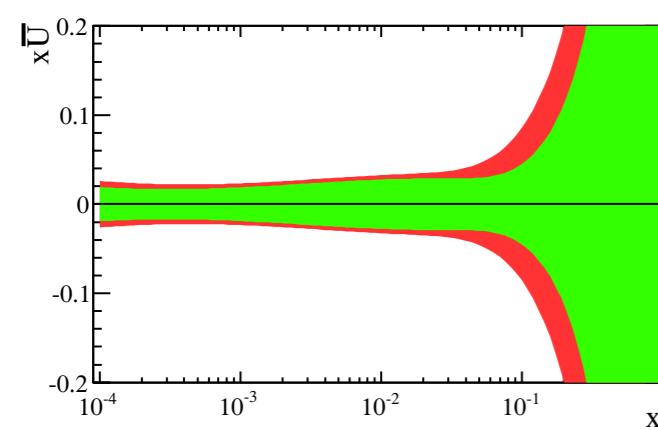
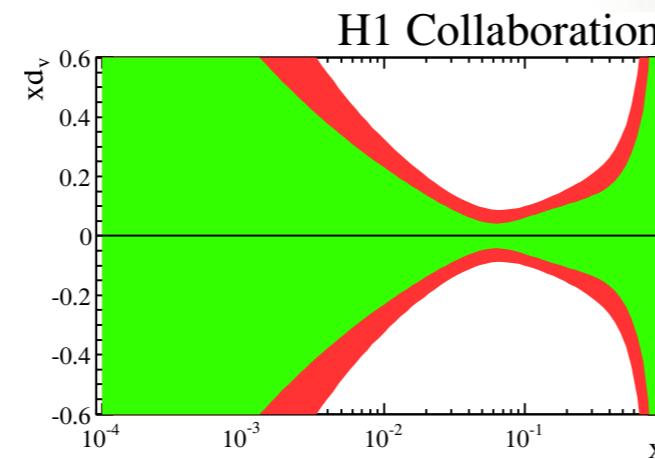
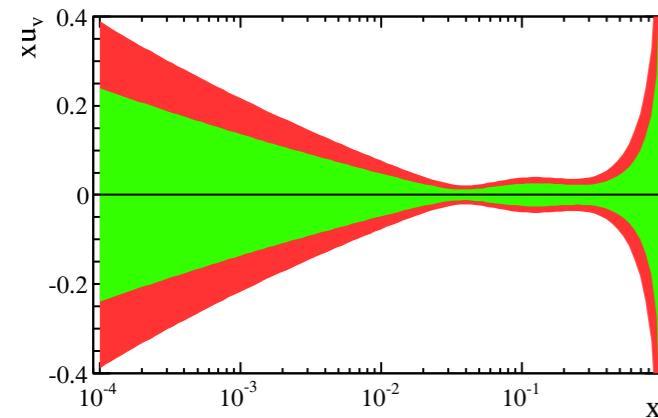
$$\chi^2 = \sum_i \frac{\left[\mu_i - m_i \left(1 - \sum_j \gamma_j^i b_j \right) \right]^2}{\delta_{i,\text{unc}}^2 m_i^2 + \delta_{i,\text{stat}}^2 \mu_i m_i} + \sum_j b_j^2 + \sum_i \ln \frac{\delta_{i,\text{unc}}^2 m_i^2 + \delta_{i,\text{stat}}^2 \mu_i m_i}{\delta_{i,\text{unc}}^2 \mu_i^2 + \delta_{i,\text{stat}}^2 \mu_i^2}$$

modified χ^2 definition includes ln term to account for likelihood transition to χ^2 after error scaling



$$\chi^2/\text{ndf} = 1570/1461 = 1.07$$

Fit with unsuppressed strange sea ($f_s=0.5$) is well within error bands



Uncert. due to H1 HERA I data

Uncert. due to H1 HERA I+II data

$Q^2 = 1.9 \text{ GeV}^2$

Comparison of PDF uncertainties from H1 fits with and without new HERA-II data

Large improvement in xd_v and xD over wide x range - driven by more precise CC e^+p data

Improvement in xu_v from NC at high x .
Error reduction at low x arises from sum rules

High x gluon is also improved from scaling violations



HERAPDF1.0

Combine NC and CC HERA-I data from HI & ZEUS

Complete MSbar NLO fit

NLO: standard parameterisation with 10 parameters

$\alpha_s = 0.1176$ (fixed in fit)

HERAPDF1.5

Include additional NC and CC HERA-II data

Complete MSbar NLO and NNLO fit

NLO: standard parameterisation with 10 parameters

HERAPDF1.5f

NNLO: extended fit with 14 parameters

HERAPDF1.6

Include additional NC inclusive jet data $5 < Q^2 < 15000$

Complete MSbar NLO fit

NLO: standard parameterisation with 14 parameters

$\alpha_s = 0.1202 \pm 0.0013$ (exp) ± 0.004 (scales) free in fit

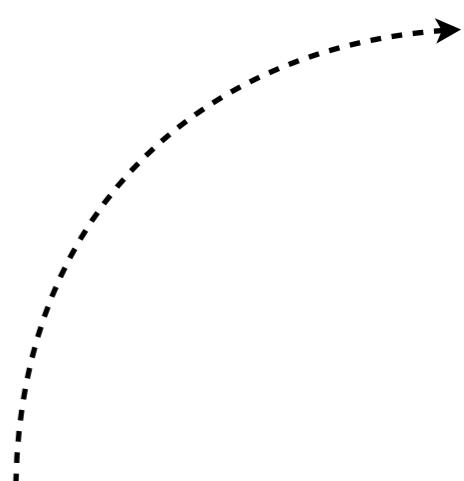
HERAPDF1.7

Include 41 additional F_2^{cc} data $4 < Q^2 < 1000$

Include 224 combined cross section points $E_p=575/460$ GeV

Complete MSbar NLO fit

NLO: standard parameterisation with 14 parameters





HERAPDF2.0

Include final:

HERA-I low/medium Q^2 precision F_2

HERA-II high Q^2 polarised NC/CC data

HERA-II low/medium energy NC data

HERA-I+II F_2^{cc} combined data - almost ready

HERA-I+II multijet data - awaiting H1 publication

Combined F_2^{cc} now at 2nd stage of internal review

Expect journal submission ~ early Nov.

Final structure function measurements from H1 / ZEUS now published

Combination of the data is underway

New combination will include:

HERA-I published data

HERA-II published data

low/medium energy $E_p=575/460$ GeV run data

Expect several fits:

NLO vs NNLO

NLO will be: inclusive NC/CC data & inclusive + F_2^{cc} (+ jets?)

Include fit to α_s

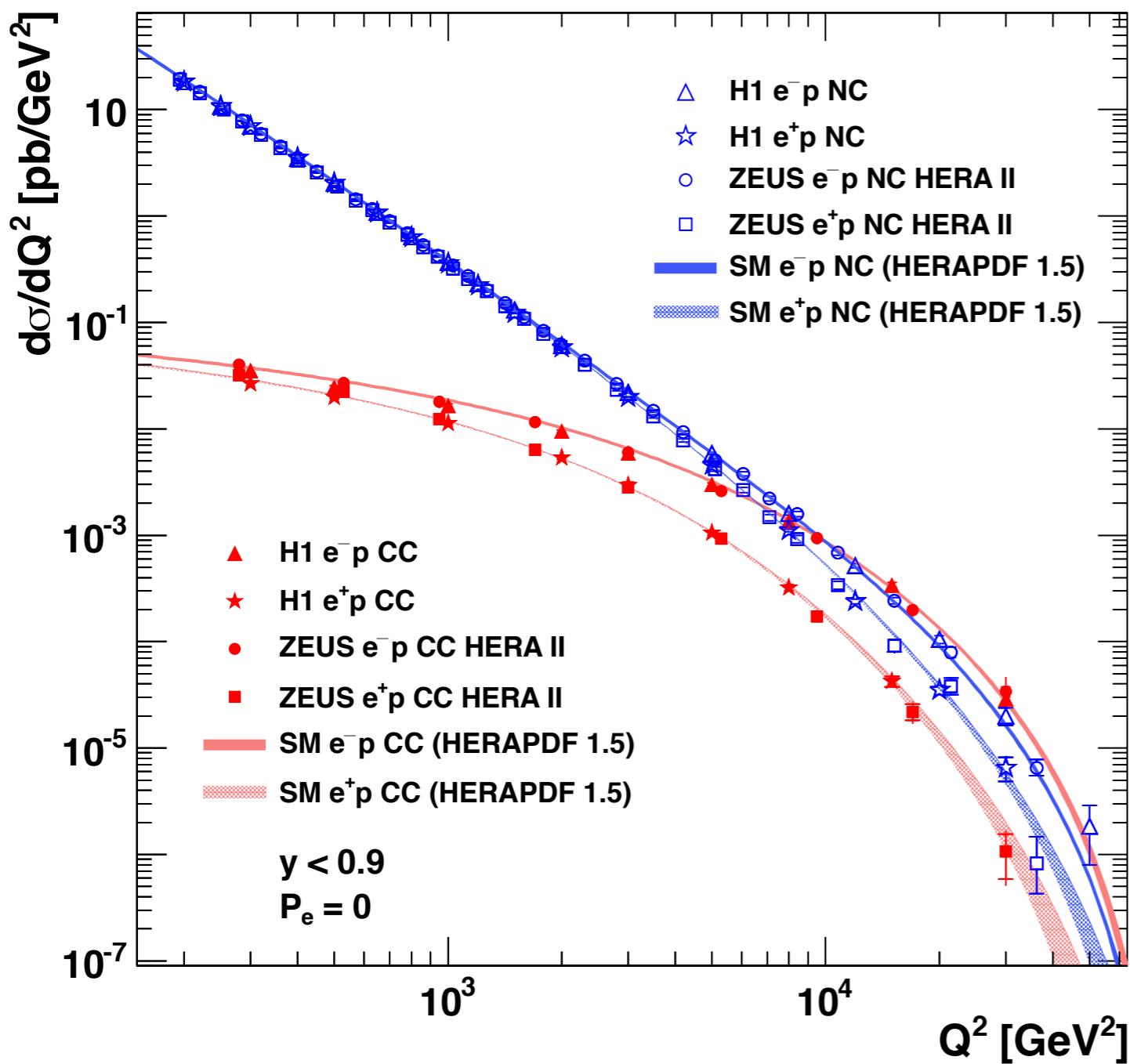
MC method for experimental errors will be used

Timescale ~ spring 2013 (DIS workshop?)

Conclusions



HERA



- H1 / ZEUS completed their final SF measurements
- New HERA-II data provide tighter constraints at high x / Q^2
- These data provide some of the most stringent constraints on PDFs
- Stress-test of QCD over 4 orders of mag. in Q^2
- DGLAP evolution works very well
- HERA data provide a self-consistent data set for complete flavour decomposition of the proton
- New combination of HERA data underway
- Combination \Rightarrow HERAPDF2.0 QCD fit

Backup Slides



H1 Systematic Error Source Correlation



Data set	$\delta^{\mathcal{L}}$	δ^E	δ^θ	δ^h	δ^N	δ^B	δ^V	δ^S	δ^{pol}
e^+ Combined low Q^2	$\delta^{\mathcal{L}1}$								
e^+ Combined low E_p	$\delta^{\mathcal{L}1}$								
e^+ NC 94-97	$\delta^{\mathcal{L}1}$	$\delta^{\mathcal{L}2}$	δ^{E1}	$\delta^{\theta1}$	δ^{h1}	δ^{N1}	δ^{B1}	—	—
e^+ CC 94-97	$\delta^{\mathcal{L}1}$	$\delta^{\mathcal{L}2}$	—	—	δ^{h1}	δ^{N1}	δ^{B1}	δ^{V1}	—
e^- NC 98-99	$\delta^{\mathcal{L}1}$	$\delta^{\mathcal{L}3}$	δ^{E1}	$\delta^{\theta2}$	δ^{h1}	δ^{N1}	δ^{B1}	—	—
e^- NC 98-99 <i>high y</i>	$\delta^{\mathcal{L}1}$	$\delta^{\mathcal{L}3}$	δ^{E1}	$\delta^{\theta2}$	δ^{h1}	δ^{N1}	—	—	δ^S1
e^- CC 98-99	$\delta^{\mathcal{L}1}$	$\delta^{\mathcal{L}3}$	—	—	δ^{h1}	δ^{N1}	δ^{B1}	δ^{V2}	—
e^+ NC 99-00	$\delta^{\mathcal{L}1}$	$\delta^{\mathcal{L}4}$	δ^{E1}	$\delta^{\theta2}$	δ^{h1}	δ^{N1}	δ^{B1}	—	δ^S1
e^+ CC 99-00	$\delta^{\mathcal{L}1}$	$\delta^{\mathcal{L}4}$	—	—	δ^{h1}	δ^{N1}	δ^{B1}	δ^{V2}	—
e^+ NC <i>high y</i>	$\delta^{\mathcal{L}5}$	$\delta^{\mathcal{L}6}, \delta^{\mathcal{L}7}$	δ^{E2}	$\delta^{\theta3}$	δ^{h2}	δ^{N2}	—	—	δ^S2
e^- NC <i>high y</i>	$\delta^{\mathcal{L}5}$	$\delta^{\mathcal{L}8}, \delta^{\mathcal{L}9}$	δ^{E2}	$\delta^{\theta3}$	δ^{h2}	δ^{N2}	—	—	δ^S2
e^+ NC <i>L</i>	$\delta^{\mathcal{L}5}$	$\delta^{\mathcal{L}6}$	δ^{E2}	$\delta^{\theta3}$	δ^{h2}	δ^{N2}	δ^{B1}	—	—
e^+ CC <i>L</i>	$\delta^{\mathcal{L}5}$	$\delta^{\mathcal{L}6}$	—	—	δ^{h2}	δ^{N3}	δ^{B1}	δ^{V3}	—
e^+ NC <i>R</i>	$\delta^{\mathcal{L}5}$	$\delta^{\mathcal{L}7}$	δ^{E2}	$\delta^{\theta3}$	δ^{h2}	δ^{N2}	δ^{B1}	—	—
e^+ CC <i>R</i>	$\delta^{\mathcal{L}5}$	$\delta^{\mathcal{L}7}$	—	—	δ^{h2}	δ^{N3}	δ^{B1}	δ^{V3}	—
e^- NC <i>L</i>	$\delta^{\mathcal{L}5}$	$\delta^{\mathcal{L}8}$	δ^{E2}	$\delta^{\theta3}$	δ^{h2}	δ^{N2}	δ^{B1}	—	—
e^- CC <i>L</i>	$\delta^{\mathcal{L}5}$	$\delta^{\mathcal{L}8}$	—	—	δ^{h2}	δ^{N3}	δ^{B1}	δ^{V3}	—
e^- NC <i>R</i>	$\delta^{\mathcal{L}5}$	$\delta^{\mathcal{L}9}$	δ^{E2}	$\delta^{\theta3}$	δ^{h2}	δ^{N2}	δ^{B1}	—	—
e^- CC <i>R</i>	$\delta^{\mathcal{L}5}$	$\delta^{\mathcal{L}9}$	—	—	δ^{h2}	δ^{N3}	δ^{B1}	δ^{V3}	—

correlation of H1 systematic error sources

$\delta^{\mathcal{L}1} \rightarrow 0.5\% \text{ BH theoretical error}$
HERA-I

$\delta^{\mathcal{L}5} \rightarrow 2.3\% \text{ Compton lumi error}$
HERA-II

$\delta^{\mathcal{L}6-9} \rightarrow 1.5\% \text{ Compton unc. error}$
HERA-II



Data Period	Global Normalisation	Per Period Normalisation	Total Normalisation
e^+ Combined low Q^2	0.993	—	0.993
e^+ Combined low E_p	0.993	—	0.993
HERA I e^+ 94-97	0.993	0.999	0.992
HERA I e^- 98-99	0.993	1.003	0.996
HERA I e^+ 99-00	0.993	1.005	0.998
HERA II $e^+ L$	1.029	0.991	1.020
HERA II $e^+ R$	1.029	1.013	1.042
HERA II $e^- L$	1.029	1.010	1.039
HERA II $e^- R$	1.029	1.014	1.043

normalisations from HIPDF 2012

Low Q^2 data shifted by -0.7%

HERA-I high Q^2 by -0.3%

HERA-II high Q^2 by +2 to +4%

All shifts are < 1.3 std.devs

HERAPDF1.0

Combine NC and CC HERA-I data from H1 & ZEUS

Complete MSbar NLO fit

NLO: standard parameterisation with 10 parameters

 $\alpha_s = 0.11176$ (fixed in fit)

desy-09-158

HERAPDF1.5

Include additional NC and CC HERA-II data

Complete MSbar NLO and NNLO fit

NLO: standard parameterisation with 10 parameters

HERAPDF1.5f

NNLO: extended fit with 14 parameters

$$xf(x, Q_0^2) = A \cdot x^B \cdot (1-x)^C \cdot (1+Dx+Ex^2)$$
H1-10-142 / ZEUS-prel-10-018

xg	xg	$xg(x) = A_g x^{B_g} (1-x)^{C_g},$
xu_v	$xU = xu + xc$	$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1+E_{u_v} x^2),$
xd_v	$xD = xd + xs$	$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}},$
$x\bar{U}$	$x\bar{U} = x\bar{u} + x\bar{c}$	$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}},$
$x\bar{D}$	$x\bar{D} = x\bar{d} + x\bar{s}$	$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.$

$$x\bar{s} = f_s x\bar{D} \text{ strange sea is a fixed fraction } f_s \text{ of } \bar{D} \text{ at } Q_0^2$$

Apply momentum/counting sum rules:

$$\int_0^1 dx \cdot (xu_v + xd_v + x\bar{U} + x\bar{D} + xg) = 1$$

$$\int_0^1 dx \cdot u_v = 2 \quad \int_0^1 dx \cdot d_v = 1$$

Parameter constraints:

$$B_{uv} = B_{dv}$$

$$B_{Ubar} = B_{Dbar}$$

$$\text{sea} = 2 \times (\text{Ubar} + \text{Dbar})$$

$$\text{Ubar} = \text{Dbar at } x=0$$

$$Q_0^2 = 1.9 \text{ GeV}^2 \text{ (below } m_c)$$

$$Q^2 > 3.5 \text{ GeV}^2$$

$$2 \times 10^{-4} < x < 0.65$$

Fits performed using RT-VFNS



HERAPDF1.0 central values:

	<i>A</i>	<i>B</i>	<i>C</i>	<i>E</i>
xg	6.8	0.22	9.0	
xu_v	3.7	0.67	4.7	9.7
xd_v	2.2	0.67	4.3	
$x\bar{U}$	0.113	-0.165	2.6	
$x\bar{D}$	0.163	-0.165	2.4	

$$\chi^2/\text{ndf} = 574/582$$

Experimental systematic sources of uncertainty allowed to float in fit

Include model assumptions into uncertainty:

$$f_s, m_c, m_b, Q^2_0, Q^2_{min}$$

Variation	Standard Value	Lower Limit	Upper Limit
f_s	0.31	0.23	0.38
m_c [GeV]	1.4	1.35 ^(a)	1.65
m_b [GeV]	4.75	4.3	5.0
Q^2_{min} [GeV ²]	3.5	2.5	5.0
Q^2_0 [GeV ²]	1.9	1.5 ^(b)	2.5 ^(c,d)

$$^{(a)}Q^2_0 = 1.8$$

$$^{(b)}f_s = 0.29$$

$$^{(c)}m_c = 1.6$$

$$^{(d)}f_s = 0.34$$

Excellent consistency of input data allow standard statistical error definition:

$$\Delta\chi^2 = \mathbf{I}$$

Exclusive jet data required for free α_s fit
See talk of Krzysztof Nowak

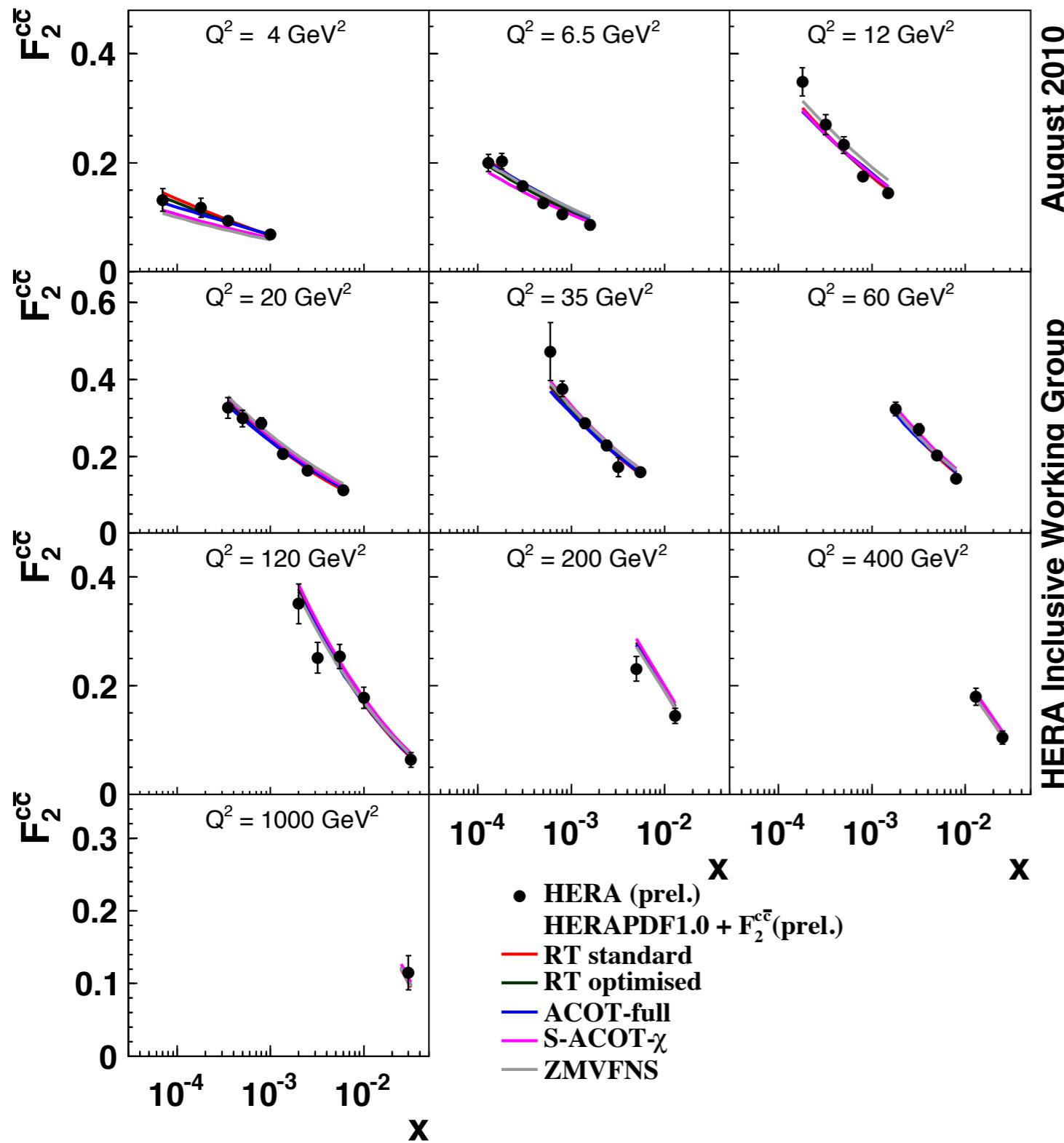
In 14 parameter fit:

release $B_{uv} = B_{dv}$ constraint
allow more flexible gluon

$$xg(x, Q_0^2) = A \cdot x^B \cdot (1-x)^C - A' \cdot x^{B'} \cdot (1-x)^{25}$$

allows for valence-like or negative gluon at Q_0^2

Charm Content of the Proton



The inclusive charm content of proton can be measured in several methods:
 D* decays , impact parameter significance...
 Combination yields $\sim 5\text{-}10\%$ precision

Data cover wide phase space region including charm threshold region

Theory predictions have small spread
 \Rightarrow use optimised m_c parameter

Spread of LHC Z/W production predictions is reduced $\sim 4.5\% \rightarrow \sim 0.7\%$
 when using optimal value of m_c



ZEUS inclusive jets	39 pb^{-1}	$Q^2 > 125$	Nucl. Phys. B765 (2007) 1-30
ZEUS inclusive jets	82 pb^{-1}	$Q^2 > 125$	Phys. Lett. B649 (2007) 12
H1 inclusive jets	395 pb^{-1}	$150 < Q^2 < 15000$	EPJ C65 (2010) 363-383
H1 inclusive jets	44 pb^{-1}	$5 < Q^2 < 100$	EPJ C67 (2010) 1-24

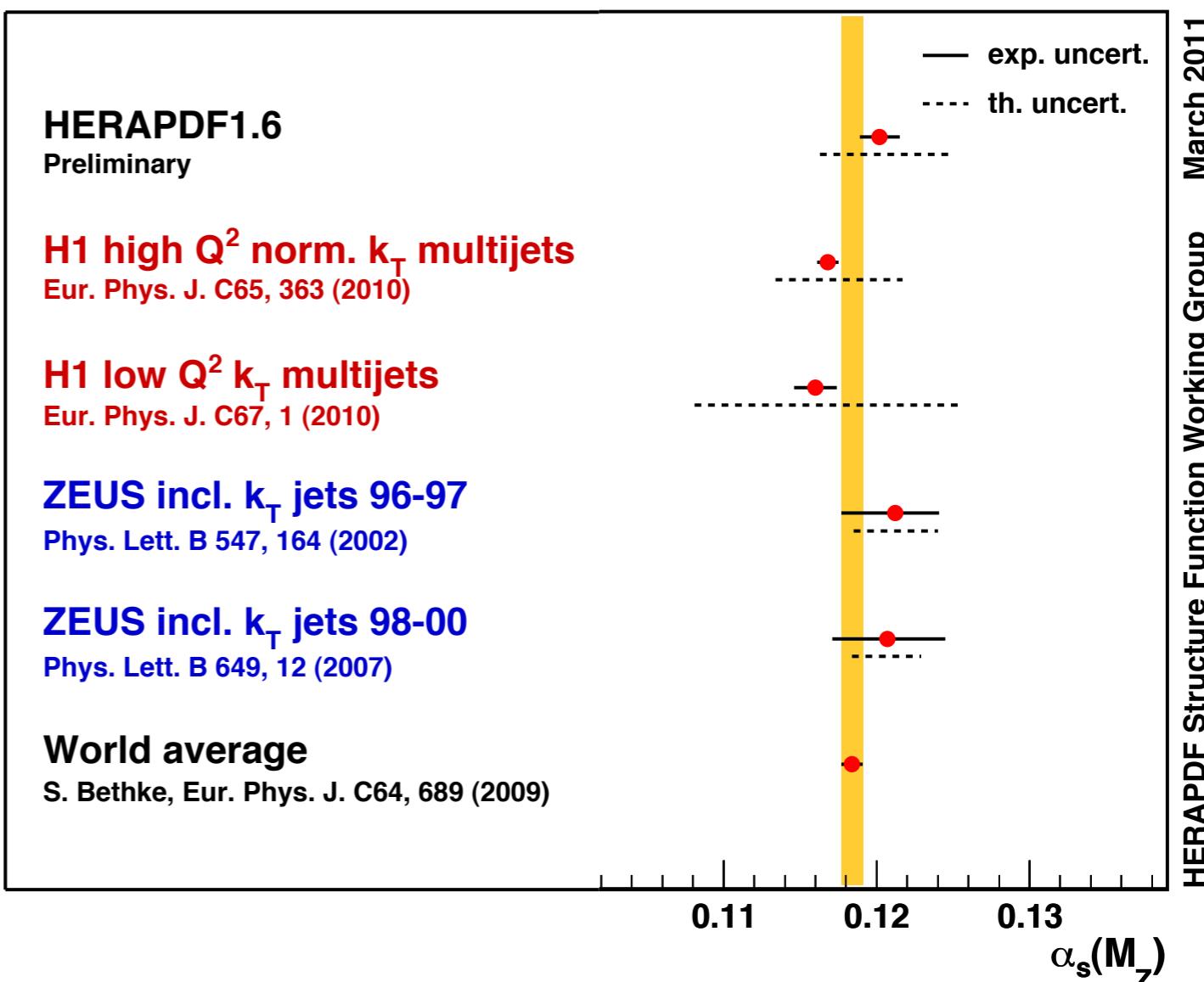
Jet data bring significant sensitivity to α_s
Disentangles correlation between $xg(x, Q^2)$ and α_s

HERAPDF1.6 : Simultaneous NLO QCD fit to
 - combined NC inclusive cross section data
 - combined CC inclusive cross sections data
 - normalised H1/ZEUS inclusive jet data

$$\begin{aligned}\alpha_s(M_Z) = 0.1202 &\pm 0.0013 \text{ (exp)} \\ &\pm 0.0007 \text{ (model)} \\ &\pm 0.0012 \text{ (hadronisation)} \\ &+0.0045 \\ &-0.0036 \text{ (scales)}\end{aligned}$$

Only combined PDF / α_s fit on the market

H1 and ZEUS (prel.)



High Q^2 NC Multi-jets

H1 prelim-II-032

New H1 measurement of inclusive, dijet and trijet rates

First measurement of double diff'l trijet cross section

Significantly reduced systematic errors

1% hadronic scale uncertainty

For now - unnormalised cross sections...

Jets in Breit frame: $5 < P_T < 50 \text{ GeV}$
 $M_{12} > 16 \text{ GeV}$

Greater sensitivity to α_s with more jets

High Q^2 and large jet $P_T \Rightarrow$ multi-scale QCD problem

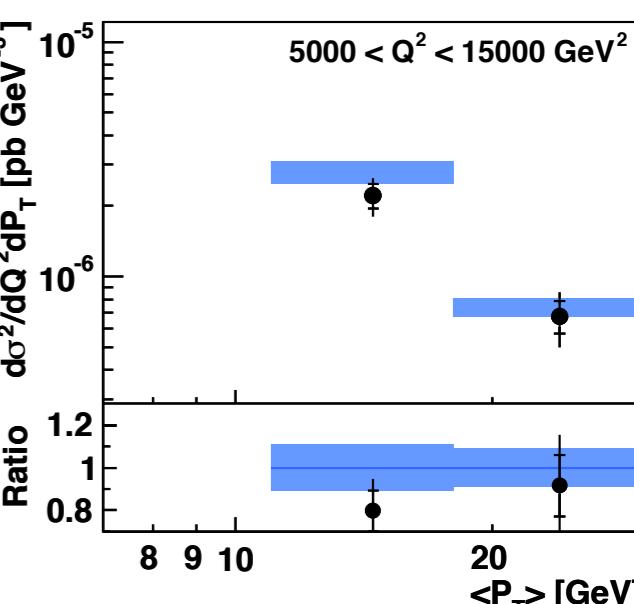
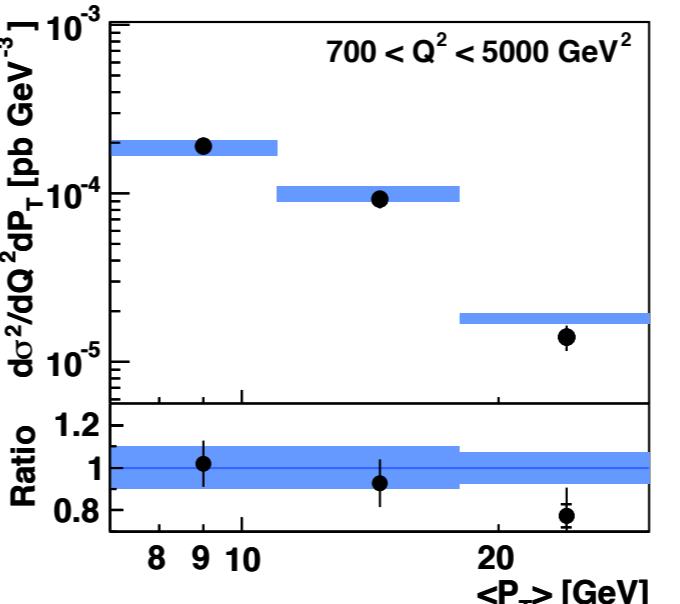
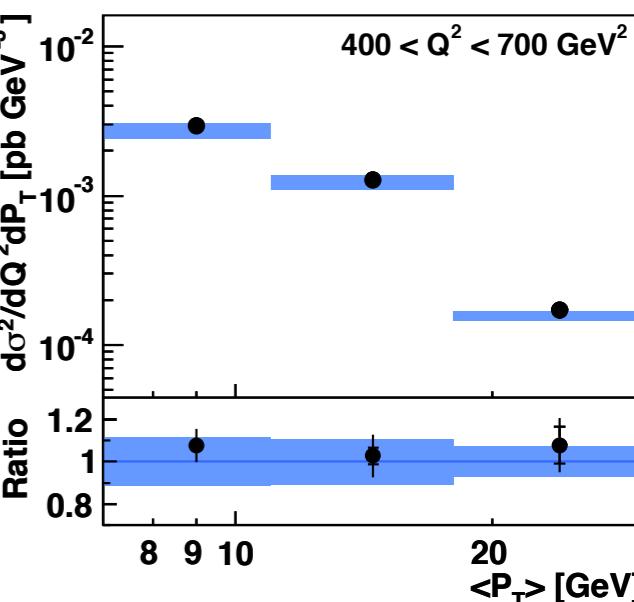
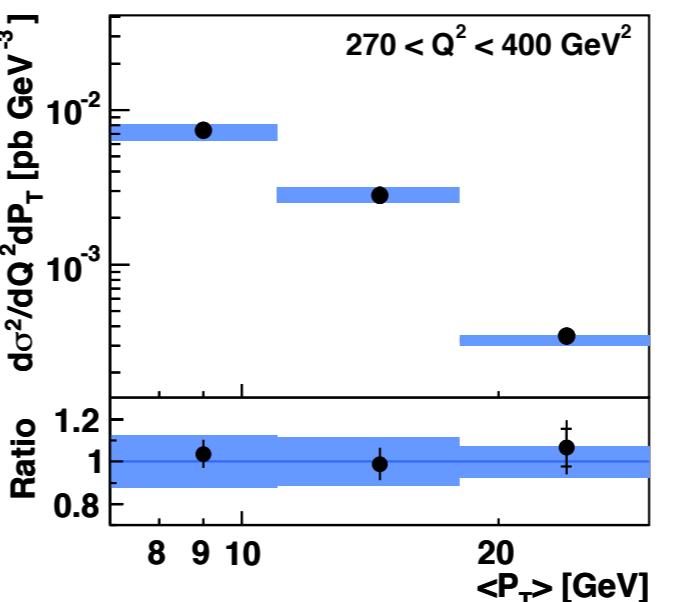
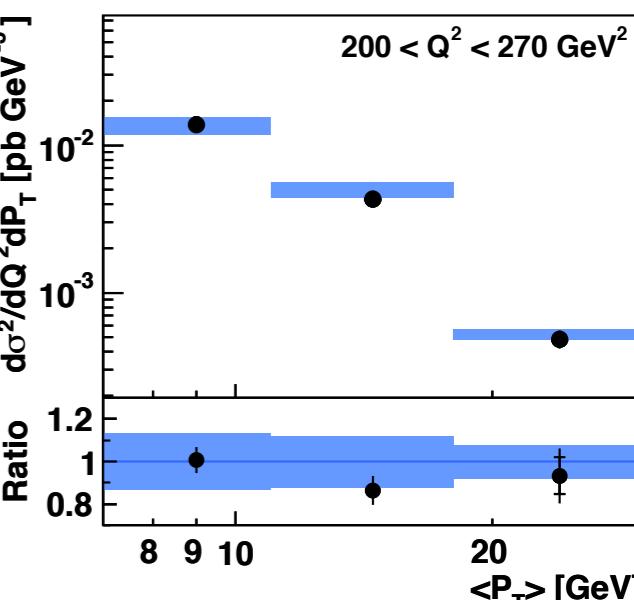
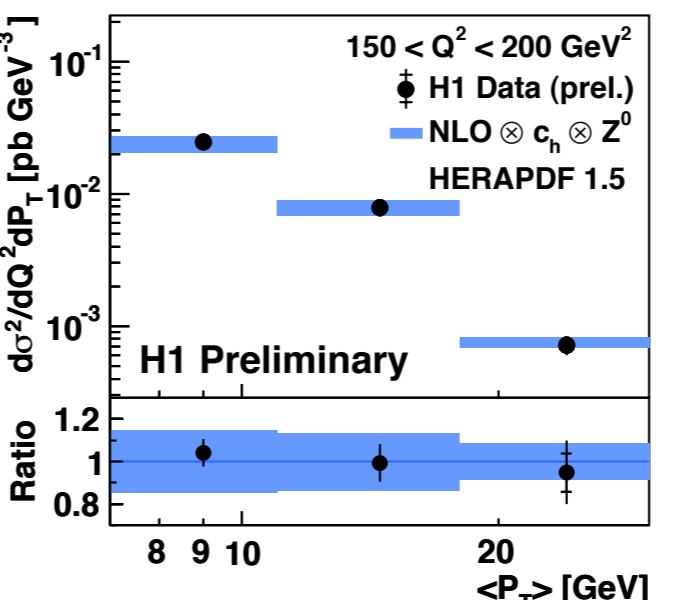
Good description in NLO

(worse for di-jets at low $\langle P_T \rangle$...)

$$\text{NLO calculation } \mu_R = \mu_F = \sqrt{\frac{1}{2}(Q^2 + P_T^2)}$$

scales varied by factors of 2 for uncertainty

Trijet Cross Section



High Q^2 NC Multi-jets

H1 prelim-II-032

Di-jet rates in reasonable agreement
 ~10% discrepancy at low $\langle P_T \rangle$
 Data want smaller α_s or smaller xg ?

Extract α_s independently for each jet data set in NLO
 PDF uncertainty from CT10 error propagation

Inclusive jets:

$$\alpha_s(M_Z) = 0.1190 \pm 0.0021 \text{ (exp.)} \pm 0.0020 \text{ (pdf)}^{+0.0050}_{-0.0056} \text{ (th.)}$$

Dijets:

$$\alpha_s(M_Z) = 0.1146 \pm 0.0022 \text{ (exp.)} \pm 0.0021 \text{ (pdf)}^{+0.0044}_{-0.0045} \text{ (th.)}$$

Trijets:

$$\alpha_s(M_Z) = 0.1196 \pm 0.0016 \text{ (exp.)} \pm 0.0010 \text{ (pdf)}^{+0.0055}_{-0.0039} \text{ (th.)}$$

Achieved ~1% experimental precision on α_s
 Theoretical uncertainty (scales) dominate ~4%
 PDF uncertainty ~1%

To come:

Use of normalised cross sections
 cancellation of systematic uncertainties
 → reduced error for α_s

Dijet Cross Section

