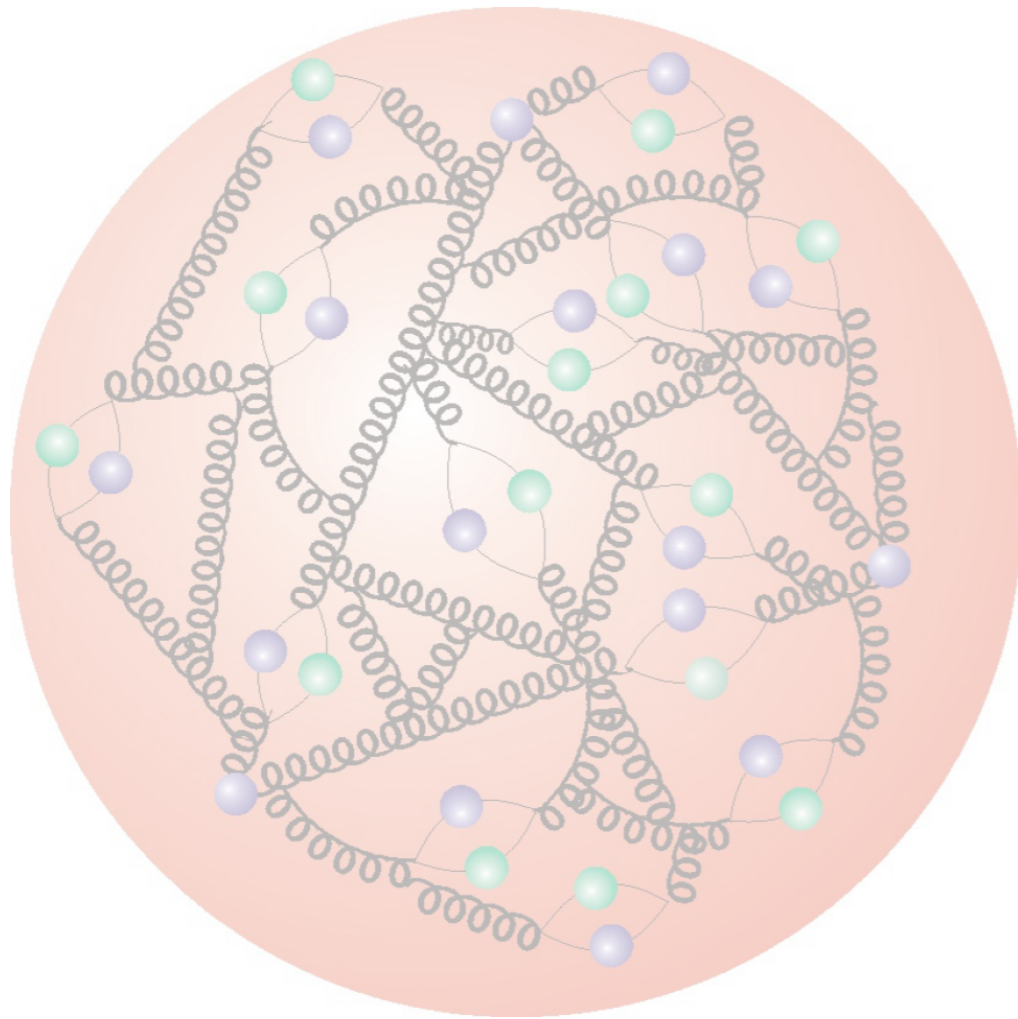
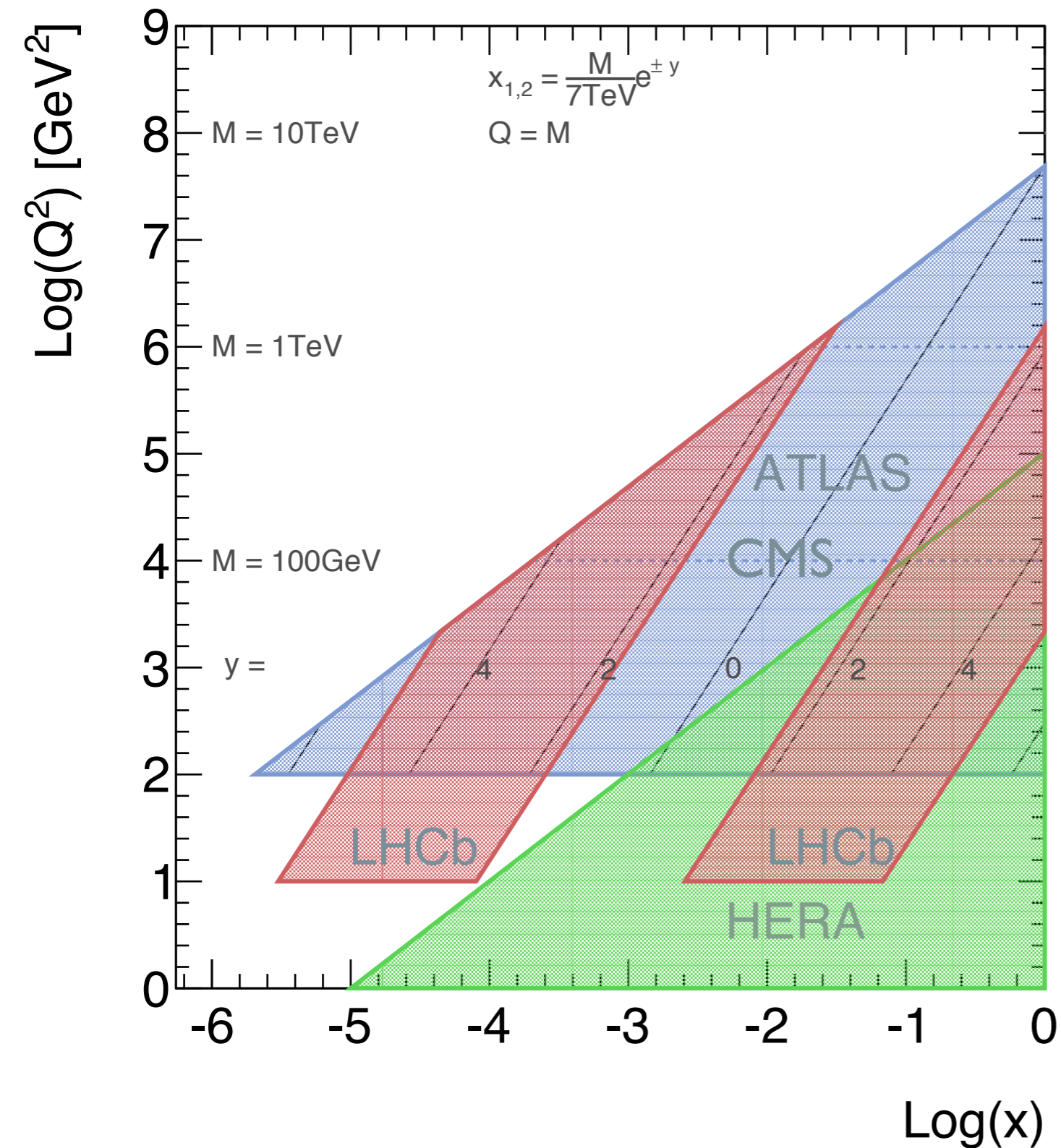


Precision QCD in DIS at HERA



- Introduction
- HERA-II Updates
- H1 NC/CC $e^\pm p$
- H1 NC High y $e^\pm p$
- ZEUS NC $e^+ p$
- HERAPDF Plans





LHC: largest mass states at large x

For central production $x=x_1=x_2$

$$M=x\sqrt{s}$$

i.e. $M > 1\text{TeV}$ probes $x > 0.1$

Searches for high mass states require precision knowledge at high x

Z' / quantum gravity / susy searches...

DGLAP evolution allows predictions to be made

High x predictions rely on

- data (DIS / fixed target)
- sum rules
- behaviour of PDFs as $x \rightarrow 1$

$$\frac{d\sigma_{NC}^{\pm}}{dx dQ^2} = \frac{2\pi\alpha^2}{x} \left[\frac{1}{Q^2} \right]^2 \left[Y_+ \tilde{F}_2 \mp Y_- x \tilde{F}_3 - y^2 \tilde{F}_L \right]$$

$$\frac{d\sigma_{CC}^{\pm}}{dx dQ^2} = \frac{G_F^2}{4\pi x} \left[\frac{M_W^2}{M_W^2 + Q^2} \right]^2 \left[Y_+ \tilde{W}_2^{\pm} \mp Y_- x \tilde{W}_3^{\pm} - y^2 \tilde{W}_L^{\pm} \right]$$

$$Y_{\pm} = 1 \pm (1-y)^2$$

$$\tilde{F}_2 \propto \sum (xq_i + x\bar{q}_i)$$

Dominant contribution

$$x\tilde{F}_3 \propto \sum (xq_i - x\bar{q}_i)$$

Only sensitive at high $Q^2 \sim M_Z^2$

$$\tilde{F}_L \propto \alpha_s \cdot xg(x, Q^2)$$

Only sensitive at low Q^2 and high y

The NC reduced cross section defined as:

$$\tilde{\sigma}_{NC}^{\pm} = \frac{Q^2 x}{2\alpha\pi^2} \frac{1}{Y_+} \frac{d^2\sigma^{\pm}}{dx dQ^2}$$

$$\tilde{\sigma}_{NC}^{\pm} \sim \tilde{F}_2 \mp \frac{Y_-}{Y_+} x\tilde{F}_3$$

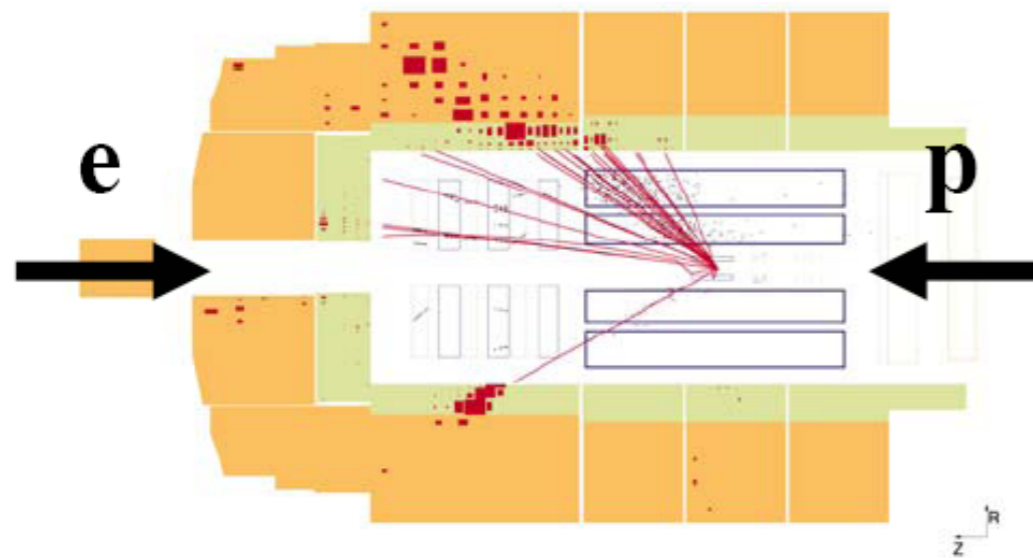
The CC reduced cross section defined as:

$$\sigma_{CC}^{\pm} = \frac{2\pi x}{G_F^2} \left[\frac{M_W^2 + Q^2}{M_W^2} \right]^2 \frac{d\sigma_{CC}^{\pm}}{dx dQ^2}$$

$$\frac{d\sigma_{CC}^{\pm}}{dx dQ^2} = \frac{1}{2} \left[Y_+ W_2^{\pm} \mp Y_- x W_3^{\pm} - y^2 W_L^{\pm} \right]$$

similarly for pure weak CC analogues:

$$W_2^{\pm}, xW_3^{\pm} \text{ and } W_L^{\pm}$$



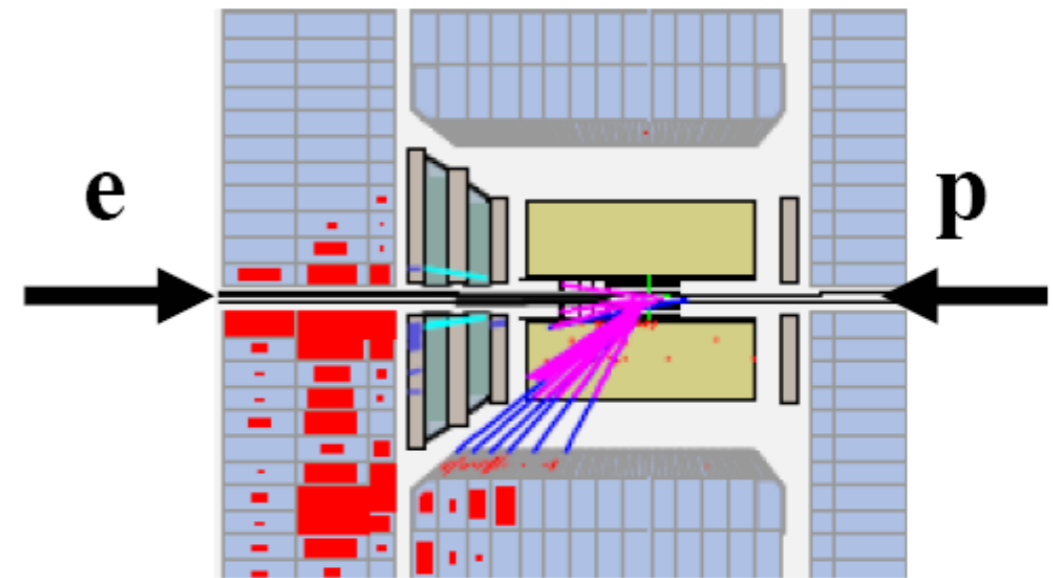
Neutral current event selection:

High P_T isolated scattered lepton
 Suppress huge photo-production background by imposing longitudinal energy-momentum conservation

Kinematics may be reconstructed in many ways:
 energy/angle of hadrons & scattered lepton provides excellent tools for sys cross checks

Removal of scattered lepton provides a high stats “pseudo-charged current sample”
 Excellent tool to cross check CC analysis

Final selection: $\sim 10^5$ events per sample at high Q^2
 $\sim 10^7$ events for $10 < Q^2 < 100 \text{ GeV}^2$



Charged current event selection:

Large missing transverse momentum (neutrino)
 Suppress huge photo-production background
 Topological finders to remove cosmic muons
 Kinematics reconstructed from hadrons
 Final selection: $\sim 10^3$ events per sample

HERA-I operation 1993-2000

$E_e = 27.6 \text{ GeV}$

$E_p = 820 / 920 \text{ GeV}$

$\int \mathcal{L} \sim 110 \text{ pb}^{-1}$ per experiment

HERA-II operation 2003-2007

$E_e = 27.6 \text{ GeV}$

$E_p = 920 \text{ GeV}$

$\int \mathcal{L} \sim 330 \text{ pb}^{-1}$ per experiment

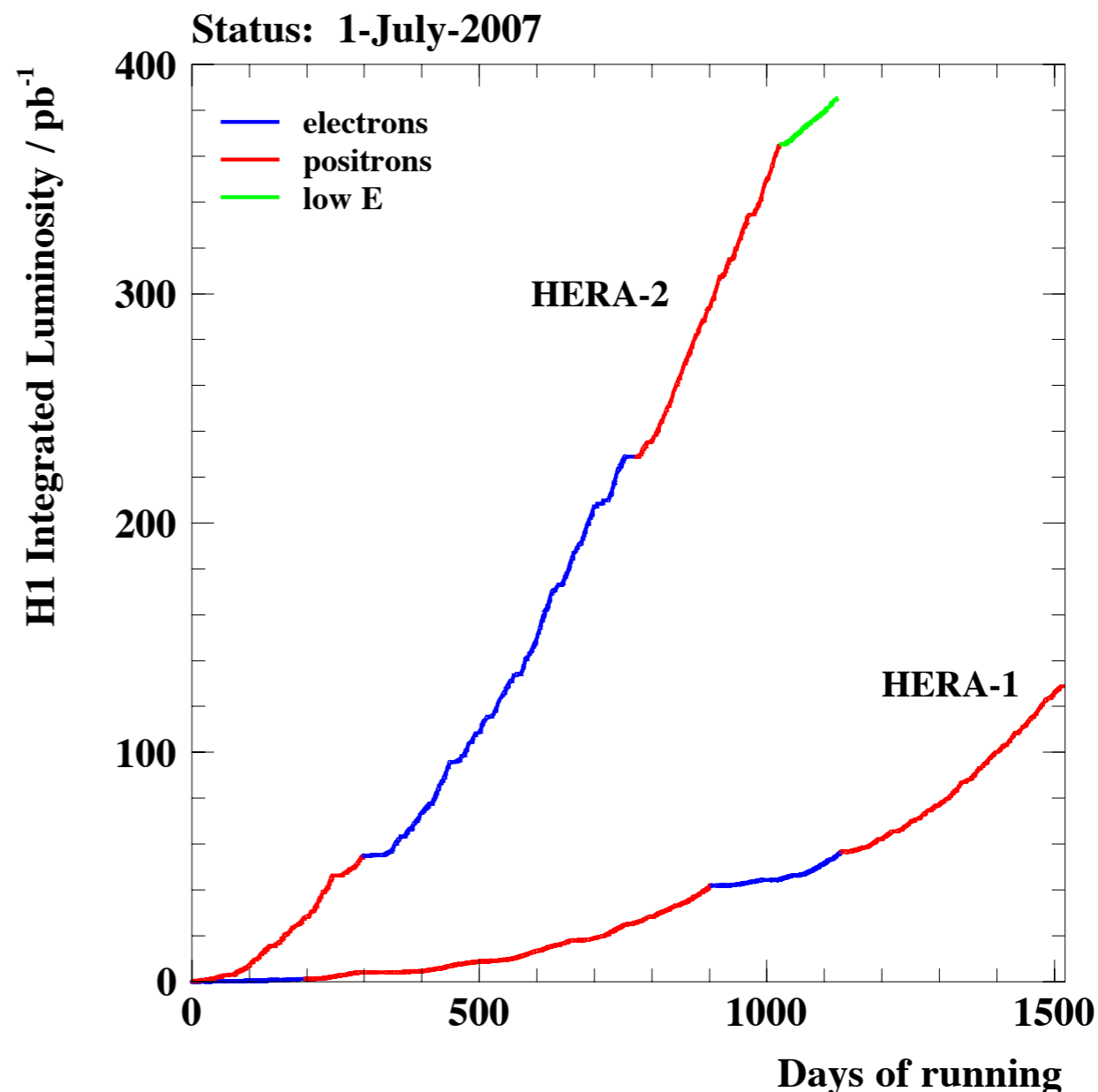
Longitudinally polarised leptons

Low Energy Run 2007

$E_e = 27.6 \text{ GeV}$

$E_p = 575 \text{ \& } 460 \text{ GeV}$

Dedicated F_L measurement



breakdown of HERA-II data samples

	R	L
e^-p	$\mathcal{L} = 47.3 \text{ pb}^{-1}$ $P_e = (+36.0 \pm 1.0)\%$	$\mathcal{L} = 104.4 \text{ pb}^{-1}$ $P_e = (-25.8 \pm 0.7)\%$
e^+p	$\mathcal{L} = 101.3 \text{ pb}^{-1}$ $P_e = (+32.5 \pm 0.7)\%$	$\mathcal{L} = 80.7 \text{ pb}^{-1}$ $P_e = (-37.0 \pm 0.7)\%$



Summary of HERA-I datasets Combined in HERAPDF1.0

Available since 2009

Data Set		x Range		Q^2 Range GeV ²		\mathcal{L} pb ⁻¹	e^+/e^-	\sqrt{s} GeV
H1 svx-mb	95-00	5×10^{-6}	0.02	0.2	12	2.1	$e^+ p$	301-319
H1 low Q^2	96-00	2×10^{-4}	0.1	12	150	22	$e^+ p$	301-319
H1 NC	94-97	0.0032	0.65	150	30000	35.6	$e^+ p$	301
H1 CC	94-97	0.013	0.40	300	15000	35.6	$e^+ p$	301
H1 NC	98-99	0.0032	0.65	150	30000	16.4	$e^- p$	319
H1 CC	98-99	0.013	0.40	300	15000	16.4	$e^- p$	319
H1 NC HY	98-99	0.0013	0.01	100	800	16.4	$e^- p$	319
H1 NC	99-00	0.0013	0.65	100	30000	65.2	$e^+ p$	319
H1 CC	99-00	0.013	0.40	300	15000	65.2	$e^+ p$	319
ZEUS BPC	95	2×10^{-6}	6×10^{-5}	0.11	0.65	1.65	$e^+ p$	301
ZEUS BPT	97	6×10^{-7}	0.001	0.045	0.65	3.9	$e^+ p$	301
ZEUS SVX	95	1.2×10^{-5}	0.0019	0.6	17	0.2	$e^+ p$	301
ZEUS NC	96-97	6×10^{-5}	0.65	2.7	30000	30.0	$e^+ p$	301
ZEUS CC	94-97	0.015	0.42	280	17000	47.7	$e^+ p$	301
ZEUS NC	98-99	0.005	0.65	200	30000	15.9	$e^- p$	319
ZEUS CC	98-99	0.015	0.42	280	30000	16.4	$e^- p$	319
ZEUS NC	99-00	0.005	0.65	200	30000	63.2	$e^+ p$	319
ZEUS CC	99-00	0.008	0.42	280	17000	60.9	$e^+ p$	319

High Q^2 NC and CC data limited to
100 pb⁻¹ $e^+ p$
16 pb⁻¹ $e^- p$



Up till now HERA-II datasets only partially published

ZEUS CC e^-p	175 pb^{-1}	EPJ C 61 (2009) 223-235
ZEUS CC e^+p	132 pb^{-1}	EPJ C 70 (2010) 945-963
ZEUS NC e^-p	170 pb^{-1}	EPJ C 62 (2009) 625-658
ZEUS NC e^+p	135 pb^{-1}	ZEUS-prel-11-003
HI CC e^-p	149 pb^{-1}	HIprelim-09-043
HI CC e^+p	180 pb^{-1}	HIprelim-09-043
HI NC e^-p	149 pb^{-1}	HIprelim-09-042
HI NC e^+p	180 pb^{-1}	HIprelim-09-042



HERA-II datasets
Combined in HERAPDF1.5
(except ZEUS NC e^+p)



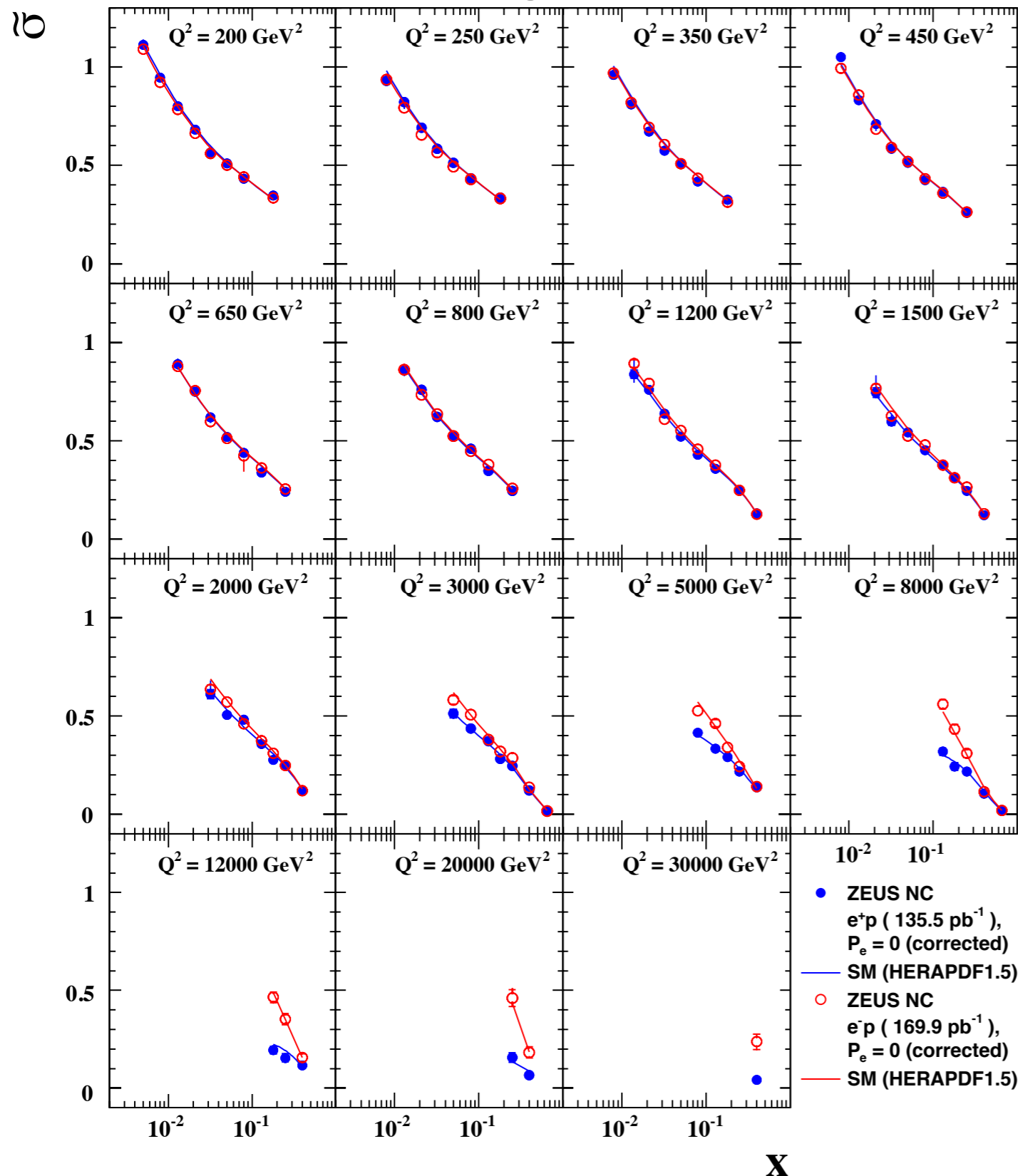
ZEUS CC e^-p	175 pb^{-1}	EPJ C 61 (2009) 223-235
ZEUS CC e^+p	132 pb^{-1}	EPJ C 70 (2010) 945-963
ZEUS NC e^-p	170 pb^{-1}	EPJ C 62 (2009) 625-658
ZEUS NC e^+p	135 pb^{-1}	arXiv:1208.6138
HI CC e^-p	149 pb^{-1}	arXiv:1206.7007
HI CC e^+p	180 pb^{-1}	
HI NC e^-p	149 pb^{-1}	
HI NC e^+p	180 pb^{-1}	

Complete the analyses of HERA high Q^2 inclusive structure function data

New published data increase $\int \mathcal{L}$ by
 ~ factor 3 for e^+p
 ~ factor 10 for e^-p
 much improved systematic uncertainties



ZEUS



High Q^2 is the EW physics regime:
 Z^0 contribution enhances as Q^2 increases

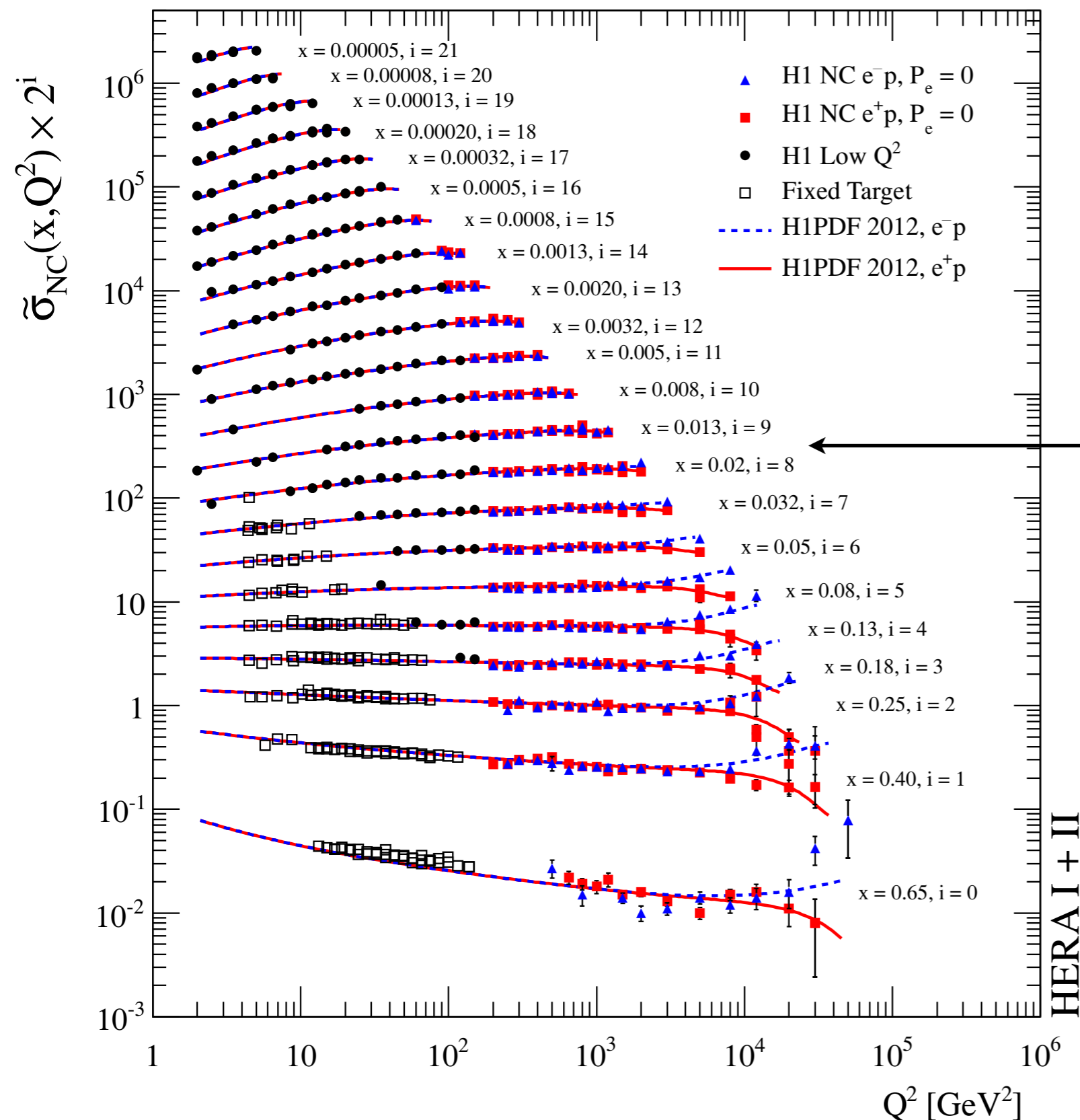
Final measurement of ZEUS NC e^+p data

Shown here for $P=0$

Polarised measurements also available

Compared to published NC e^-p data

H1 Collaboration



H1 precision 1.5% for $Q^2 < 500 \text{ GeV}^2$
 \Rightarrow factor 2 reduction in error wrt HERA-I

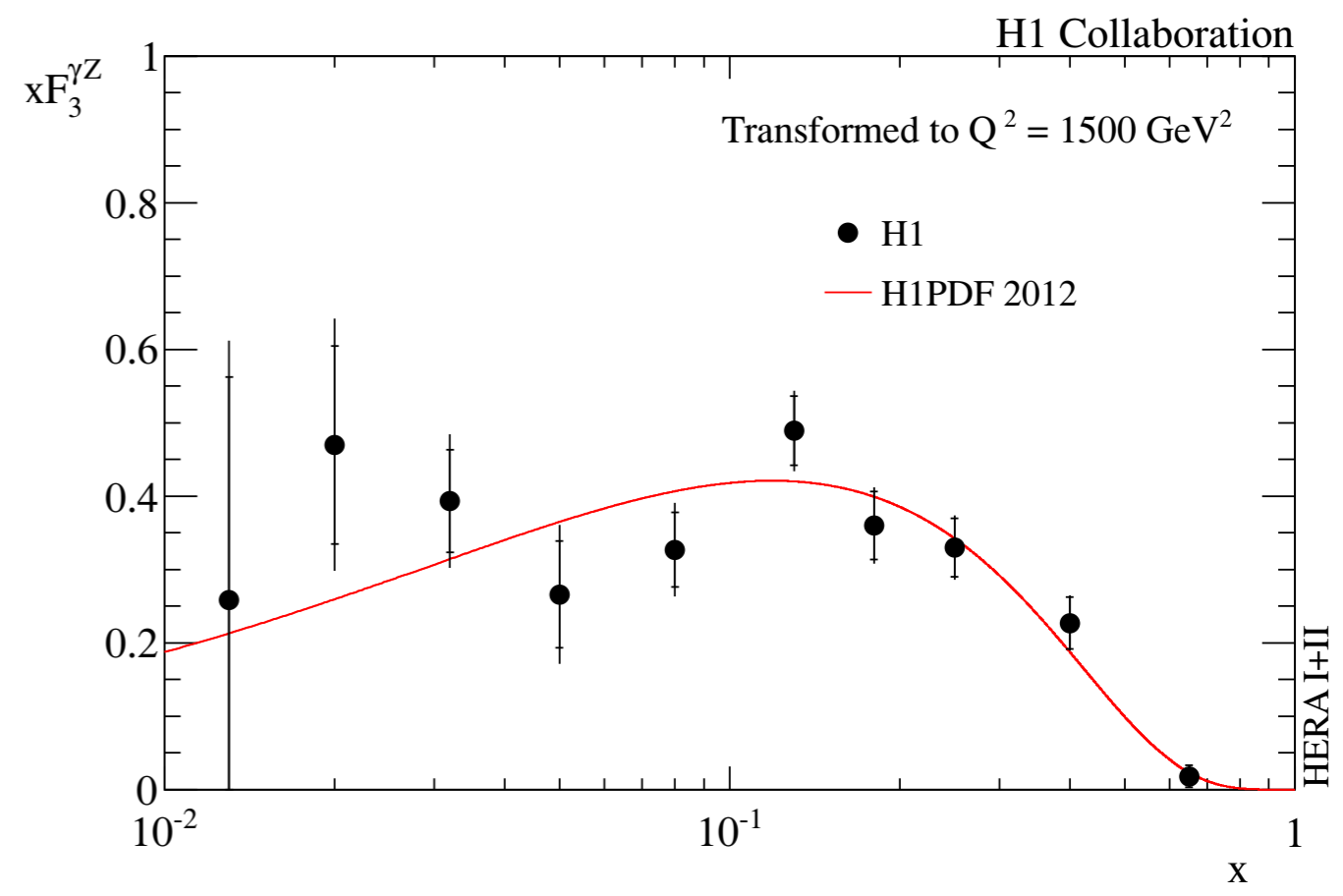
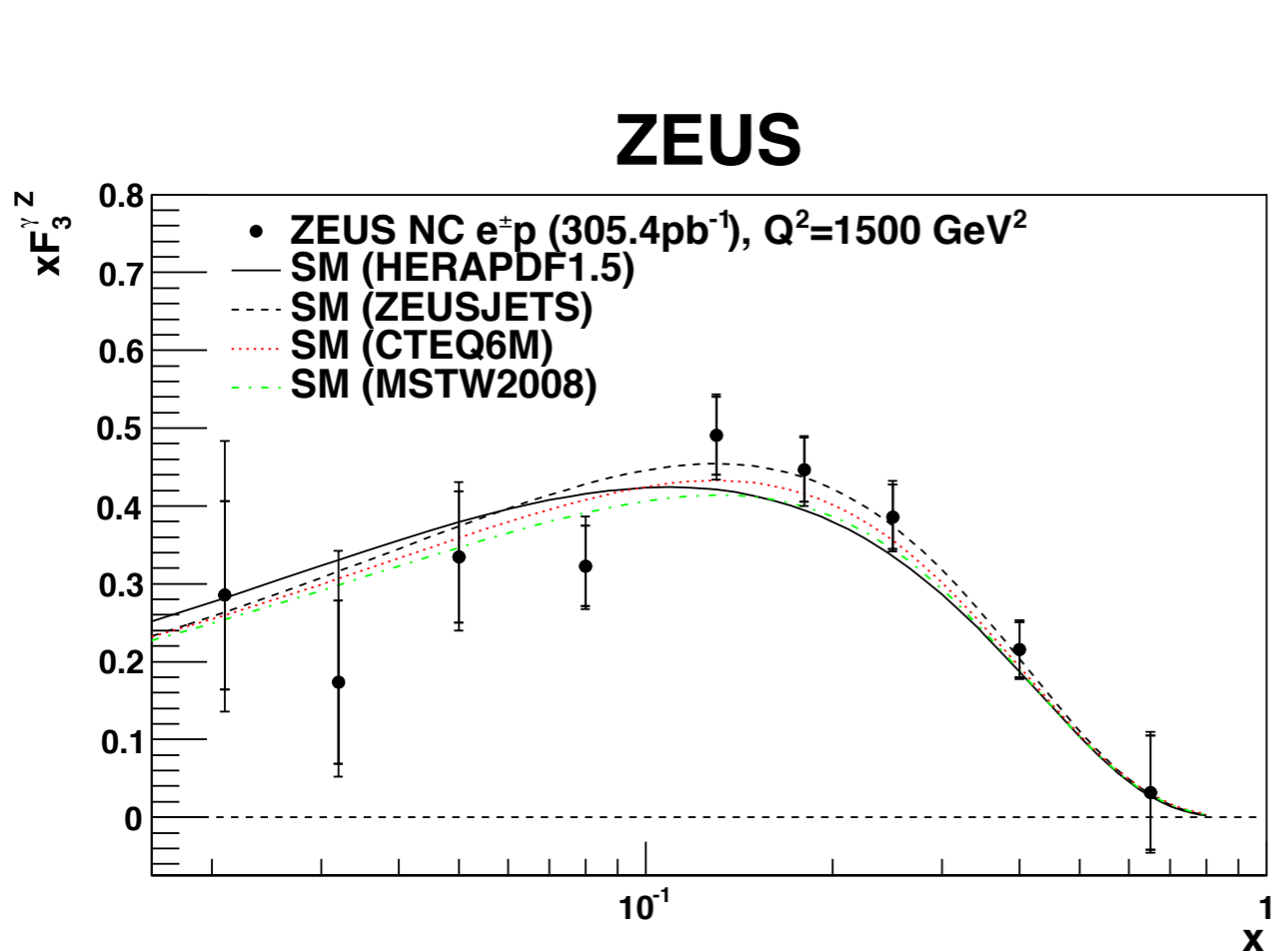
Statistics limited at higher Q^2 and high x

Extended reach at high x compared to H1 preliminary data

This x region is the 'sweet spot'
 High precision with long Q^2 lever arm
 x -range relevant for Higgs production

Combination of high Q^2 data
 HERA-I and HERA-II

Larger HERA-II luminosity
 \rightarrow improved precision at high x / Q^2



At high Q^2 xF_3 arises due to Z^0 effects
 enhanced e^- cross section wrt e^+
 Difference is xF_3
 Sensitive to valence PDFs

$$x\tilde{F}_3 = \frac{Y_+}{2Y_-} (\tilde{\sigma}_{NC}^- - \tilde{\sigma}_{NC}^+) \approx a_e \chi_Z xF_3^{\gamma Z}$$

$$x\tilde{F}_3 \propto \sum (xq_i - x\bar{q}_i)$$

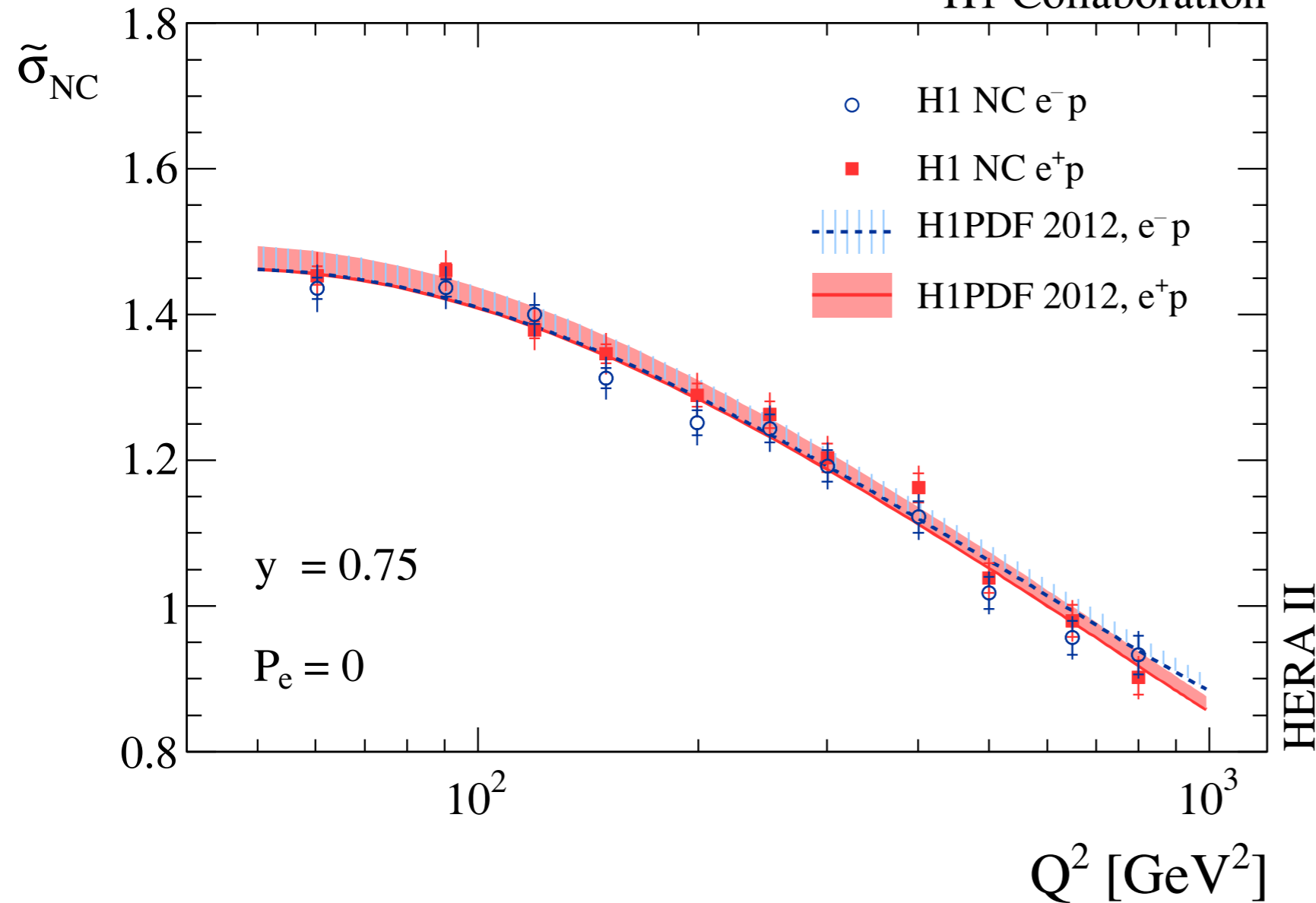
H1 measure integral of $xF_3^{\gamma Z}$ - validate sumrule:

$$\int_{0.016}^{0.725} dx F_3^{\gamma Z}(x, Q^2 = 1500 \text{ GeV}^2) = 1.22 \pm 0.09(\text{stat}) \pm 0.07(\text{syst})$$

NLO integral predicted to be $5/3 + \mathcal{O}(\alpha_s/\pi) = 1.16$



H1 Collaboration



Measurement extension to high y at high Q^2

Sensitive to F_L and xg

Difficult measurement:

- low scattered electron energy $E_e' > 5$ GeV
- large photoproduction background

HERA II

Total uncertainty reduced by factor 2:

HERA-I ~4%

HERA-II ~2%

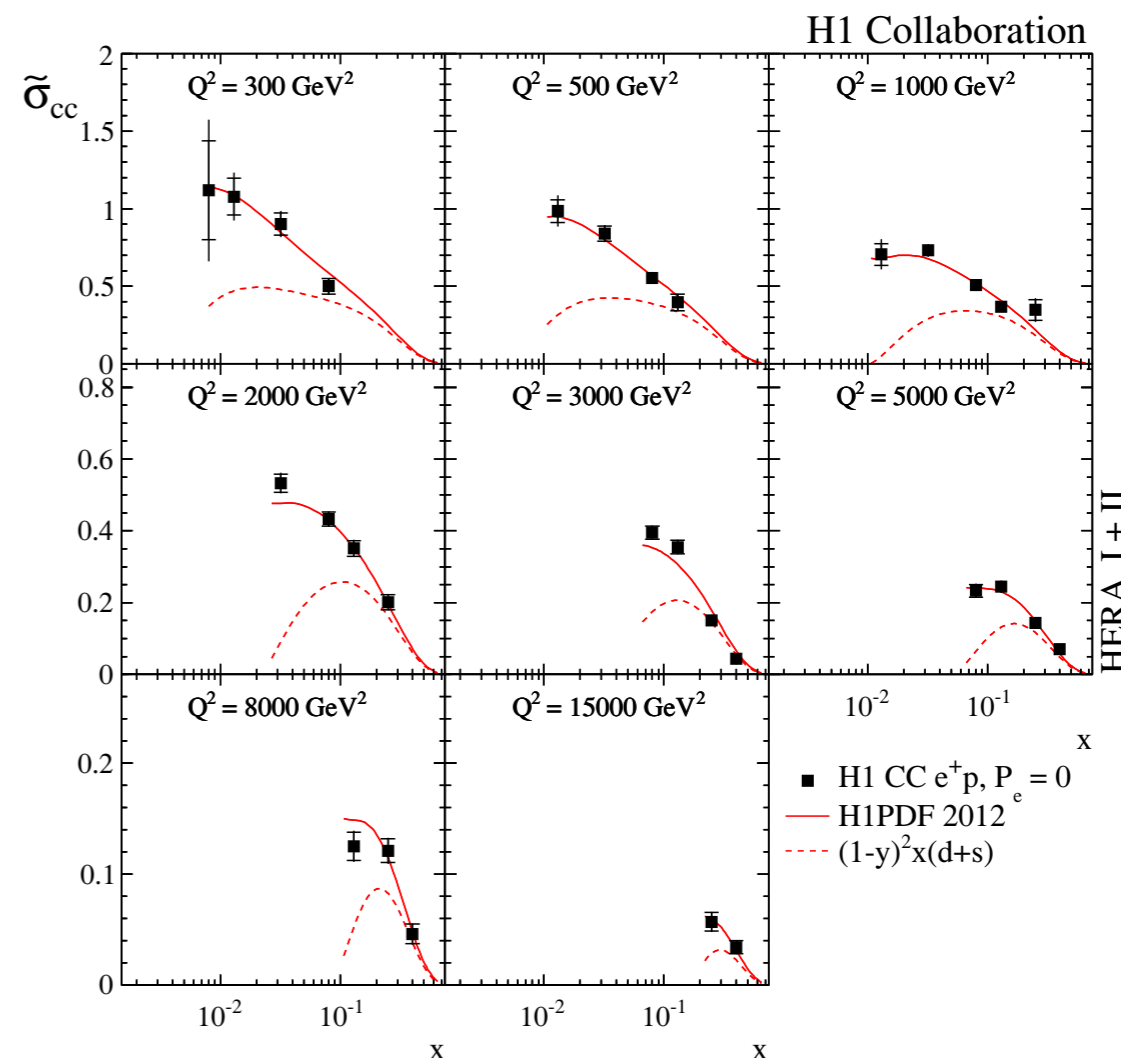
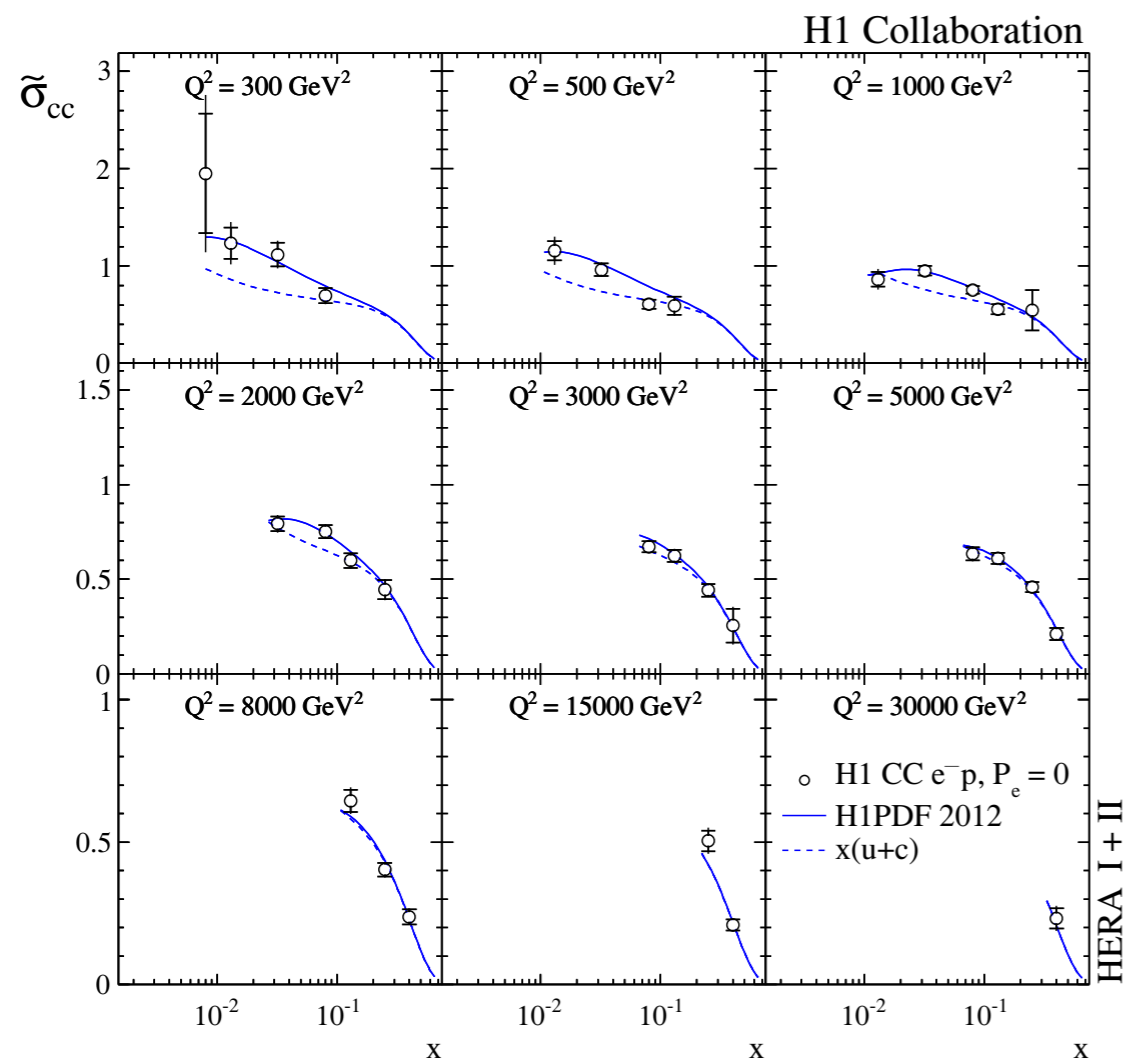


Electron scattering

$$\frac{d^2\sigma_{CC}^-}{dx dQ^2} = \frac{G_F^2}{2\pi} \left(\frac{M_W^2}{M_W^2 + Q^2} \right)^2 \left[(u+c) + (1-y)^2(\bar{d} + \bar{s}) \right]$$

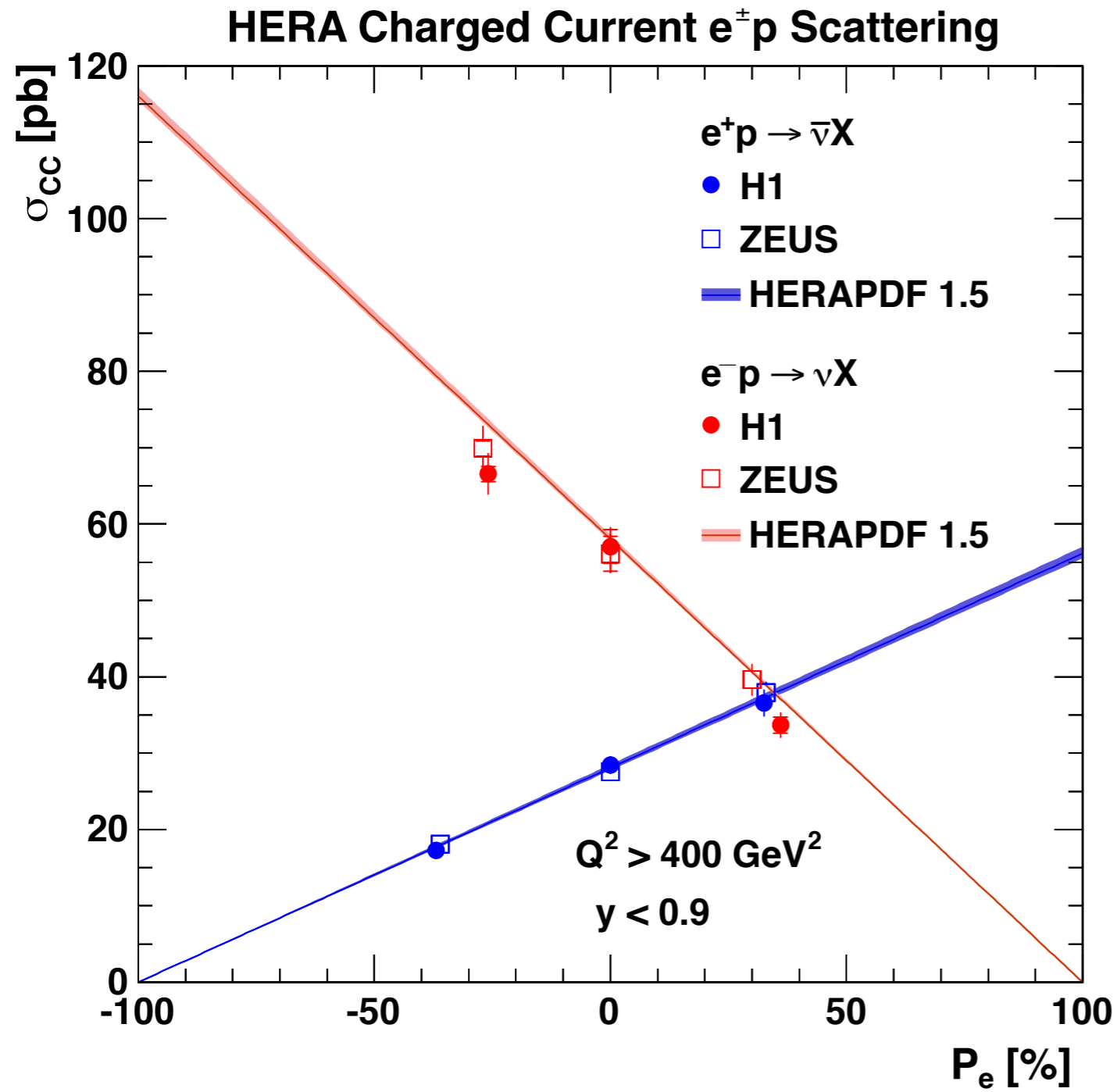
Positron scattering

$$\frac{d^2\sigma_{CC}^+}{dx dQ^2} = \frac{G_F^2}{2\pi} \left(\frac{M_W^2}{M_W^2 + Q^2} \right)^2 \left[(\bar{u} + \bar{c}) + (1-y)^2(d+s) \right]$$



H1 combination of high Q^2 CC data (HERA-I+II)
 Improvement of total uncertainty
 Dominated by statistical errors
 Provide important flavour decomposition information

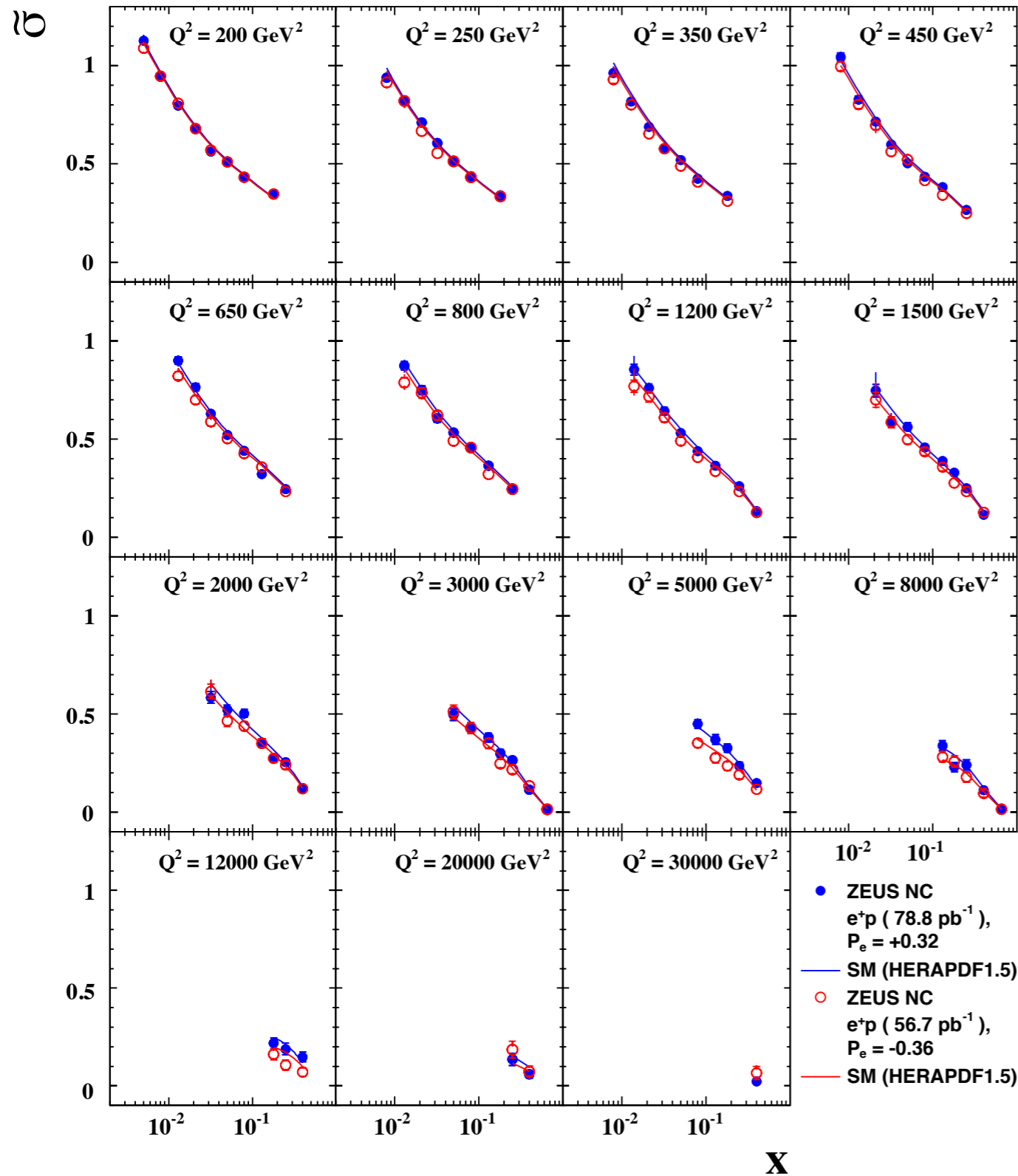
CC e^+ data provide strong d_v constraint at high x
 Precision limited by statistics: typically 5-10%
 HERA-I precision of 10-15% for e^+
 Large gain to come after combination with ZEUS



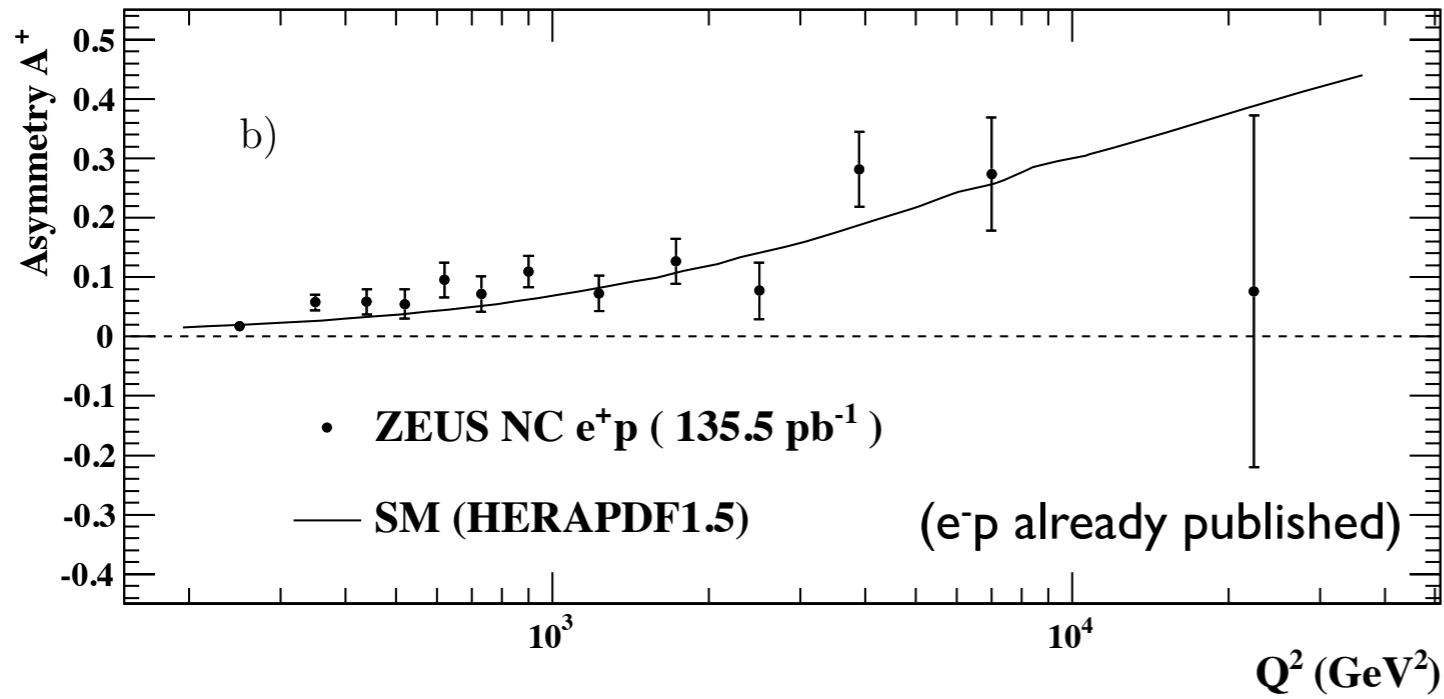
Polarisation dependence of CC cross section now final from H1 and ZEUS



ZEUS



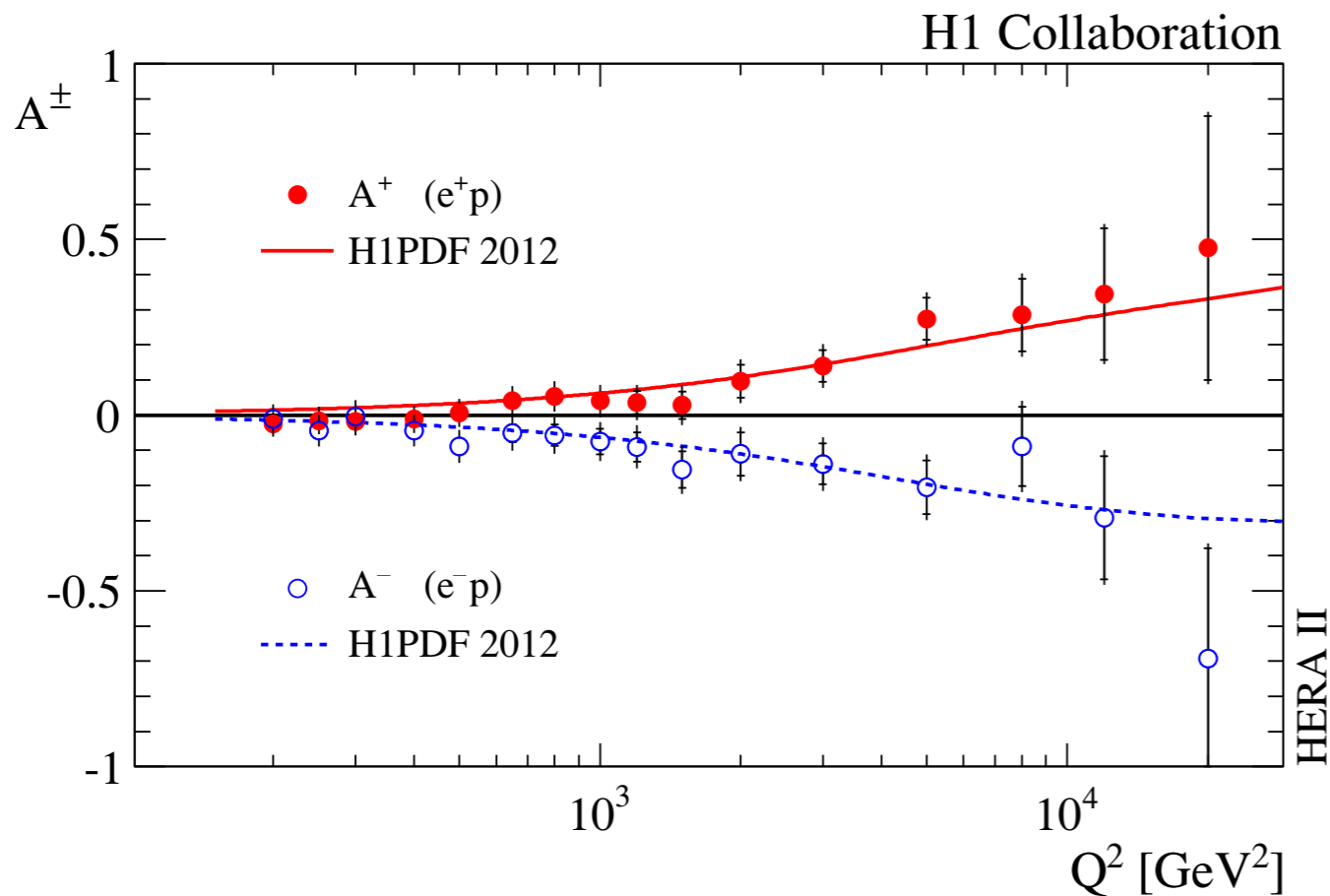
Polarised NC measurements completed for e^+p , e^-p , L-handed, R-handed scattering
 Difference in L,R scattering visible at high Q^2



NC polarisation asymmetry:

$$A^{\pm} = \frac{2}{P_L^{\pm} - P_R^{\pm}} \cdot \frac{\sigma^{\pm}(P_L^{\pm}) - \sigma^{\pm}(P_R^{\pm})}{\sigma^{\pm}(P_L^{\pm}) + \sigma^{\pm}(P_R^{\pm})}$$

At large x $A^{\pm} \propto \pm \kappa \frac{1 + d_v/u_v}{4 + d_v/u_v}$

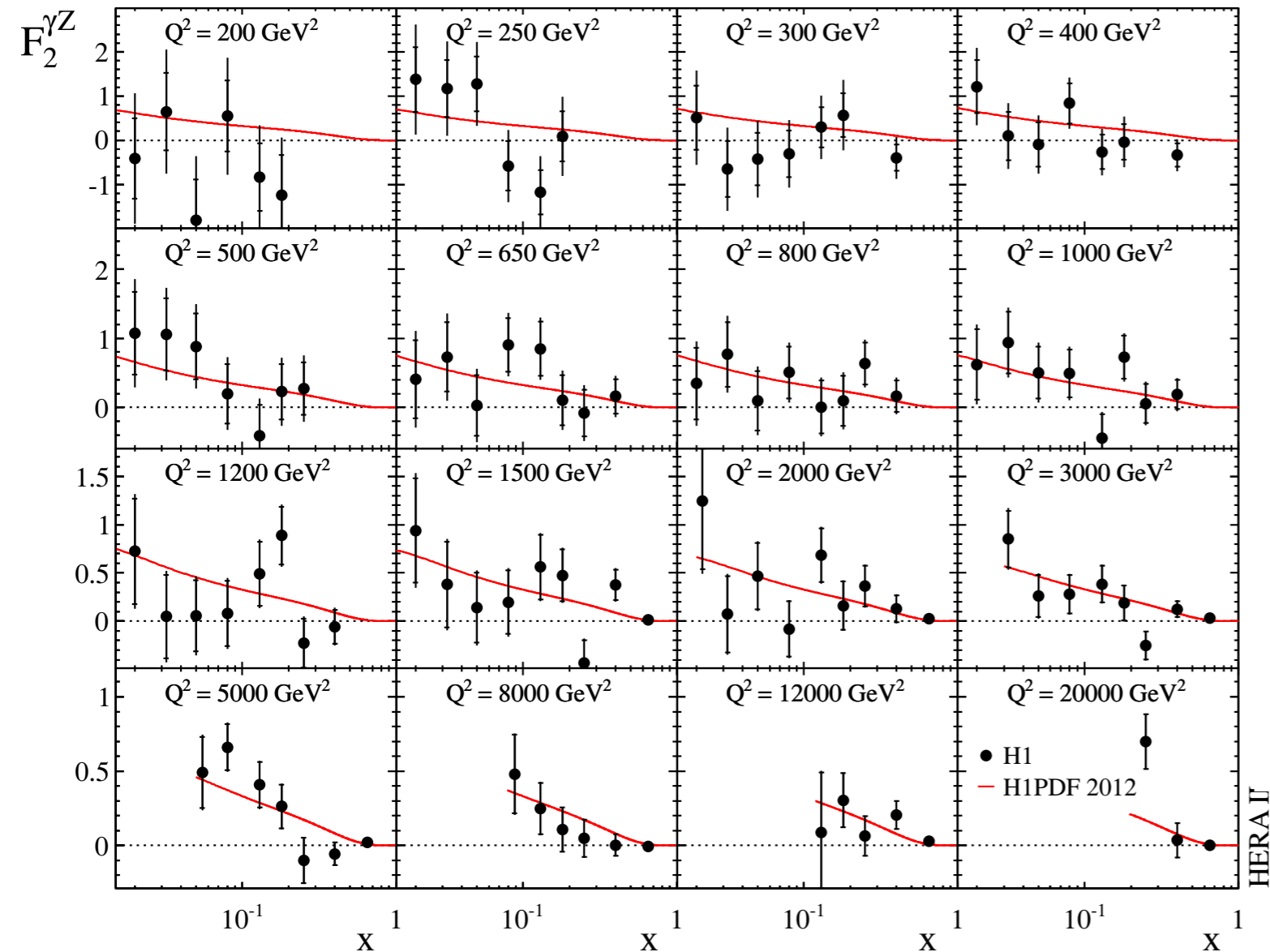


Measuring the difference in NC polarised cross sections gives access to new structure functions:

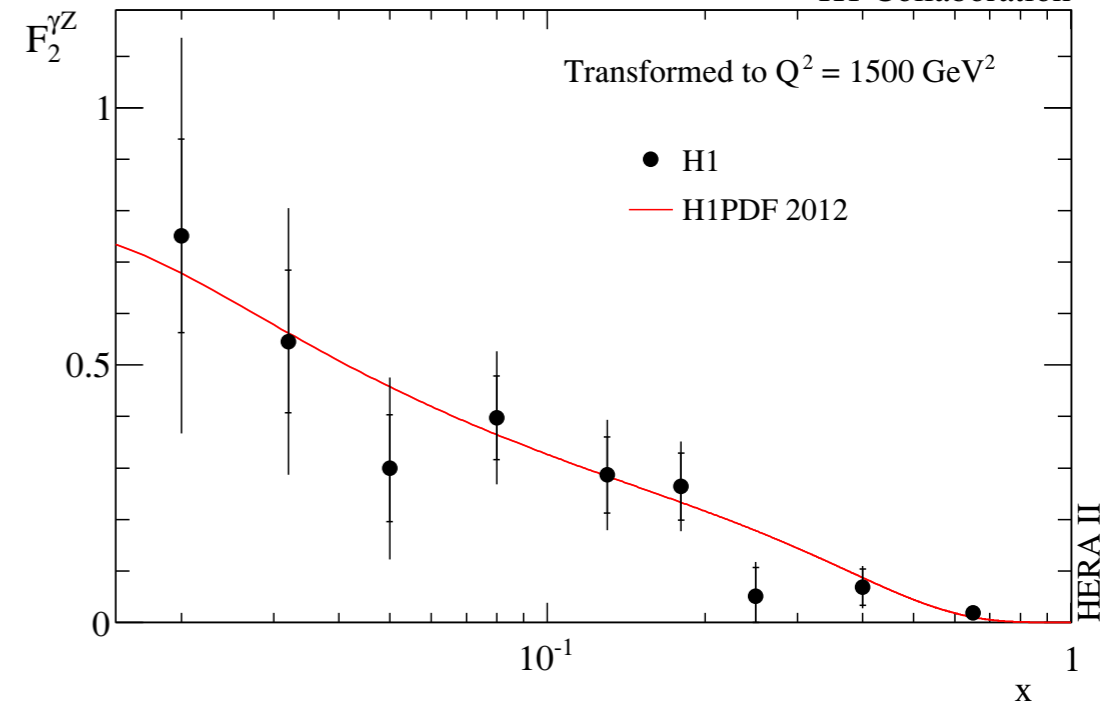
$$\frac{\sigma^\pm(P_L^\pm) - \sigma^\pm(P_R^\pm)}{P_L^\pm - P_R^\pm} = \frac{\kappa Q^2}{Q^2 + M_Z^2} \left[\mp a_e F_2^{\gamma Z} + \frac{Y_-}{Y_+} v_e x F_3^{\gamma Z} - \frac{Y_-}{Y_+} \frac{\kappa Q^2}{Q^2 + M_Z^2} (v_e^2 + a_e^2) x F_3^Z \right]$$

$x F_3$ terms eliminated by subtracted e^-p from e^+p

H1 Collaboration



H1 Collaboration



New H1 data are combined with all previously published H1 inclusive cross section measurements

854 data points averaged to 413 measurements

$$\chi^2/\text{ndf} = 412/441 = 0.93$$

Normalisation shifts for H1 data after averaging

Source	Shift in units of standard deviation	Shift in % of cross section
$\delta\mathcal{L}^1$ (BH Theory)	-0.39	-0.19
$\delta\mathcal{L}^2$ (e^+ 94-97)	-0.46	-0.66
$\delta\mathcal{L}^3$ (e^- 98-99)	-0.69	-1.20
$\delta\mathcal{L}^4$ (e^+ 99-00)	-0.07	-0.10
$\delta\mathcal{L}^5$ (QEDC)	0.81	1.70
$\delta\mathcal{L}^6, \delta\mathcal{L}^7$ ($e^+L + R$)	0.84	0.80
$\delta\mathcal{L}^8, \delta\mathcal{L}^9$ ($e^-L + R$)	0.84	0.89

Precision medium Q^2
HERA-I data ~unshifted

New high Q^2 HERA-II
data shifted by ~1.7%
(less than 1 std.dev)

New PDF fit performed: can be thought of as a 'stepping-stone' towards HERAPDF2.0

$$\begin{aligned}
 xg(x) &= A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{25}, \\
 xu_v(x) &= A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2), \\
 xd_v(x) &= A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}}, \\
 x\bar{U}(x) &= A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}}, \\
 x\bar{D}(x) &= A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.
 \end{aligned}$$

Parameter	Central Value	Lower Limit	Upper Limit
f_s	0.31	0.23	0.38
m_c (GeV)	1.4	1.35 (for $Q_0^2 = 1.8$ GeV)	1.65
m_b (GeV)	4.75	4.3	5.0
Q_{\min}^2 (GeV ²)	3.5	2.5	5.0
Q_0^2 (GeV ²)	1.9	1.5 ($f_s = 0.29$)	2.5 ($m_c = 1.6, f_s = 0.34$)

13 parameter fit: additional flexibility given to u_v and d_v compared to H1PDF2009 / HERAPDF1.0

Apply momentum/counting sum rules:

$$\begin{aligned}
 \int_0^1 dx \cdot (xu_v + xd_v + x\bar{U} + x\bar{D} + xg) &= 1 \\
 \int_0^1 dx \cdot u_v &= 2 \quad \int_0^1 dx \cdot d_v = 1
 \end{aligned}$$

Parameter constraints:

$$\begin{aligned}
 B_{\text{Ubar}} &= B_{\text{Dbar}} \\
 \text{sea} &= 2 \times (\text{Ubar} + \text{Dbar}) \\
 \text{Ubar} &= \text{Dbar at } x=0 \\
 f_s &= \text{sbar/Dbar}
 \end{aligned}$$

$$Q_0^2 = 1.9 \text{ GeV}^2 \text{ (below } m_c)$$

$$Q^2 > 3.5 \text{ GeV}^2$$

$$2 \times 10^{-4} < x < 0.65$$

Fits performed using RT-VFNS

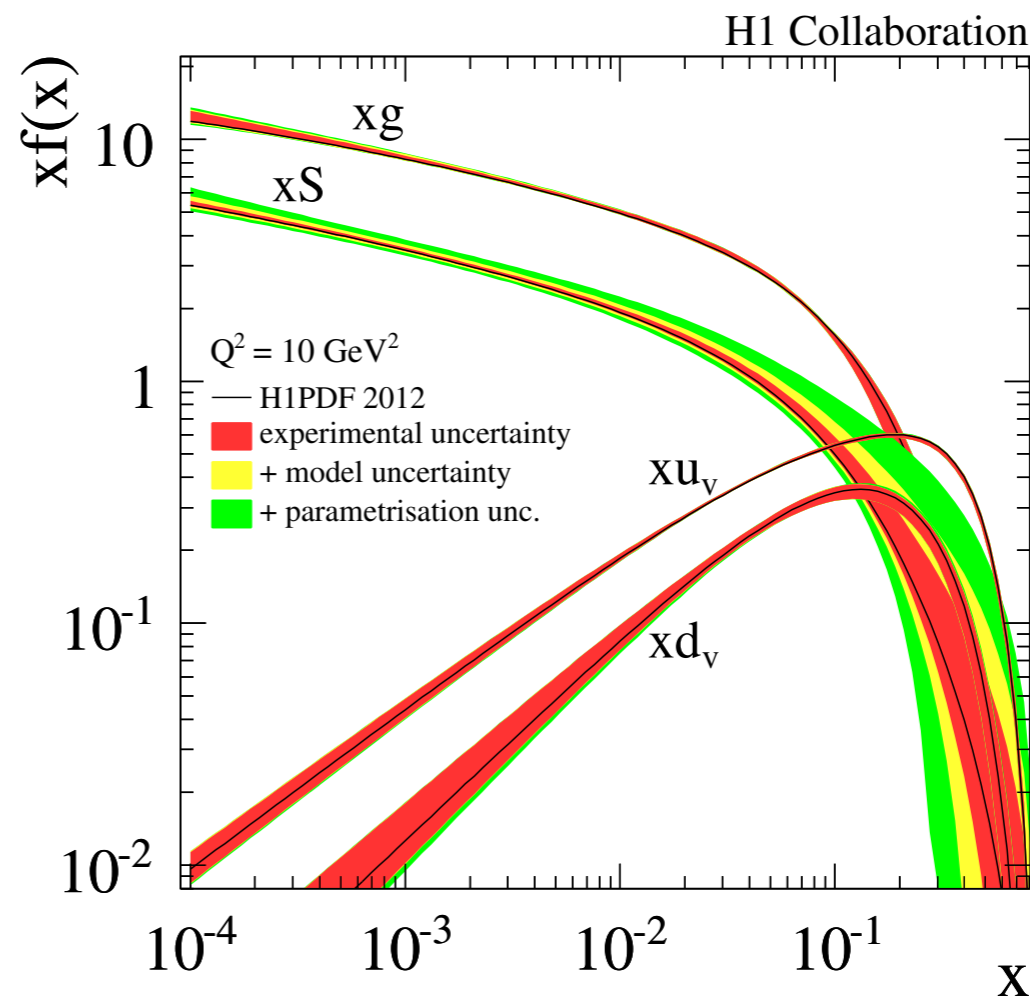
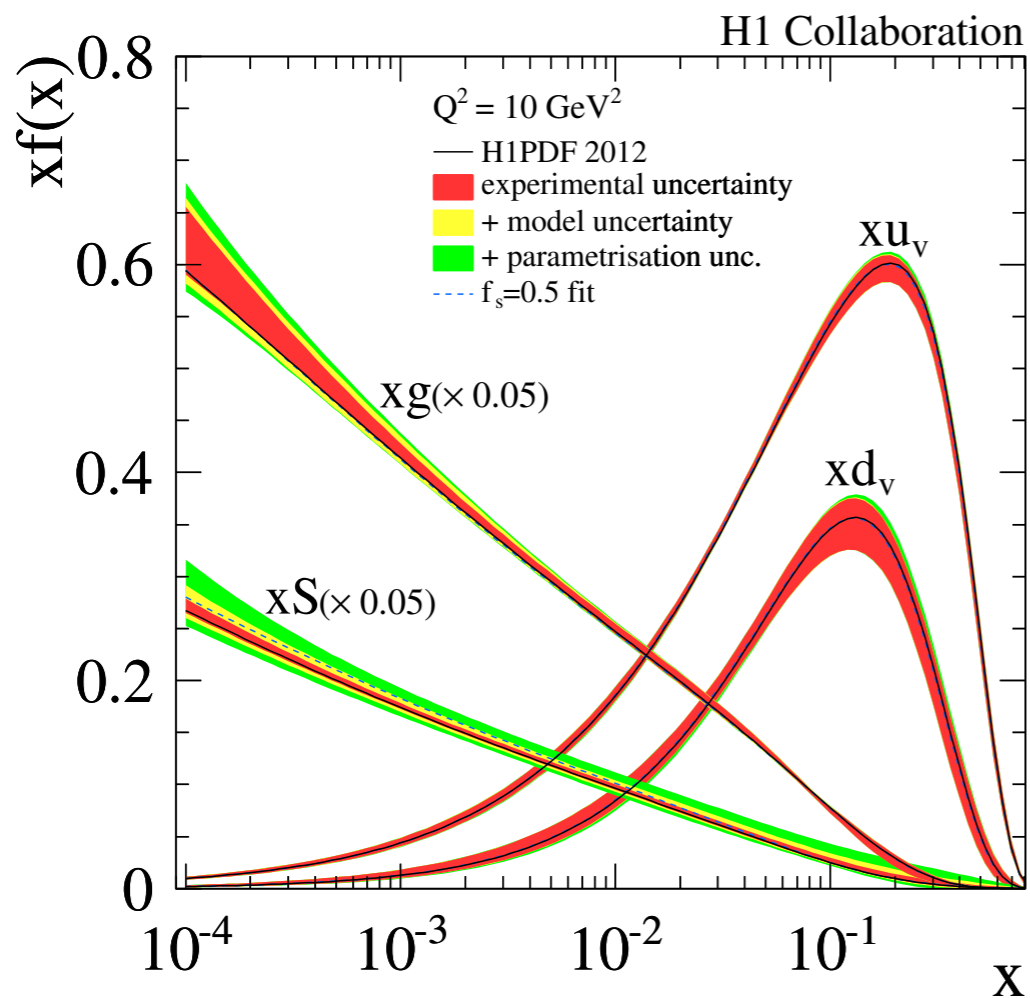
Experimental uncertainties produced using RMS spread of 400 replica fits

Parameterisation uncertainty determined from envelope of 14 parameter fit & Q_0^2 variations

Error band is applied to central value fit \Rightarrow asymmetric errors since mean of replicas \neq central fit

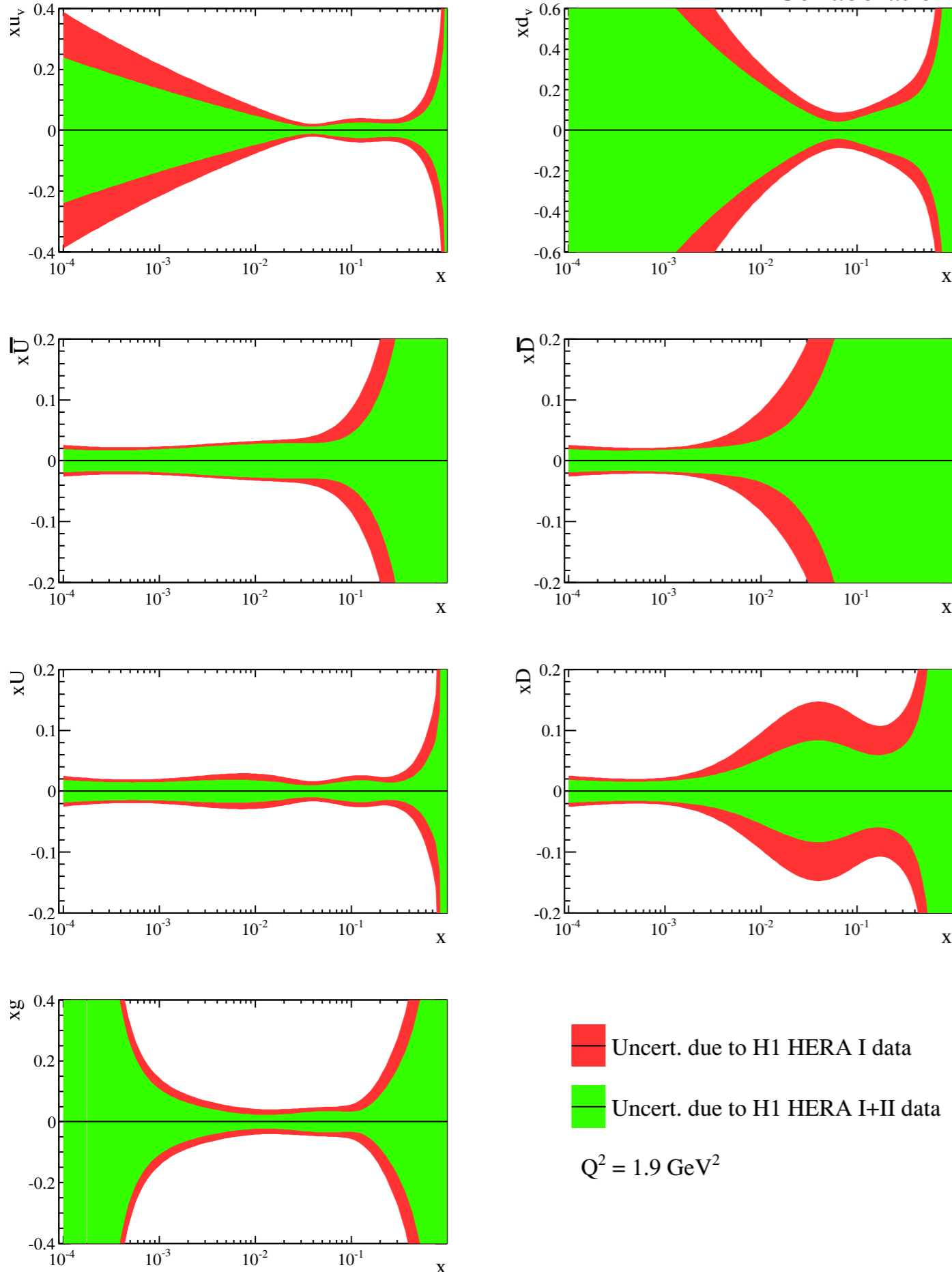
$$\chi^2 = \sum_i \frac{\left[\mu_i - m_i \left(1 - \sum_j \gamma_j^i b_j \right) \right]^2}{\delta_{i,\text{unc}}^2 m_i^2 + \delta_{i,\text{stat}}^2 \mu_i m_i \left(1 - \sum_j \gamma_j^i b_j \right)} + \sum_j b_j^2 + \sum_i \ln \frac{\delta_{i,\text{unc}}^2 m_i^2 + \delta_{i,\text{stat}}^2 \mu_i m_i}{\delta_{i,\text{unc}}^2 \mu_i^2 + \delta_{i,\text{stat}}^2 \mu_i^2}$$

modified χ^2 definition includes ln term to account for likelihood transition to χ^2 after error scaling



$$\chi^2/\text{ndf} = 1570/1461 = 1.07$$

Fit with unsuppressed strange sea ($f_s=0.5$) is well within error bands



Comparison of PDF uncertainties from H1 fits with and without new HERA-II data

Large improvement in $x d_v$ and $x D$ over wide x range - driven by more precise CC e^+p data

Improvement in $x u_v$ from NC at high x . Error reduction at low x arises from sum rules

High x gluon is also improved from scaling violations



HERAPDF1.0

Combine NC and CC HERA-I data from H1 & ZEUS
Complete MSbar NLO fit
NLO: standard parameterisation with 10 parameters
 $\alpha_s = 0.1176$ (fixed in fit)

HERAPDF1.5

Include additional NC and CC HERA-II data
Complete MSbar NLO and NNLO fit
NLO: standard parameterisation with 10 parameters

HERAPDF1.5f

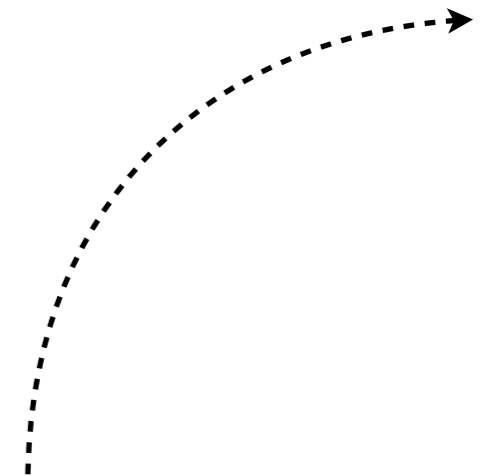
NNLO: extended fit with 14 parameters

HERAPDF1.6

Include additional NC inclusive jet data $5 < Q^2 < 15000$
Complete MSbar NLO fit
NLO: standard parameterisation with 14 parameters
 $\alpha_s = 0.1202 \pm 0.0013$ (exp) ± 0.004 (scales) free in fit

HERAPDF1.7

Include 41 additional F_2^{cc} data $4 < Q^2 < 1000$
Include 224 combined cross section points $E_p=575/460$ GeV
Complete MSbar NLO fit
NLO: standard parameterisation with 14 parameters



HERAPDF2.0

Include final:

HERA-I low/medium Q^2 precision F_2

HERA-II high Q^2 polarised NC/CC data

HERA-II low/medium energy NC data

HERA-I+II F_2^{cc} combined data - almost ready

HERA-I+II multijet data - awaiting H1 publication

Combined F_2^{cc} now at 2nd stage of internal review

Expect journal submission ~ early Nov.

Final structure function measurements from H1 / ZEUS now published

Combination of the data is underway

New combination will include:

HERA-I published data

HERA-II published data

low/medium energy $E_p=575/460$ GeV run data

Expect several fits:

NLO vs NNLO

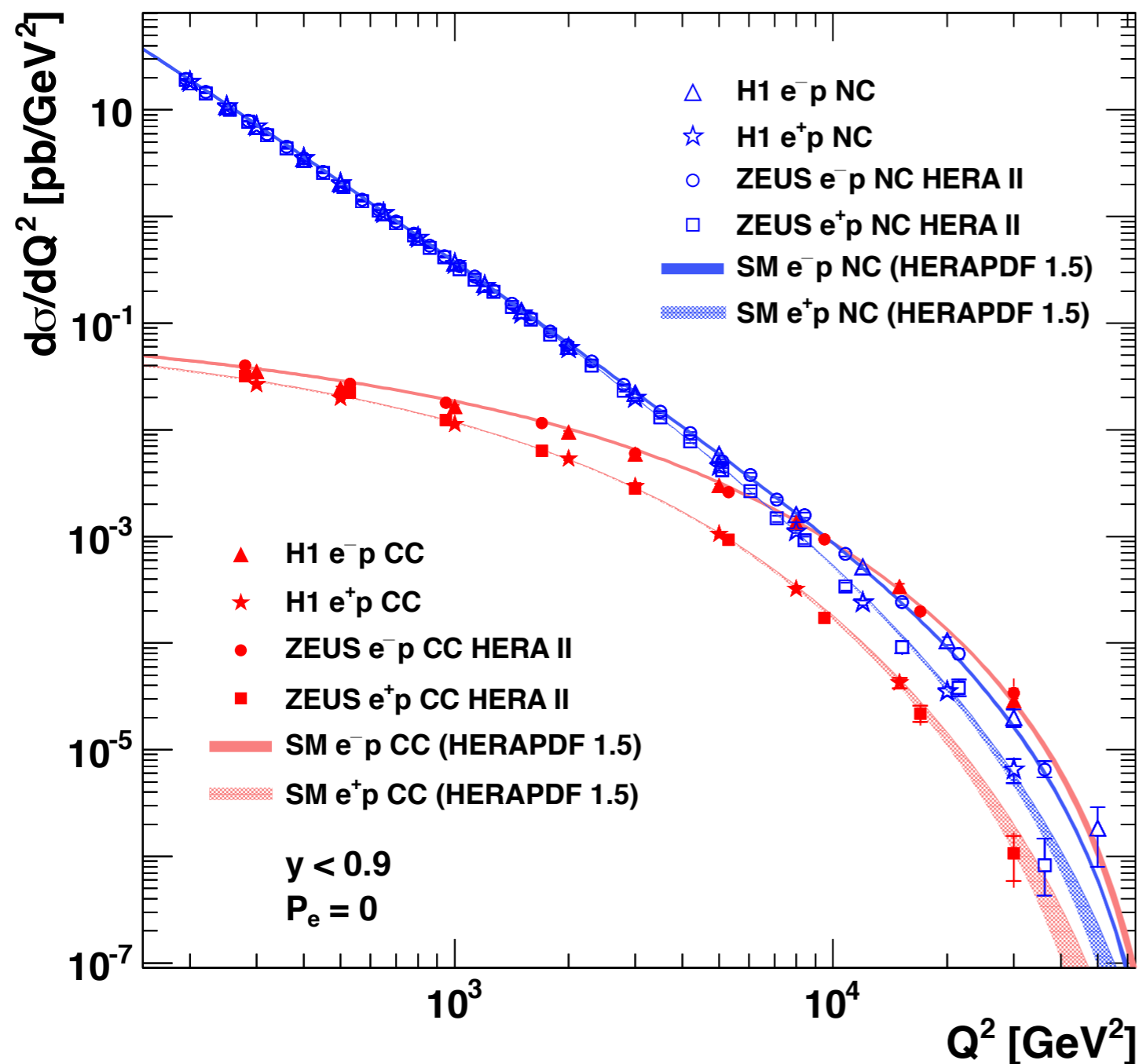
NLO will be: inclusive NC/CC data & inclusive + F_2^{cc} (+ jets?)

Include fit to α_s

MC method for experimental errors will be used

Timescale ~ spring 2013 (DIS workshop?)

HERA



- H1 / ZEUS completed their final SF measurements
- New HERA-II data provide tighter constraints at high x / Q^2
- These data provide some of the most stringent constraints on PDFs
- Stress-test of QCD over 4 orders of mag. in Q^2
- DGLAP evolution works very well
- HERA data provide a self-consistent data set for complete flavour decomposition of the proton
- New combination of HERA data underway
- Combination \Rightarrow HERAPDF2.0 QCD fit



H1 Systematic Error Source Correlation



Data set	$\delta\mathcal{L}$	δE	$\delta\theta$	δh	δN	δB	δV	δS	δpol
e^+ Combined low Q^2	$\delta\mathcal{L}1$								
e^+ Combined low E_p	$\delta\mathcal{L}1$								
e^+ NC 94-97	$\delta\mathcal{L}1$	$\delta\mathcal{L}2$	$\delta E1$	$\delta\theta1$	$\delta h1$	$\delta N1$	$\delta B1$	—	—
e^+ CC 94-97	$\delta\mathcal{L}1$	$\delta\mathcal{L}2$	—	—	$\delta h1$	$\delta N1$	$\delta B1$	$\delta V1$	—
e^- NC 98-99	$\delta\mathcal{L}1$	$\delta\mathcal{L}3$	$\delta E1$	$\delta\theta2$	$\delta h1$	$\delta N1$	$\delta B1$	—	—
e^- NC 98-99 <i>high y</i>	$\delta\mathcal{L}1$	$\delta\mathcal{L}3$	$\delta E1$	$\delta\theta2$	$\delta h1$	$\delta N1$	—	—	$\delta S1$
e^- CC 98-99	$\delta\mathcal{L}1$	$\delta\mathcal{L}3$	—	—	$\delta h1$	$\delta N1$	$\delta B1$	$\delta V2$	—
e^+ NC 99-00	$\delta\mathcal{L}1$	$\delta\mathcal{L}4$	$\delta E1$	$\delta\theta2$	$\delta h1$	$\delta N1$	$\delta B1$	—	$\delta S1$
e^+ CC 99-00	$\delta\mathcal{L}1$	$\delta\mathcal{L}4$	—	—	$\delta h1$	$\delta N1$	$\delta B1$	$\delta V2$	—
e^+ NC <i>high y</i>	$\delta\mathcal{L}5$	$\delta\mathcal{L}6, \delta\mathcal{L}7$	$\delta E2$	$\delta\theta3$	$\delta h2$	$\delta N2$	—	—	$\delta S2$
e^- NC <i>high y</i>	$\delta\mathcal{L}5$	$\delta\mathcal{L}8, \delta\mathcal{L}9$	$\delta E2$	$\delta\theta3$	$\delta h2$	$\delta N2$	—	—	$\delta S2$
e^+ NC <i>L</i>	$\delta\mathcal{L}5$	$\delta\mathcal{L}6$	$\delta E2$	$\delta\theta3$	$\delta h2$	$\delta N2$	$\delta B1$	—	$\delta P1$
e^+ CC <i>L</i>	$\delta\mathcal{L}5$	$\delta\mathcal{L}6$	—	—	$\delta h2$	$\delta N3$	$\delta B1$	$\delta V3$	$\delta P1$
e^+ NC <i>R</i>	$\delta\mathcal{L}5$	$\delta\mathcal{L}7$	$\delta E2$	$\delta\theta3$	$\delta h2$	$\delta N2$	$\delta B1$	—	$\delta P2$
e^+ CC <i>R</i>	$\delta\mathcal{L}5$	$\delta\mathcal{L}7$	—	—	$\delta h2$	$\delta N3$	$\delta B1$	$\delta V3$	$\delta P2$
e^- NC <i>L</i>	$\delta\mathcal{L}5$	$\delta\mathcal{L}8$	$\delta E2$	$\delta\theta3$	$\delta h2$	$\delta N2$	$\delta B1$	—	$\delta P3$
e^- CC <i>L</i>	$\delta\mathcal{L}5$	$\delta\mathcal{L}8$	—	—	$\delta h2$	$\delta N3$	$\delta B1$	$\delta V3$	$\delta P3$
e^- NC <i>R</i>	$\delta\mathcal{L}5$	$\delta\mathcal{L}9$	$\delta E2$	$\delta\theta3$	$\delta h2$	$\delta N2$	$\delta B1$	—	$\delta P4$
e^- CC <i>R</i>	$\delta\mathcal{L}5$	$\delta\mathcal{L}9$	—	—	$\delta h2$	$\delta N3$	$\delta B1$	$\delta V3$	$\delta P4$

correlation of H1 systematic error sources

$\delta\mathcal{L}1 \rightarrow 0.5\%$ BH theoretical error
HERA-I

$\delta\mathcal{L}5 \rightarrow 2.3\%$ Compton lumi error
HERA-II

$\delta\mathcal{L}6-9 \rightarrow 1.5\%$ Compton unc. error
HERA-II

Data Period	Global Normalisation	Per Period Normalisation	Total Normalisation
e^+ Combined low Q^2	0.993	—	0.993
e^+ Combined low E_p	0.993	—	0.993
HERA I e^+ 94-97	0.993	0.999	0.992
HERA I e^- 98-99	0.993	1.003	0.996
HERA I e^+ 99-00	0.993	1.005	0.998
HERA II e^+ L	1.029	0.991	1.020
HERA II e^+ R	1.029	1.013	1.042
HERA II e^- L	1.029	1.010	1.039
HERA II e^- R	1.029	1.014	1.043

normalisations from HIPDF 2012

Low Q^2 data shifted by -0.7%
 HERA-I high Q^2 by -0.3%
 HERA-II high Q^2 by +2 to +4%

All shifts are <1.3 std.devs

HERAPDF1.0

Combine NC and CC HERA-I data from H1 & ZEUS

Complete MSbar NLO fit

NLO: standard parameterisation with 10 parameters

 $\alpha_s = 0.1176$ (fixed in fit)HERAPDF1.5

Include additional NC and CC HERA-II data

Complete MSbar NLO and NNLO fit

NLO: standard parameterisation with 10 parameters

HERAPDF1.5f

NNLO: extended fit with 14 parameters

desy-09-158

H1-10-142 / ZEUS-prel-10-018

$$xf(x, Q_0^2) = A \cdot x^B \cdot (1-x)^C \cdot (1 + Dx + Ex^2)$$

xg		xg		$xg(x) = A_g x^{B_g} (1-x)^{C_g},$
xu_v	\longrightarrow	$xU = xu + xc$	\longrightarrow	$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2),$
xd_v	\longrightarrow	$xD = xd + xs$	\longrightarrow	$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}},$
$x\bar{U}$		$x\bar{U} = x\bar{u} + x\bar{c}$		$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}},$
$x\bar{D}$		$x\bar{D} = x\bar{d} + x\bar{s}$		$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}},$

 $x\bar{s} = f_s x\bar{D}$ strange sea is a fixed fraction f_s of \bar{D} at Q_0^2

Apply momentum/counting sum rules:

$$\int_0^1 dx \cdot (xu_v + xd_v + x\bar{U} + x\bar{D} + xg) = 1$$

$$\int_0^1 dx \cdot u_v = 2 \quad \int_0^1 dx \cdot d_v = 1$$

Parameter constraints:

$B_{uv} = B_{dv}$

$B_{Ubar} = B_{Dbar}$

sea = 2 x (Ubar + Dbar)

Ubar = Dbar at $x=0$

$Q_0^2 = 1.9 \text{ GeV}^2$ (below m_c)

$Q^2 > 3.5 \text{ GeV}^2$

$2 \times 10^{-4} < x < 0.65$

Fits performed using RT-VFNS

HERAPDF1.0 central values:

	A	B	C	E
xg	6.8	0.22	9.0	
xu_v	3.7	0.67	4.7	9.7
xd_v	2.2	0.67	4.3	
$x\bar{U}$	0.113	-0.165	2.6	
$x\bar{D}$	0.163	-0.165	2.4	

$$\chi^2 / \text{ndf} = 574/582$$

Exclusive jet data required for free α_s fit
See talk of Krzysztof Nowak

Experimental systematic sources of uncertainty allowed to float in fit
Include model assumptions into uncertainty:

$f_s, m_c, m_b, Q_0^2, Q_{min}^2$

Variation	Standard Value	Lower Limit	Upper Limit
f_s	0.31	0.23	0.38
m_c [GeV]	1.4	1.35 ^(a)	1.65
m_b [GeV]	4.75	4.3	5.0
Q_{min}^2 [GeV ²]	3.5	2.5	5.0
Q_0^2 [GeV ²]	1.9	1.5 ^(b)	2.5 ^(c,d)

$$^{(a)}Q_0^2 = 1.8$$

$$^{(c)}m_c = 1.6$$

$$^{(b)}f_s = 0.29$$

$$^{(d)}f_s = 0.34$$

Excellent consistency of input data allow standard statistical error definition:

$$\Delta\chi^2 = 1$$

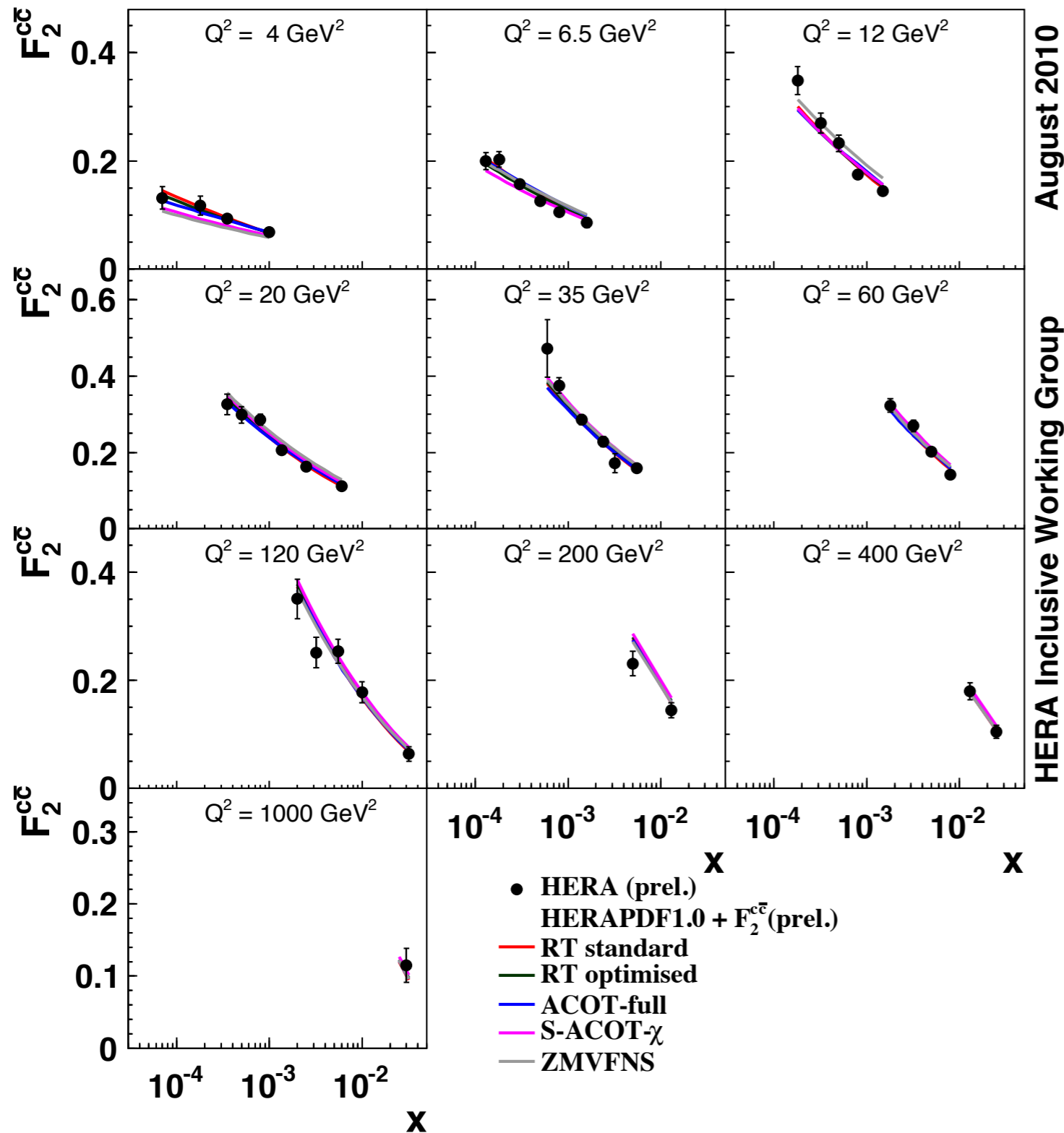
In 14 parameter fit:

release $B_{uv} = B_{dv}$ constraint

allow more flexible gluon

$$xg(x, Q_0^2) = A \cdot x^B \cdot (1-x)^C - A' \cdot x^{B'} \cdot (1-x)^{25}$$

allows for valence-like or negative gluon at Q_0^2



The inclusive charm content of proton can be measured in several methods: D^* decays, impact parameter significance...
Combination yields $\sim 5\text{-}10\%$ precision

Data cover wide phase space region including charm threshold region

Theory predictions have small spread \Rightarrow use optimised m_c parameter

Spread of LHC Z/W production predictions is reduced $\sim 4.5\% \rightarrow \sim 0.7\%$ when using optimal value of m_c

ZEUS inclusive jets	39 pb ⁻¹	Q ² > 125	Nucl. Phys. B765 (2007) 1-30
ZEUS inclusive jets	82 pb ⁻¹	Q ² > 125	Phys. Lett. B649 (2007) 12
H1 inclusive jets	395 pb ⁻¹	150 < Q ² < 15000	EPJ C65 (2010) 363-383
H1 inclusive jets	44 pb ⁻¹	5 < Q ² < 100	EPJ C67 (2010) 1-24

Jet data bring significant sensitivity to α_s
 Disentangles correlation between $xg(x, Q^2)$ and α_s

HERAPDF1.6 : Simultaneous NLO QCD fit to

- combined NC inclusive cross section data
- combined CC inclusive cross sections data
- normalised H1/ZEUS inclusive jet data

$$\alpha_s(M_Z) = 0.1202 \pm 0.0013 \text{ (exp)}$$

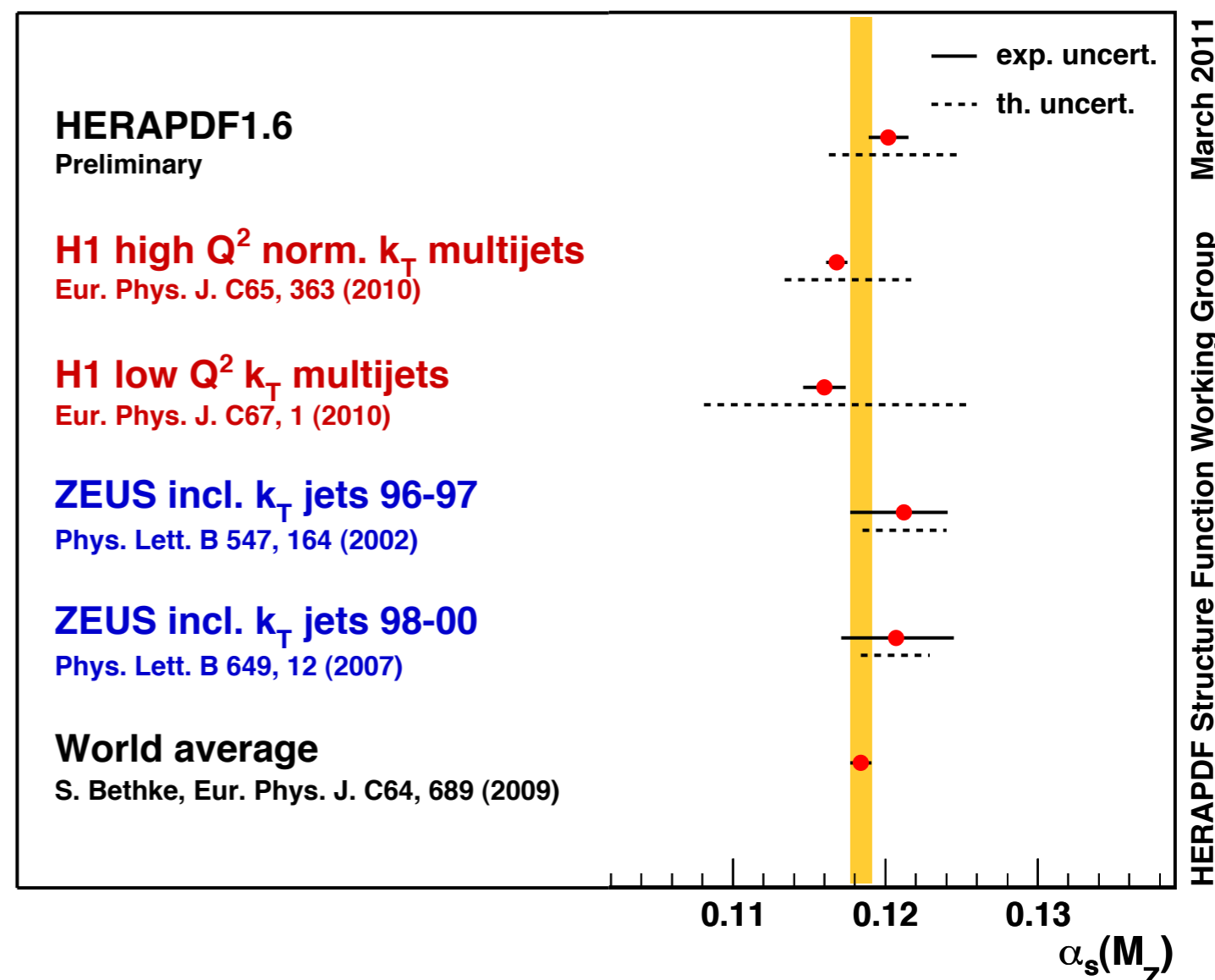
$$\pm 0.0007 \text{ (model)}$$

$$\pm 0.0012 \text{ (hadronisation)}$$

$$\begin{matrix} +0.0045 \\ -0.0036 \end{matrix} \text{ (scales)}$$

Only combined PDF / α_s fit on the market

H1 and ZEUS (prel.)



High Q^2 NC Multi-jets



H1prelim-I I-032

New H1 measurement of inclusive, dijet and trijet rates
 First measurement of double diff'l trijet cross section

Significantly reduced systematic errors

1% hadronic scale uncertainty

For now - unnormalised cross sections...

Jets in Breit frame: $5 < P_T < 50$ GeV
 $M_{12} > 16$ GeV

Greater sensitivity to α_s with more jets

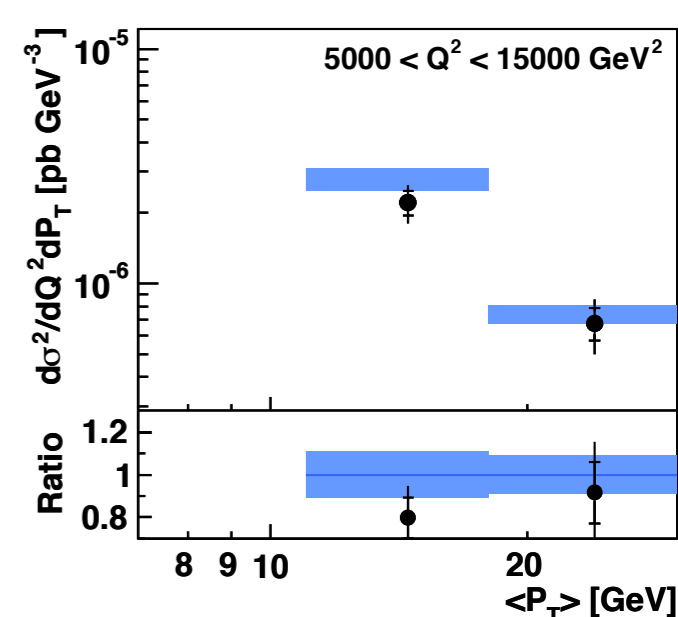
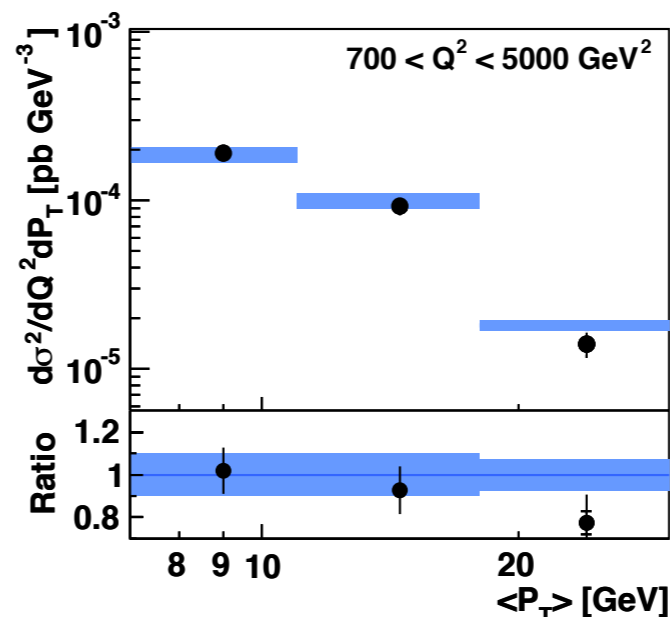
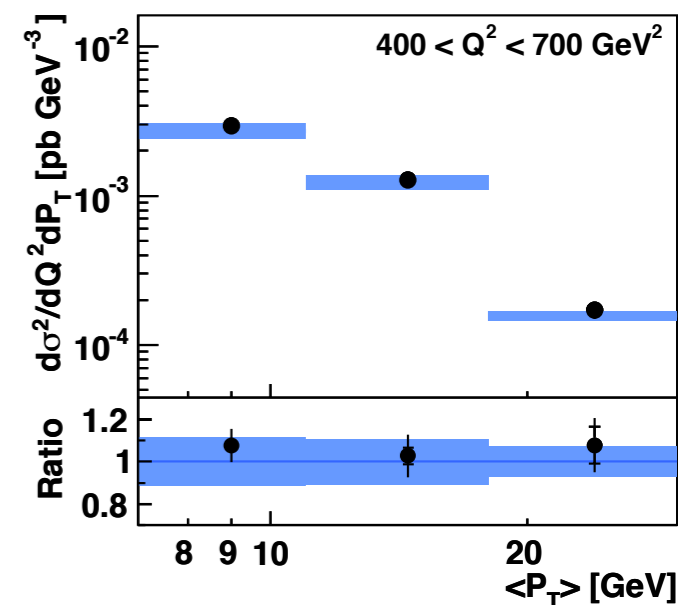
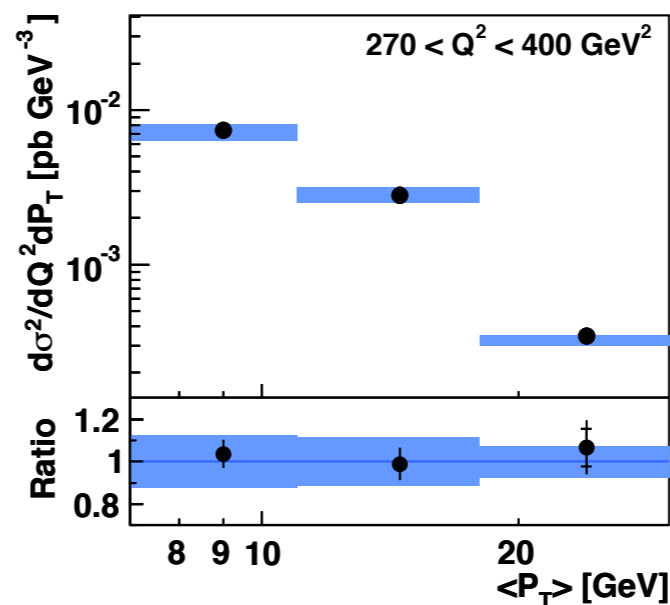
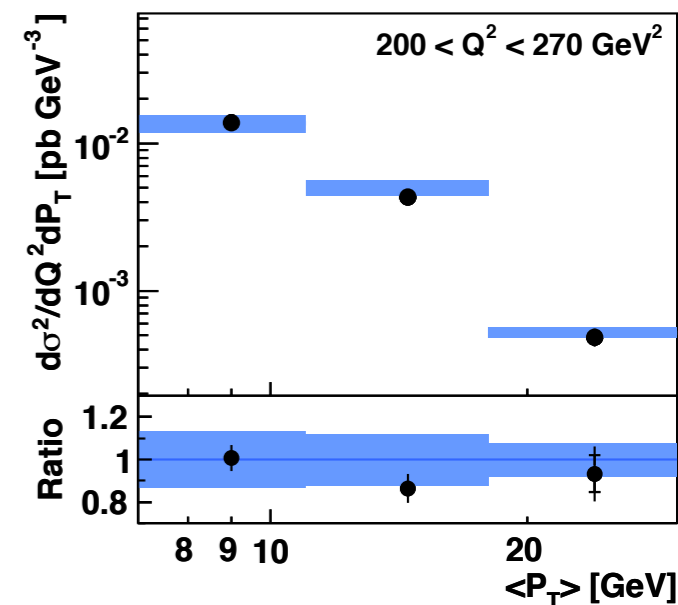
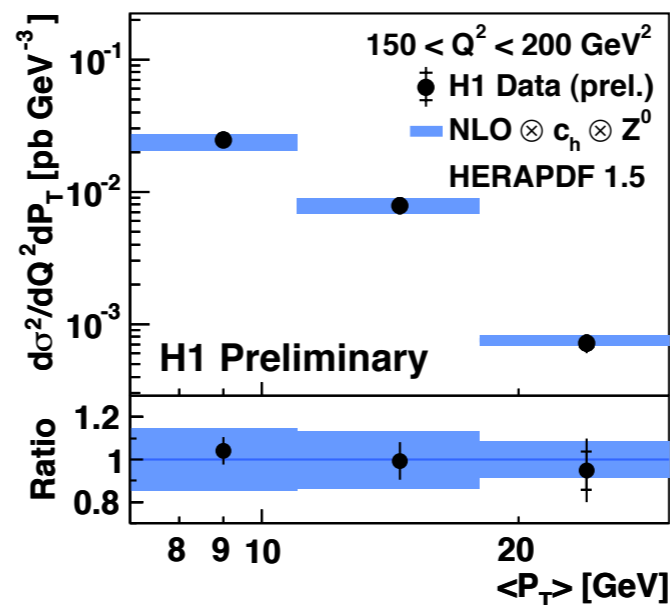
High Q^2 and large jet $P_T \Rightarrow$ multi-scale QCD problem

Good description in NLO

(worse for di-jets at low $\langle P_T \rangle$...)

NLO calculation $\mu_R = \mu_F = \sqrt{\frac{1}{2}(Q^2 + P_T^2)}$
 scales varied by factors of 2 for uncertainty

Trijet Cross Section



High Q^2 NC Multi-jets



H1prelim-I I-032

Di-jet rates in reasonable agreement
 $\sim 10\%$ discrepancy at low $\langle P_T \rangle$
 Data want smaller α_s or smaller x_g ?

Extract α_s independently for each jet data set in NLO
 PDF uncertainty from CT10 error propagation

Inclusive jets:

$$\alpha_s(M_Z) = 0.1190 \pm 0.0021(\text{exp.}) \pm 0.0020(\text{pdf})^{+0.0050}_{-0.0056}(\text{th.})$$

Dijets:

$$\alpha_s(M_Z) = 0.1146 \pm 0.0022(\text{exp.}) \pm 0.0021(\text{pdf})^{+0.0044}_{-0.0045}(\text{th.})$$

Trijets:

$$\alpha_s(M_Z) = 0.1196 \pm 0.0016(\text{exp.}) \pm 0.0010(\text{pdf})^{+0.0055}_{-0.0039}(\text{th.})$$

Achieved $\sim 1\%$ experimental precision on α_s
 Theoretical uncertainty (scales) dominate $\sim 4\%$
 PDF uncertainty $\sim 1\%$

To come:

Use of normalised cross sections
 cancellation of systematic uncertainties
 \rightarrow reduced error for α_s

Dijet Cross Section

